

**Research on Load-Independent Design  
for High-Frequency Resonant Inverters  
and Rectifiers**

**February 2025**

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Graduate School of Science and Engineering  
CHIBA UNIVERSITY

(千葉大学審査学位論文)

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# Table of Contents

<b>Acknowledgement</b>	<b>1</b>
<b>Chapter 1 General Introduction</b>	<b>2</b>
1.1 Research Background . . . . .	2
1.2 Research Work . . . . .	6
1.3 Thesis Outline . . . . .	7
<b>Chapter 2 High-Frequency Resonant Circuits</b>	<b>15</b>
2.1 Class-E Inverter . . . . .	16
2.1.1 Circuit Topology . . . . .	16
2.1.2 Operating Principle . . . . .	16
2.2 Class-E Rectifier . . . . .	17
2.2.1 Circuit Topology . . . . .	17
2.2.2 Operating Principle . . . . .	18
2.3 Class-E Power Oscillator . . . . .	18
2.3.1 Circuit Topology . . . . .	18
2.3.2 Operating Principle . . . . .	19
2.4 Class-E Synchronous Rectifier . . . . .	19
2.5 Load-Independent Class-E Inverter . . . . .	20

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2.5.1	Challenge in Class-E Resonant Circuits . . . . .	20
2.5.2	Circuit Topology . . . . .	20
2.5.3	Operating Principle . . . . .	21
<b>Chapter 3 Load-Independent Class-E<sup>-1</sup> Inverter With Constant Current</b>		<b>28</b>
3.1	Introduction . . . . .	28
3.2	Load-Independent Inverter With CC-SR Property . . . . .	31
3.2.1	Load-Independent Class-EF Inverter . . . . .	31
3.2.2	Proposed Inverter . . . . .	32
3.3	Analysis of Proposed Inverter . . . . .	33
3.3.1	Waveform Derivation . . . . .	35
3.3.2	Boundary Condition . . . . .	36
3.3.3	Load-Independent Condition . . . . .	37
3.3.4	SR Output Filter . . . . .	38
3.3.5	Inverter Characteristics . . . . .	39
3.3.6	Circuit Design for Maximum Power-Output Capability . . . . .	39
3.3.7	Circuit Design for Reducing Switching Loss . . . . .	40
3.4	Application for WPT . . . . .	42
3.4.1	System Configuration . . . . .	42
3.4.2	Analytical Expressions of Proposed WPT System . . . . .	42
3.5	Experimental Results . . . . .	44
3.5.1	Experimental Prototype . . . . .	44
3.5.2	Operating Waveform . . . . .	46

---

3.5.3	Circuit Characteristics . . . . .	47
3.6	Comparison With Previous Works . . . . .	50
3.7	Conclusion . . . . .	51
<b>Chapter 4 Load-Independent Class-<math>\Phi_3</math> Inverter</b>		<b>75</b>
4.1	Introduction . . . . .	75
4.2	Load-Independent Inverters . . . . .	77
4.2.1	Load-Independent Class- $\Phi_2$ Inverter . . . . .	78
4.2.2	Load-Independent Class- $\Phi_3$ Inverter . . . . .	78
4.3	Circuit Analysis . . . . .	79
4.3.1	Waveform equations . . . . .	80
4.3.2	Boundary Conditions . . . . .	81
4.3.3	Design Conditions . . . . .	82
4.4	Experimental Verification . . . . .	83
4.5	Performance Comparison . . . . .	85
4.6	Conclusion . . . . .	86
<b>Chapter 5 Load-Independent Class-<math>E^{-1}</math> Power Oscillator</b>		<b>99</b>
5.1	Load-Independent CC/ZCS inverter . . . . .	101
5.2	Proposed oscillator . . . . .	102
5.3	Circuit design . . . . .	103
5.4	Experimental verifications . . . . .	104
5.5	Conclusion . . . . .	106
<b>Chapter 6 Load-Independent Class-E Power Oscillator</b>		<b>118</b>

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6.1	Introduction . . . . .	118
6.2	Conventional Class-E Power Oscillator . . . . .	120
6.3	Load-Independent Class-E Power Oscillator . . . . .	121
6.4	Circuit Analysis . . . . .	123
6.4.1	LCCL filter . . . . .	124
6.4.2	Equivalent Class-E Inverter . . . . .	126
6.4.2.1	Waveform Equations . . . . .	126
6.4.2.2	Boundary Condition . . . . .	128
6.4.2.3	Design Condition . . . . .	129
6.4.2.4	Circuit Characteristics . . . . .	130
6.5	Experimental Verification . . . . .	131
6.5.1	Circuit Design for Proposed Power Oscillator . . . . .	131
6.5.2	Experimental Results for Class-E Power Oscillator . . . . .	133
6.5.3	Experimental Results for Proposed Power Oscillator . . . . .	134
6.5.4	Circuit Characteristics . . . . .	135
6.6	Conclusion . . . . .	136
<b>Chapter 7 Load-Independent Class-E Synchronous Rectifier</b>		<b>153</b>
7.1	Introduction . . . . .	153
7.2	Proposed Rectifier . . . . .	154
7.3	Circuit Analysis . . . . .	155
7.4	Experimental Verifications . . . . .	156
7.5	Conclusion . . . . .	157

<b>Chapter 8 Overall Conclusion and Future Work</b>	<b>166</b>
8.1 Overall Conclusion . . . . .	166
8.2 Future Work . . . . .	168

# List of Figures

1.1	Outline of this thesis. (black characters show the conventional re- search, and red characters show my proposal.) . . . . .	11
2.1	Class-E inverter. (a) Circuit topology. (b) Typical waveform. . . . .	22
2.2	Class-E rectifier. (a) Circuit topology. (b) Typical waveform. . . . .	23
2.3	Class-E power oscillator. (a) Circuit topology. (b) Typical waveform. . . . .	24
2.4	Circuit topology of the synchronous class-E rectifier. . . . .	25
2.5	Load-independent class-E inverter. (a) Circuit topology. (b) Typical waveform. (solid line: rated load condition, dashed line: varied load condition.) . . . . .	26
3.1	The load-independent class-EF inverter. (a) Circuit topology. (b) Example waveforms at fixed load resistances (solid line: $R/R_r = 1$ , dashed line: $R/R_r = 0.1$ .) . . . . .	52
3.2	Proposed inverter. (a) Circuit topology. (b) Example waveforms for fixed load resistances (solid line: $R/R_r = 1$ , dashed line: $R/R_r = 0.1$ .) . . . . .	53
3.3	Analytical model of the proposed inverter. . . . .	54

---

3.4	The circuit parameters that satisfy the load-independent conditions as functions of duty ratio $D$ . (a) The normalized resonant angular frequency $\omega_S^*$ . (b) The phase shift between output current and gate-drive voltage. . . . .	55
3.5	Inverter characteristics as functions of duty ratio $D$ and normalized shunt capacitance $\gamma_S$ . (a) Switch-voltage stress $V_{Smax}^*$ . (b) Switch-current stress $I_{Smax}^*$ . (c) Power-output capability. . . . .	56
3.6	Design curves of the proposed inverter as functions of duty ratio $D$ . (a) Normalized inductance $\lambda_b$ . (b) Normalized output-current amplitude $I_m^*$ . . . . .	57
3.7	The example waveforms of switch current and voltage of the proposed inverter. . . . .	58
3.8	The circuit configurations of the WPT system. (a) With the load-independent class-EF inverter. (b) With the proposed inverter. . . . .	59
3.9	The output capacitance of the selected GaN E-HEMT as a function of the switch voltage. . . . .	62
3.10	Photograph of the implemented proposed WPT system. . . . .	63

---

3.11	Experimental and numerical waveforms of the WPT systems. (a) With the load-independent class-EF inverter for $R_L = 100 \Omega$ (Experiment). (b) With the load-independent class-EF inverter for $R_L = 1 \text{ k}\Omega$ (Experiment). (c) With the load-independent class-EF inverter for open load (Experiment). (d) With the proposed inverter for $R_L = 100 \Omega$ (Experiment). (e) With the proposed inverter for $R_L = 1 \text{ k}\Omega$ (Experiment). (f) With the proposed inverter for open load (Experiment). (g) With the proposed inverter for $R_L = 100 \Omega$ (Numerical). (h) With the proposed inverter for $R_L = 1 \text{ k}\Omega$ (Numerical). (i) With the proposed inverter for open load (Numerical). . . . .	64
3.12	Experimental characteristics of the WPT system with the load-independent class-EF and the proposed inverters as a function of normalized load resistance. (a) Amplitude of the current $i_1$ and output voltage $V_O$ . (b) Power-delivery efficiency $\eta$ . . . . .	65
3.13	Power-loss breakdown of the WPT system with the proposed inverter for $R_L = 100 \Omega$ and $R_L = 1 \text{ k}\Omega$ . . . . .	66
3.14	The THD of the output current as a function of normalized load resistance. . . . .	67
4.1	Circuit topology of the load-independent class- $\Phi_2$ and class- $\Phi_3$ inverters.	87
4.2	Example waveforms for fixed load resistance (solid line: $R_L/R_{Lr} = 1$ , dashed line: $R_L/R_{Lr} = 10$ ). (a) Load-independent class- $\Phi_2$ inverter. (b) Load-independent class- $\Phi_3$ inverter. . . . .	88
4.3	Analytical circuit model of the class- $\Phi_3$ inverter. . . . .	89

---

4.4	Photo of the implemented load-independent class- $\Phi_3$ inverter. . . . .	92
4.5	Superimposed experimental and analytical waveforms for fixed load resistance (solid line: experiment, dashed line: analytical). (a)-(c) Load-independent class- $\Phi_2$ inverter. (d)-(f) Load-independent class- $\Phi_3$ inverter. (a) and (d) For $R_L/R_{Lr} = 1$ . (b) and (e) For $R_L/R_{Lr} = 5$ . (c) and (f) For $R_L/R_{Lr} = 10$ . . . . .	93
4.6	Circuit characteristics as a function of normalized load resistance. (a) Normalized output-voltage amplitude. (b) Power-conversion efficiency. . . . .	94
5.1	The load-independent CC/ZCS inverter. (a) Circuit topology. (b) Operating waveforms. (Black line: $R_L/R_{Lr} = 1$ and blue line: $R_L/R_{Lr} = 0.1$ .) . . . . .	107
5.2	The switch-current waveforms against variations in resonant inductance for fixed load resistance. (a) For load-independent CC/ZCS inverter at $R_L/R_{Lr} = 1$ . (b) For load-independent CC/ZCS inverter at $R_L/R_{Lr} = 0.1$ . (c) For proposed oscillator at $R_L/R_{Lr} = 1$ . (d) For proposed oscillator at $R_L/R_{Lr} = 0.1$ . . . . .	108
5.3	The proposed oscillator. (a) Circuit topology. (b) Operating waveforms. . . . .	109
5.4	Photo of the implemented proposed oscillator. . . . .	111
5.5	The experimental waveforms of the load-independent CC/ZCS inverter against load-resistance variations for fixed resonant inductance. (a) For $L_0/L_{0r} = 0.9$ . (b) For $L_0/L_{0r} = 1$ . (c) For $L_0/L_{0r} = 1.1$ . . . . .	112

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5.6	The waveforms of the proposed oscillator against load-resistance variations for fixed resonant inductance. (a) Analytical waveforms for $L_0/L_{0r} = 0.9$ . (b) Analytical waveforms for $L_0/L_{0r} = 1$ . (c) Analytical waveforms for $L_0/L_{0r} = 1.1$ . (d) Experimental waveforms for $L_0/L_{0r} = 0.9$ . (e) Experimental waveforms for $L_0/L_{0r} = 1$ . (f) Experimental waveforms for $L_0/L_{0r} = 1.1$ . . . . .	113
5.7	The normalized output-current amplitude and the power-conversion efficiency as a function of the load resistance. (a) For $L_0/L_{0r} = 0.9$ . (b) For $L_0/L_{0r} = 1$ . (c) For $L_0/L_{0r} = 1.1$ . . . . .	114
6.1	Circuit topology of the conventional class-E power oscillator. . . . .	137
6.2	Example waveforms of the conventional class-E power oscillator. (solid line: for the nominal state, dashed line: for load variations.) . . . . .	138
6.3	Circuit topology of the load-independent class-E power oscillator. . . . .	139
6.4	Typical waveforms of the load-independent class-E power oscillator. (solid line: $R_L/R_{Lr} = 1$ , dashed line: $R_L/R_{Lr} = 0.1$ .) . . . . .	140
6.5	Analytical circuit model of the proposed power oscillator. (a) Overall circuit. (b) Equivalent inverter model. . . . .	141
6.6	Circuit characteristics as functions of normalized inductance $\omega L_1/R_{Lr}$ . (a) Normalized maximum switch voltage and current. (b) Power-output capability $c_p$ . . . . .	142
6.7	Waveforms of the normalized switch voltage for fixed load resistances. . . . .	143
6.8	Gain $\log_{10}  I_O/V_{eq} $ and phase of the LCCL filter as functions of the frequency. . . . .	145

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6.9	Photo of the implemented load-independent class-E power oscillator. .	146
6.10	Experimental waveforms of the conventional class-E power oscillator for fixed load resistance. (black: $R_L/R_{Lr} = 1$ , blue: $R_L/R_{Lr} = 1.2$ .) .	147
6.11	Superimposed experimental and analytical waveforms of the load- independent class-E power oscillator for fixed load resistance. (solid line: experiment, dashed line: analytical.) (a) $R_L/R_{Lr} = 1$ . (a) $R_L/R_{Lr} = 0.5$ . (c) $R_L/R_{Lr} = 0.1$ . . . . .	148
6.12	Output-current amplitude $I_m$ and power-conversion efficiency $\eta$ as functions of load resistance $R_L$ . . . . .	149
7.1	Proposed rectifier. (a) Circuit topology. (b) Example waveforms for fixed load resistance (solid line: $R_L/R_{Lr} = 1$ , dashed line: $R_L/R_{Lr} =$ 10). . . . .	158
7.2	Equivalent circuit model of the proposed rectifier. . . . .	159
7.3	Circuit configuration of the WPT system with the proposed rectifier for the experimental verifications. . . . .	160
7.4	Experimental waveforms of the WPT system with proposed rectifier for fixed load resistance. (a) For $R_L/R_{Lr} = 1$ . (b) For $R_L/R_{Lr} = 5$ . (c) For $R_L/R_{Lr} = 10$ . . . . .	161
7.5	Output voltage and power-transfer efficiency as functions of normal- ized load resistance. . . . .	163

# List of Tables

3.1	Geometric parameters of transmitter and receiver coils. . . . .	60
3.2	Analytical and measured component values of the WPT systems. . .	61
3.3	Load-independent inverters with CC output feature. . . . .	68
4.1	Analytical and experimental component values. . . . .	90
4.2	Components and devices used on the PCB. . . . .	91
4.3	Comparison between the load-independent class- $\Phi_2$ and class- $\Phi_3$ inverters. . . . .	95
5.1	Analytical and measured component values. . . . .	110
6.1	The specifications for the experimental verifications. . . . .	144
7.1	Component values of the WPT system. . . . .	162

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# Chapter 1

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## General Introduction

### 1.1 Research Background

Today, electric energy has become a fundamental and essential part of human life. Electrical energy can be used in wide range of applications because it can be converted into various type of other energy, such as kinetic, heat, light, and sound. Additionally, electrical energy is well-suited for power conversion and transmission, making it a critical infrastructure in modern society. In order to utilize electrical energy in various applications and scenarios, power converters are necessary. The primary function of power converters is to convert the type of electrical power, such as DC and AC, as well as the voltage and current levels, into the desired form.

Most power converters are based the switching power converter, which uses the switching device in the circuit. The switching devices can switch between short-circuit and open-circuit conditions, which can realize high-efficiency power conversion. As the switching devices play a central role in the switching power converters, the power electronics technology has grown following the development of the switching devices [1]. The switching devices trace their origins to the thyristor

developed in 1956, and have evolved through Gate Turn-Off thyristor (GTO) [2], Metal-Oxide-Semiconductor Field-Effect Transistor (MOSFET) [3], and Insulated Gate Bipolar Transistor (IGBT) [4]. These technological advancements have not only improved the ease of use of the devices but also significantly enhanced their operating frequency and power levels. In recent years, switching devices using wide-bandgap semiconductors such as Gallium Nitride (GaN) and Silicon Carbide (SiC) have garnered attention [5]. The GaN and SiC devices expand the operating range compared to conventional devices, enabling high-frequency operation in the MHz range at power levels up to several kW. Also, the GaN and SiC switching devices are rapidly expanding their market size, with an expected growth rate of 35.80% CAGR, reaching a market size of 5 billion USD by 2032 [6].

With the evolution of the switching devices as a backdrop, high-frequency operation has become one of the key directions in the power converter development. By increasing the switching frequency, the required passive components become smaller, contributing to the miniaturization of overall circuit size. Compact and lightweight circuits are highly demanded in various applications such as AC/DC adapters, in-vehicle power supplies, and portable devices. Moreover, the trend toward higher frequencies also occurs in Wireless Power Transfer (WPT) systems. The standards for WPT, including Qi and AirFuel, have been established, with specifications in the MHz frequency range. In this way, power electronics technology is evolving towards higher frequencies, and it is of great significance in the industrial demand. On the other hand, a technical challenge in increasing the switching frequency is the increase in switching losses. As the switching losses occur with the turn ON and OFF operation, the switching losses increase proportionally with the frequency.

In order to suppress the switching losses, achieving soft switching is an effective measure. By achieving soft switching, the overlap of current and voltage during the switching period can be eliminated, enabling high-efficiency operation even at high frequencies. Therefore, achieving soft switching is an essential design principle for high-frequency switching circuits.

A representative high-frequency soft-switching circuit is the class-E inverter [7]. The class-E inverter achieves Zero-Voltage Switching (ZVS) and Zero-Derivative Switching (ZDS), where both the voltage and its derivative are zero when the switch turns ON. These switching conditions enable high-efficiency power conversion even under high-frequency operation. In addition, the class-E inverter works with a single switching device whose source terminal is connected to a grand. Therefore, the class-E inverter is suitable for high-frequency drives as there is no requirement for high-side gate drives. Due to the superior performance of the class-E inverter in high-frequency operation, the class-E topology has been extended to various circuit topologies. The class-E rectifier [8] is the time-reversal dual of the class-E inverter. Namely, it performs AC-DC conversion, which is the reverse operation of the DC-AC inversion. Although the class-E rectifier can be implemented with diode rectification, the class-E synchronous rectifiers [9] have also been proposed to achieve even higher efficiency. By replacing the diode with the active switch, the power loss due to the forward voltage drop in the diode can be eliminated. Additionally, the class-E power oscillator [10] has been proposed. The class-E power oscillator makes a self-oscillation by adding a passive feedback network to the class-E inverter. Since the power oscillator is unnecessary to have auxiliary power supplies or digital devices, they contribute to circuit simplification and cost reduction. In this way, class-E

resonant circuits have been extensively researched and advanced for applications in high-frequency domains.

However, the class-E inverter exhibits high sensitivity to load variations [11]. When load variations occur, it fails to maintain ZVS, resulting in a significant deterioration in power conversion efficiency. Moreover, output voltage and current fluctuate, making it impossible to achieve the desired output. The weakness in the sensitivity arises because the class-E switching is only satisfied under specific component values, including the load resistance, which is a common drawback of all the class-E resonant circuits. In order to address the load variations, the frequency-modulation control and ON/OFF control are typically applied to the class-E resonant circuits to achieve output regulation and compensation for the ZVS. Nevertheless, the controls at the MHz range have limitations in their bandwidth and accuracy. Additionally, the propagation delays that occur in digital devices appear at high-frequency operation, which complicates the control. Therefore, managing output power and power conversion efficiency against load variations is a significant challenge in the class-E resonant circuits.

Within this background, the load-independent class-E inverter [12] has garnered significant attention. The load-independent operation is a special mode discovered in the class-E inverters, where appropriate parameter tuning can impart robustness to the inverter. In this operating mode, soft switching and output regulation can be achieved without additional control or circuit, even against load variations. As such, it holds the potential to fundamentally solve the issue of load variations in high-frequency circuits. Therefore, it is valuable to extend the concept of the load-independent for various other circuit topologies.

## 1.2 Research Work

This thesis presents a high-frequency load-independent resonant circuit, including an inverter, power oscillator, and synchronous rectifier. A summary of contributions in this thesis is as follows.

First, the load-independent class- $E^{-1}$  and class- $\Phi_3$  inverters are proposed. The circuit analysis reveals the load-independent design conditions. As the common feature of the load-independent inverters, additional degrees of design freedom to achieve the load-independent operation are obtained by introducing a new resonant structure within the circuit. Additionally, this research demonstrates that the load-independent operation can also be feasible for Zero-Current Switching (ZCS) and constant-current amplitude. Therefore, the applicability of the load-independent inverter is further broadened. The load-independent class- $E^{-1}$  inverter is experimentally applied to a WPT system. The load-independent operation eliminates the need for feedback communication from the secondary side to the primary side in WPT systems, thereby facilitating the simplification of high-frequency circuit design.

Second, the load-independent class- $E^{-1}$  and class-E power oscillators are proposed. In order to achieve load-independent operation in the power oscillator, both the phase condition for sustained oscillation and the load-independent condition must be simultaneously satisfied. This study demonstrates that both conditions can be met by providing feedback from the resonant capacitor in the load-independent constant-current inverter. The proposed feedback network also makes the gate-drive voltage of the power oscillator independent of the load resistance. Consequently, the load-

independent power oscillator gains robustness, achieving high efficiency and stable oscillation against load variations.

Third, the load-independent class-E synchronous rectifier is proposed. The load-independent operation in the rectifiers requires synchronous rectification. In this research, the load-independent rectifier is realized by utilizing the time-reversal duality between power oscillators and synchronous rectifiers. The proposed synchronous rectifier is highly suitable for the secondary-side circuit of high-frequency WPT systems because it requires no auxiliary power supply or control circuits. Experimental validation is conducted on a WPT system using the load-independent class-E inverter as the transmitter, demonstrating the effectiveness of the proposed rectifier.

### 1.3 Thesis Outline

Chapter 2 will introduce the basic high-frequency circuits, including class-E inverter (Section 2.1), class-E rectifier (Section 2.2), class-E power oscillator (Section 2.3), and class-E synchronous rectifier (Section 2.4). The circuit topologies, operating principles, and relationships between the circuits are explained. Additionally, the load-independent class-E inverter is also introduced in Section 2.5. This section discusses the challenge of load sensitivity in the class-E inverters and how the load-independent class-E inverter has been addressed. The graphical outline of this thesis is shown in Fig. 1.1.

Chapter 3 presents a load-independent inverse class-E inverter, which essentially produces a sinusoidal output current even with a low- $Q$  series resonant filter. Be-

sides, the proposed inverter achieves ZCS and constant current output simultaneously, regardless of the load resistance. The experiment was carried out with a WPT system incorporating the proposed inverter as a transmitter and the class-D rectifier as a receiver. Although the input reactance of the class-D rectifier changed against DC-load variations due to the parasitic capacitances, the proposed inverter showed consistent, constant current operation by using the low- $Q$  series resonant filter. Also, the proposed WPT system maintained a low total harmonic distortion of the transmission current over the wide load range, even with the low- $Q$  output filter.

Chapter 4 presents a load-independent class- $\Phi_3$  resonant inverter. The class- $\Phi_3$  inverter is analyzed and reveals that the feasibility of load-independent operation in the class- $\Phi_3$  operation is revealed. The load-independent class- $\Phi_3$  inverter achieves the ZVS and a constant output-voltage amplitude regardless of the load resistance. The design conditions for achieving the load-independent operation are analytically described in this chapter. The experiment verifications were carried out to confirm the validity of the proposed design.

Chapter 5 presents a load-independent self-tuned series resonant power oscillator. The proposed power oscillator is derived from the load-independent inverse class-E inverter presented in Chapter 3. The proposed power oscillator achieves constant current output and high efficiency against load-resistance variations and component tolerances by adding the self-tuned feedback network. The design method of the proposed oscillator is presented in this chapter. The experimental results show the effectiveness of the proposed power oscillator.

Chapter 6 presents a load-independent class-E power oscillator. The load-independent

class-E inverter is incorporated into the power oscillator by introducing the feedback network using the LCCL filter. The LCCL filter compensates for the phase shift between the output and gate-drive voltages of the load-independent class-E inverter. Furthermore, the input impedance of the LCCL filter becomes purely resistive, which does not interfere with the load-independent operation of the inverter. Consequently, the proposed power oscillator obtains load independence in ZVS, output current, and gate-drive voltage. The proposed circuit works with high stability and efficiency over a wide load range, overcoming the sensitivity issue against load variations in the power oscillator. An analytical investigation of the proposed power oscillator is provided to reveal design conditions for achieving the load-independent operation. The experimental verifications were carried out at 6.78 MHz oscillation frequency.

Chapter 7 presents a load-independent class-E synchronous rectifier with a passive feedforward network. The proposed rectifier generates the synchronized drive voltage using the voltage across the resonant capacitor. Therefore, additional phase-detection circuits and digital devices are not required for the synchronous rectification. Moreover, the proposed synchronous rectifier achieves the ZVS and constant output voltage against load variations. The validity and effectiveness of the proposed rectifier are confirmed by the experiment.

Chapter 8 shows the conclusion of this thesis. Additionally, future research topics are introduced in this section.

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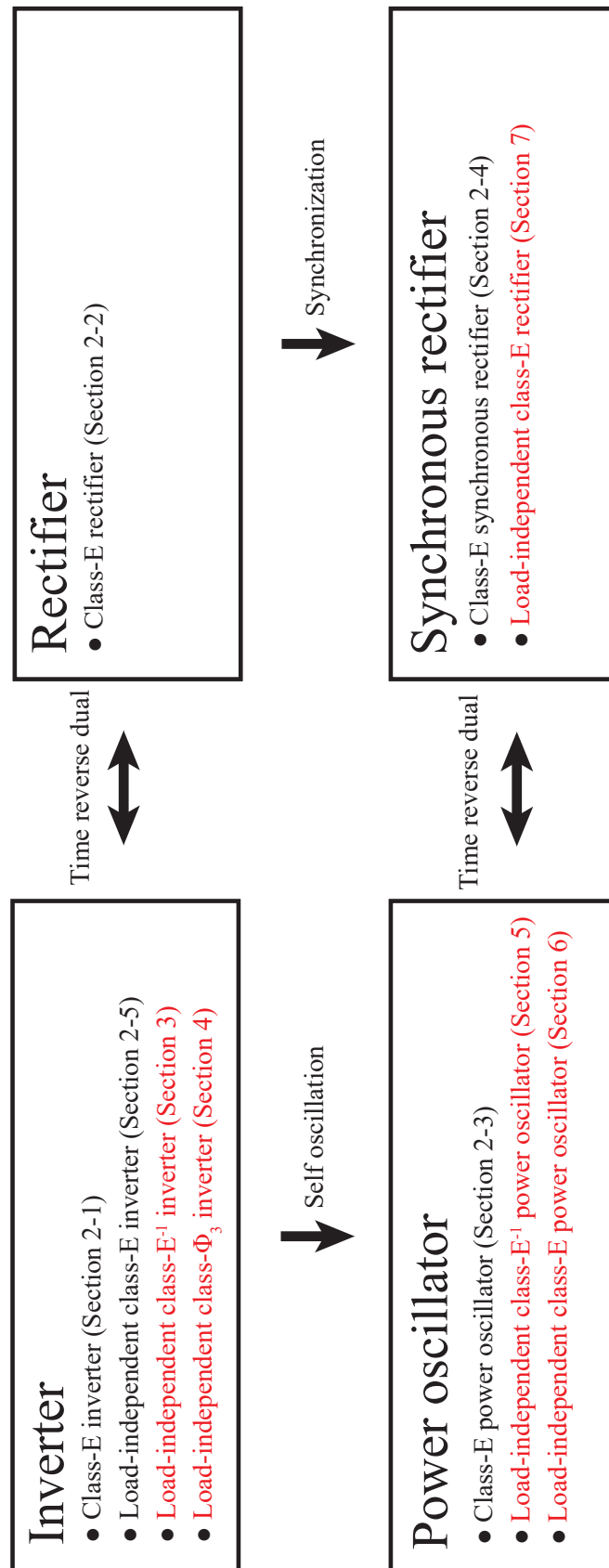


Fig. 1.1: Outline of this thesis. (black characters show the conventional research, and red characters show my proposal.)

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## Chapter 2

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# High-Frequency Resonant Circuits

### ●● ABSTRACT ●●

This chapter will provide background knowledge on high-frequency resonant circuits. The class-E resonant circuits are introduced as the representative of the high-frequency resonant circuits. Circuit topologies and operation principles of the class-E inverter, class-E rectifier, class-E power oscillator, and class-E synchronous rectifier are presented. Additionally, the relationships between them are described. Also, this chapter discusses the common challenge of the class-E resonant circuits, which is the sensitivity against load variations. Finally, the load-independent class-E inverter, which enhances the robustness against load variations, is introduced.

## 2.1 Class-E Inverter

### 2.1.1 Circuit Topology

Fig. 2.1(a) shows the circuit topology of the class-E inverter [1]. The class-E inverter is composed of the input voltage  $V_I$ , input-choke inductor  $L_1$ , switching device  $S$ , shunt capacitor  $C_1$ , series-resonant filter  $L_2$ - $C_2$ , and load resistance  $R_L$ .

One of the reasons that the class-E inverter is suitable for high-frequency operation is its topological simplicity. The class-E inverter is driven with a single switch, whose source terminal is grounded. Therefore, no high-side drive is required. Additionally, the innovative aspect of the class-E topology, compared with the class-D inverters, is that it uses an external shunt capacitor. In general, the switching loss increases in proportion to the drain-source capacitance. Hence, the circuit designers used to select the switching device with low output capacitance for class-D inverters. Nevertheless, Sokal deliberately added the drain-source capacitance to absorb the parasitic capacitance of the switching device [1].

### 2.1.2 Operating Principle

The class-E inverter achieves high efficiency even in high frequency because of the zero-voltage switching (ZVS) and the zero-derivative switching (ZDS), formulated as

$$v_S(2\pi D) = 0, \tag{2.1}$$

and

$$\left. \frac{dv_S(\theta)}{d\theta} \right|_{\theta=2\pi D} = 0, \quad (2.2)$$

respectively, where  $D$  is the OFF-duty ratio,  $\theta = 2\pi ft$  represents the angular time, and  $f$  is the operating frequency. This specific switching condition is called the class-E switching, which is the definition of the class-E inverter. The class-E switching can be achieved for a unique set of component values, including shunt capacitance, load resistance, and extra load inductance.

Fig. 2.1(b) shows the typical waveforms of the class-E inverter. The input-choke inductance eliminates the ripple current, producing a current source. The switching device turns ON and OFF periodically, with a fixed duty ratio. The switch voltage  $v_S$  achieves turn-ON ZVS and ZDS, contributing to reducing the switching loss. The series-resonant filter extracts a fundamental frequency component from the switch voltage, generating the sinusoidal output voltage in the load resistance.

## 2.2 Class-E Rectifier

### 2.2.1 Circuit Topology

Fig. 2.2(a) shows the circuit topology of the class-E rectifier [2]. The class-E rectifier is composed of the input AC voltage  $\dot{V}_{in}$ , series-resonant filter  $L_1$ - $C_1$ , rectification diode  $D$ , shunt capacitor  $C_1$ , output-choke inductor  $L_1$ , filter capacitor  $C_f$ , and load resistance  $R_L$ .

The class-E rectifier has a rectification diode instead of the switching device in the class-E inverter. This is because the turn-OFF class-E switching can be auto-

matically achieved using the diode. The diode turns OFF when the switch current becomes zero, resulting in the automatic turn-OFF ZDS. Besides, the continuity of the switch voltage allows the turn-OFF ZVS. Accordingly, the turn-ON ZVS is also ensured for a set of component values that satisfies the class-E switching condition.

### 2.2.2 Operating Principle

Fig. 2.2(b) shows the typical waveforms of the class-E rectifier. The class-E rectifier has a time-reversed duality against the class-E inverter. Namely, the waveforms of the class-E rectifier completely agree with the class-E inverter by replacing the angular time  $\theta$  to  $-\theta$ . Therefore, the AC to DC rectification, which is the reverse operation of the inverter, can be realized.

## 2.3 Class-E Power Oscillator

### 2.3.1 Circuit Topology

Fig. 2.3(a) shows the circuit topology of the class-E power oscillator [3]. The class-E power oscillator consists of the class-E inverter and the passive feedback network. The passive feedback network is composed of the capacitors  $C_3$  and  $C_4$ , inductor  $L_3$ , and the voltage-device resistances  $R_1$  and  $R_2$ .

The class-E power oscillator is a variant of the class-E inverter, which autonomously oscillates by adding a passive feedback network. The class-E power oscillator generates the gate-drive voltage using the output AC voltage. Therefore, the feedback network needs to compensate for the phase shift between the output and gate-drive

voltages. The class-E power oscillator works without the gate-drive circuits, including a crystal oscillator, gate driver, and additional power supplies, which further promotes circuit simplification and cost reduction.

### 2.3.2 Operating Principle

Fig. 2.3(b) shows the typical waveforms of the class-E power oscillator. The switch is driven by the excitation of the biased sinusoidal voltage  $v_{gs}$ , which is generated using the output AC voltage  $v_O$ . To induce the sustained oscillation, the total phase shift in the closed loop must be an integer multiple of  $2\pi$ . Meanwhile, the nominal phase shift of the output voltage is  $0.82\pi$  in the class-E inverter. Therefore, the feedback network  $C_3$ - $C_4$ - $L_3$  provides an additional phase shift, compensating the phase shift between the output and the gate-drive voltages. Additionally, the class-E power oscillator features to achieve the ZVS at the nominal state, which contributes to high-efficiency operation.

## 2.4 Class-E Synchronous Rectifier

Fig. 2.4(a) shows the circuit topology of the class-E synchronous rectifier [4]. The class-E synchronous rectifier uses the switching device instead of the rectification diode in the class-E rectifier.

The main purpose of using the switching device instead of the diode is to increase the power-conversion efficiency. In general, the diode has higher conduction losses than the switching device due to the ON resistance and forward voltage drop.

Therefore, active switches can reduce heat dissipation in the device and improve the overall efficiency.

The operating waveforms are exactly the same as the class-E rectifier, shown in Fig. 2.2(b). To achieve synchronous rectification, the switching device needs to turn OFF when the switch current becomes zero.

## 2.5 Load-Independent Class-E Inverter

### 2.5.1 Challenge in Class-E Resonant Circuits

The class-E resonant circuits, including inverter, power oscillator, and rectifier, are suitable for high-frequency operation. However, they are highly sensitive to load variations. The class-E switching can be satisfied for a specific parameter set, including the load resistance. Therefore, even a small change in the load resistance causes significant performance deterioration. The ZVS cannot be maintained, and power-conversion efficiency decreases against load variations. In addition, the output voltage and current fluctuate depending on the load resistance. Therefore, power and efficiency management is an essential challenge in the class-E resonant circuits.

### 2.5.2 Circuit Topology

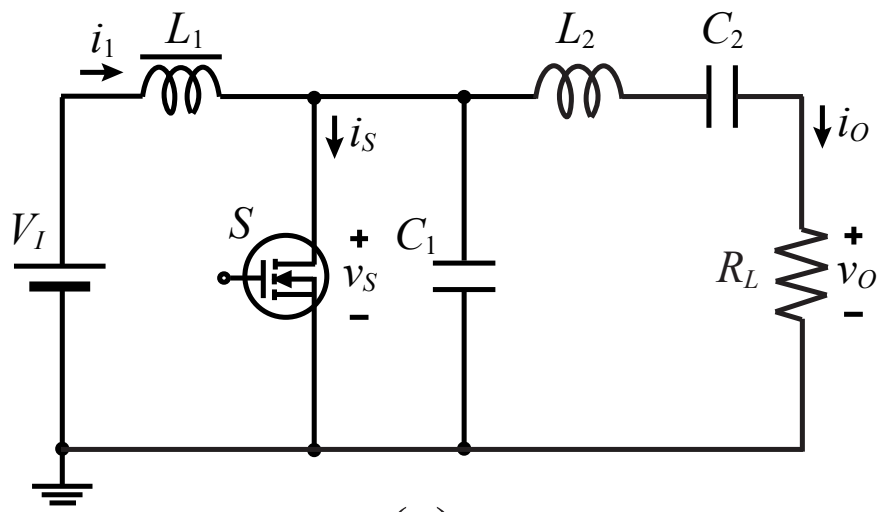
Fig. 2.5(a) shows the circuit topology of the load-independent class-E inverter [5]. There is no topological difference between the load-independent and original class-E inverters. However, the load-independent class-E inverter uses finite-input inductance instead of the choke inductance.

The load-independent class-E inverter achieves the ZVS regardless of the load resistance. This feature can be enabled by the introduction of the finite-input inductance. In the original class-E inverter, there is no current path to discharge the shunt capacitor under light load conditions, leading to turn-on non-ZVS. In contrast, the load-independent class-E inverter introduces a large ripple in the input current, providing a current path for discharging the shunt capacitor to the input side.

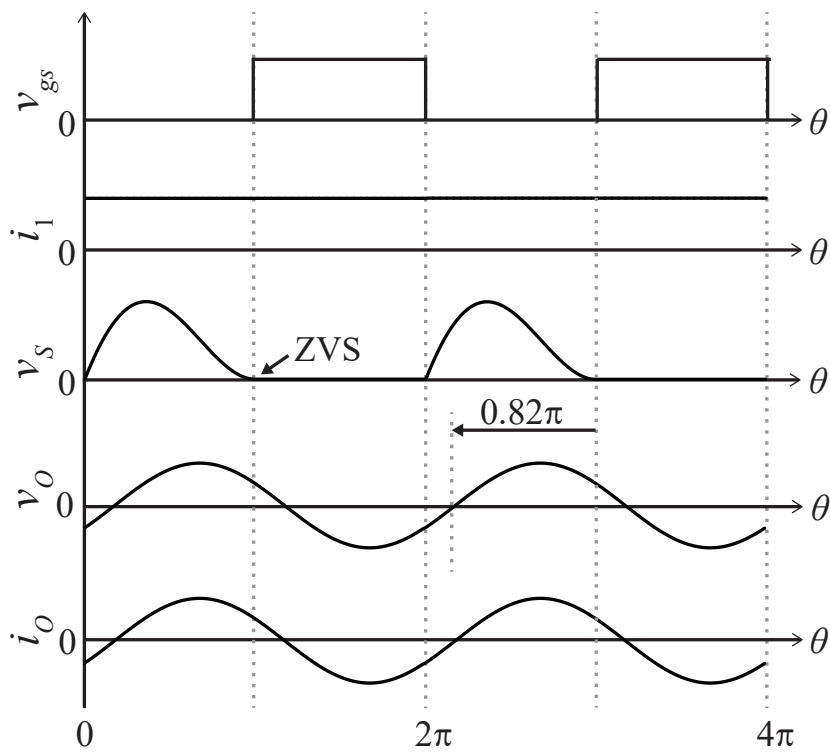
Additionally, the load-independent class-E inverter inherently has a constant voltage gain against load variations. Therefore, no additional control is required to satisfy the output regulation.

### 2.5.3 Operating Principle

Fig. 2.5(b) shows the typical waveforms of the load-independent class-E inverter. The input current  $i_1$  has a large ripple because of the resonance between  $L_1$  and  $C_1$  during the turn-OFF period. The resonant frequency between  $L_1$  and  $C_1$  is slightly higher than the operating frequency. The switch voltage  $v_S$  achieves the ZVS, and output voltage  $v_O$  has constant amplitude against load variations.



(a)



(b)

Fig. 2.1: Class-E inverter. (a) Circuit topology. (b) Typical waveform.

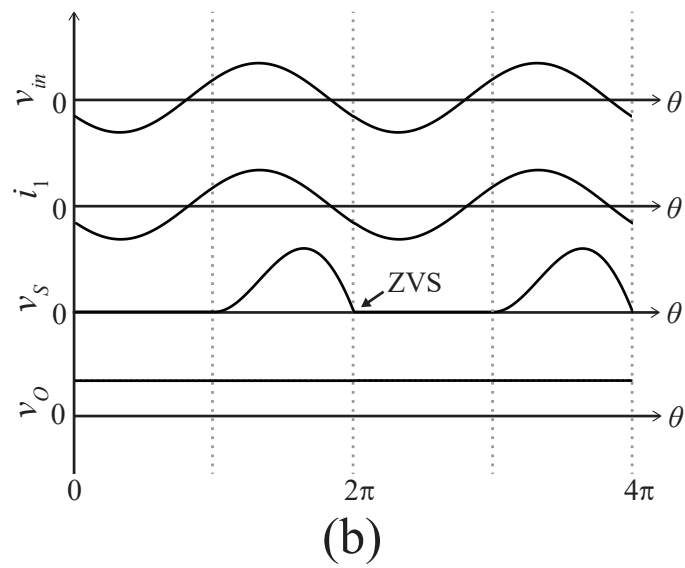
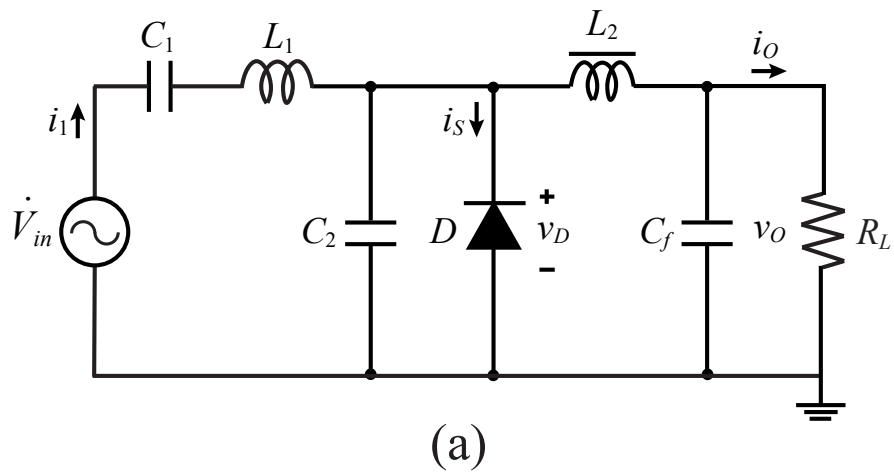


Fig. 2.2: Class-E rectifier. (a) Circuit topology. (b) Typical waveform.

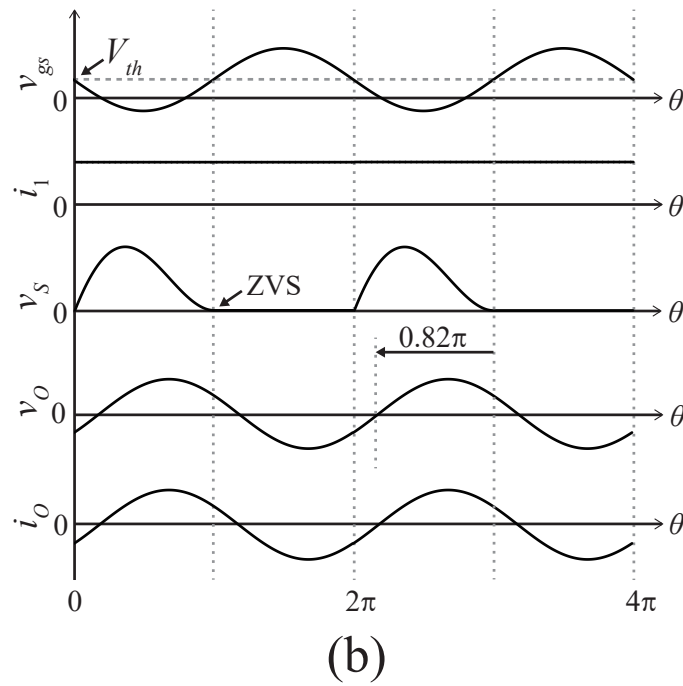
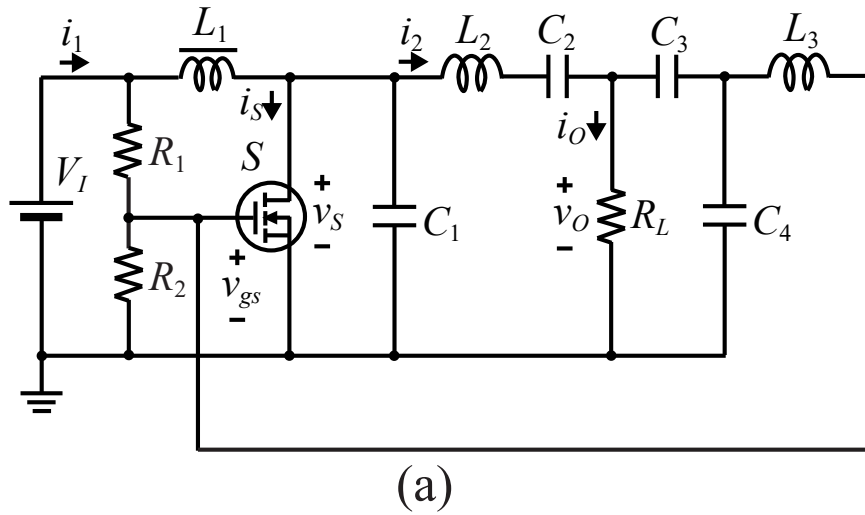


Fig. 2.3: Class-E power oscillator. (a) Circuit topology. (b) Typical waveform.

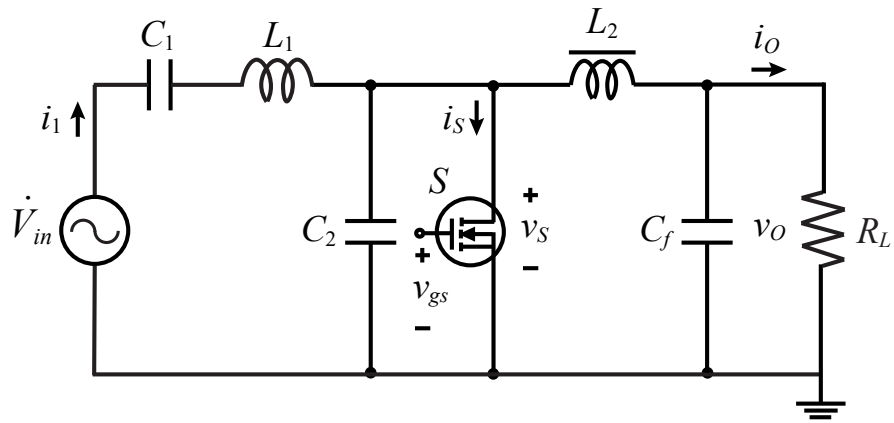
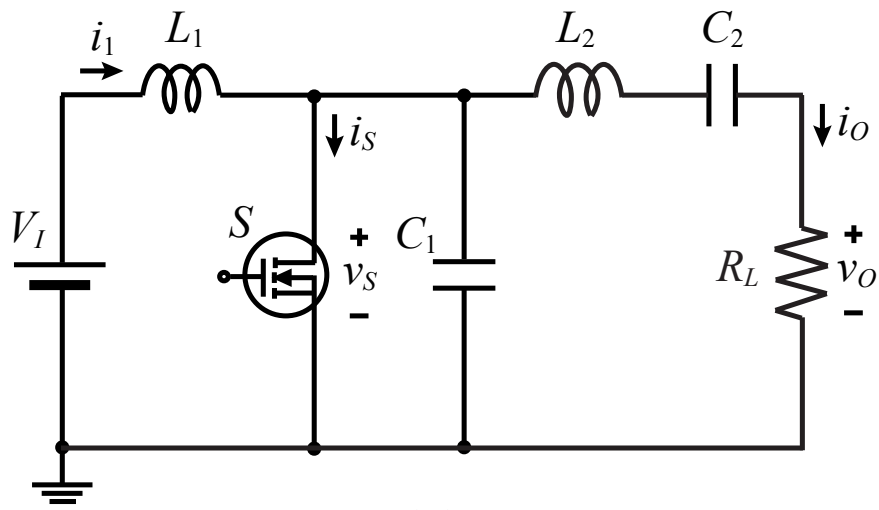
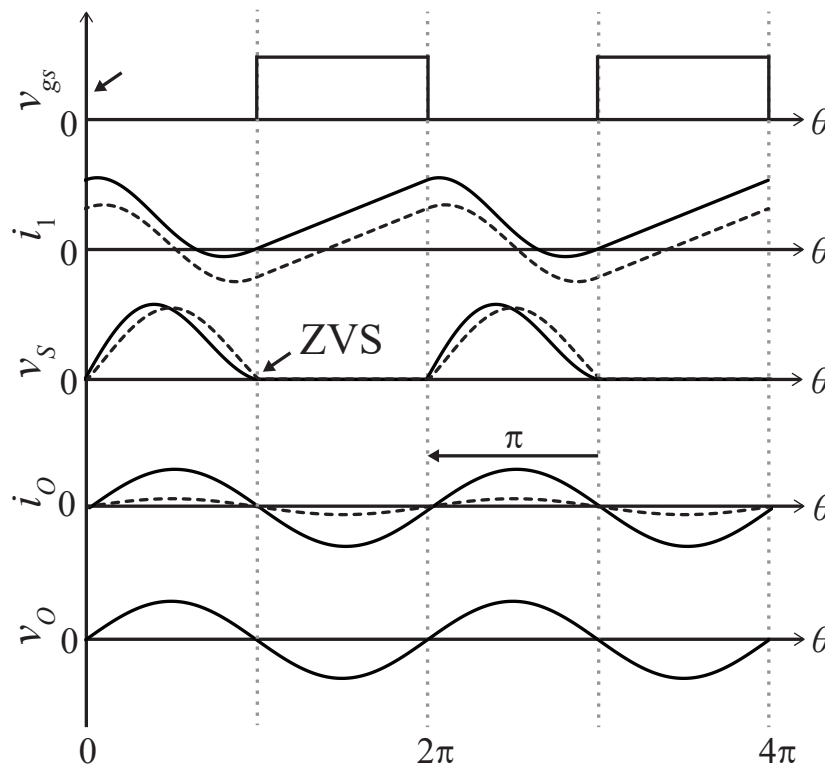


Fig. 2.4: Circuit topology of the synchronous class-E rectifier.



(a)



(b)

Fig. 2.5: Load-independent class-E inverter. (a) Circuit topology. (b) Typical waveform. (solid line: rated load condition, dashed line: varied load condition.)

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## Chapter 3

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# Load-Independent Class-E<sup>-1</sup> Inverter With Constant Current

### 3.1 Introduction

High performance power semiconductor devices, such as GaN and SiC devices, have enabled the high-frequency and high-efficiency operation of inverters [1–3]. The inverters at the megahertz frequency band are explored and developed, reducing the size and weight of the passive components. Meanwhile, high-frequency operation brings challenges, including growing switching losses and difficulty in high-side gate drives. Thus, the class-E inverter family, including class-E [1–14], class-EF [15–17], and class- $\Phi$  inverters [18,19], have attracted attention due to its simple configuration and soft switching feasibility. However, the class-E inverters are essentially sensitive against load variations [5,6]. The load variations change the circuit operation drastically, causing output voltage variations and efficiency degradation due to hard switching.

To overcome the sensitivity, a load-independent class-E inverter was proposed [7], which enhances the robustness against load variations. The load-independent class-

E inverter uses a finite input coil, which works as a resonant inductance. Namely, the load-independent class-E inverter expands the design flexibility to obtain robustness by introducing a new resonant structure. The load-independent class-E inverter maintains soft switching against load variations. Additionally, the amplitude of the output AC voltage is constant regardless of the load resistance. The robustness can be obtained by a specific tuning of component values without additional controls [8] and circuitry [9]. The design technique of the load-independent class-E inverter has also been applied to various circuit topologies in the class-E inverter family [11–21]. Depending on the circuit topology, the load-independent inverters inherently exhibit different characteristics in output types (constant current: CC or constant voltage: CV), soft switching (ZVS or ZCS), and output-resonant filters (series resonant: SR or parallel resonant: PR). Accordingly, the load-independent inverters can be adapted to a wide range of applications and specifications, such as DC-DC converters [13] and the transmitter of WPT systems [15–17]. Especially for WPT applications, the CC output inverter with the SR output filter is preferable. This is because it avoids overcurrents flowing through the transmitter coil even when the receiver circuit moves away.

Owing to the CC-SR feature, the load-independent class-EF inverter has proven successful in applications as a transmitter for WPT systems [15–17]. Additionally, the class-EF inverter mitigates switch-voltage stress by adding a harmonic resonant branch. In the original class-EF<sub>2</sub> and class-E/F<sub>3</sub> inverters [22–24], the harmonic resonant filter is tuned to an integer multiple of the switching frequency. On the other hand, the load-independent class-EF inverter employs a resonant frequency approximately 1.7 times the switching frequency [15]. This design, however, leads to

significant harmonic distortion in the output current because the harmonic resonant branch cannot fully filter out the harmonics [25]. The high total harmonic distortion (THD) of the current degrades electromagnetic interference (EMI) performance [26] and efficiency [27]. Furthermore, the harmonics in the output current deteriorate the consistency of the CC operation. Therefore, it is important to develop another CC-SR inverter topology with a low THD output current.

This chapter presents an analysis and design of the load-independent SR inverter with CC output. A novel circuit topology with CC-SR property is introduced, which can inherently output sinusoidal current even with a low- $Q$  SR filter. Analytical design equations of the proposed inverter are provided, which allows a quick and intuitive component-value selection. This chapter also presents the design procedure and experiment for the WPT system incorporating the proposed inverter as the transmitter. The experimental verifications were conducted with the WPT system with the proposed inverter. The proposed inverter achieved superior consistency of the CC operation and a lower THD transmission current compared with the load-independent class-EF inverter. Furthermore, the proposed inverter showed low sensitivity to reactance components because it can produce sufficiently pure sinusoidal wave even with the low- $Q$  SR filter. The experimental results showed the validity of the inverter design and analysis.

## 3.2 Load-Independent Inverter With CC-SR Property

This section provides a brief review of the load-independent class-EF inverter [15] and introduces the proposed inverter. These inverters have a common feature in the CC-SR property.

### 3.2.1 Load-Independent Class-EF Inverter

Fig. 3.1(a) and 3.1(b) show the circuit topology and example waveforms of the load-independent class-EF inverter, respectively, where  $D$  is the on-duty ratio,  $\theta = \omega t = 2\pi ft$  is the angular displacement,  $\omega$  denotes the angular switching frequency, and  $f$  is the switching frequency. Besides, the subscript ‘ $r$ ’ of the symbol means its rated value.

The load-independent class-EF inverter achieves ZVS and a constant amplitude output current simultaneously, regardless of the load resistance  $R$ , as shown in Fig. 3.1(b). The load-independent operation is obtained for a specific set of component values, which is determined by satisfying the design conditions of [15]

$$\frac{dI_m}{dR} = 0, \quad (3.1)$$

and

$$v_S(2\pi D) = 0, \quad (3.2)$$

where  $I_m$  is the amplitude of the output current  $i$ . The condition (3.1) represents the CC operating condition, and (3.2) shows the ZVS condition. By satisfying (3.1)

and (3.2) simultaneously, the design parameters for the load-independent operation are derived. Therefore, the class-EF inverter only requires specific tuning to obtain robustness against load variations without requiring additional controls and circuits.

However, the load-independent class-EF inverter introduces significant harmonic distortion into the output current. This is because the resonant frequency of  $L_h$ - $C_h$  needs to be tuned to approximately 1.7 times the switching frequency, and thus, the harmonic current cannot be fully filtered out by  $L_h$ - $C_h$ .

Although the harmonics in the output current can be reduced by using a high- $Q$  SR filter, it results in higher sensitivity, a large inductance, and increased voltage stress and power losses for the resonant components. Also, the push-pull topology is effective for suppressing second-order harmonics. It has a tradeoff against the increase in device and component numbers and accurate tuning for circuit balance.

### 3.2.2 Proposed Inverter

Fig. 3.2(a) shows the circuit topology of the proposed inverter, which consists of the DC-input voltage source  $V_I$ , choke inductance  $L_C$ , series inductance  $L_S$ , switching device  $S$ , shunt capacitance  $C_S$ , SR filter  $L_0$ - $C_0$ , and load resistance  $R$ . Fig. 3.2(b) depicts the example waveforms of the proposed inverter for fixed load resistances.

The choke inductance  $L_C$  sufficiently reduces the ripple current and behaves as a DC-current source. The switching device turns on and off periodically. During the turn-on period, current flows into the switching device, which achieves ZCS at the turn-off moment, as shown in Fig. 3.2(b). The ZCS is a dual operation

of the ZVS in the class-E inverters [28]. Namely, the proposed inverter can be called load-independent inverse class-E inverter. The  $L_S$  and  $C_S$  resonate at slightly higher than the switching frequency, and the nearly sinusoid voltage appears across the capacitor  $C_S$ . The output voltage is generated by extracting a fundamental frequency component from the voltage across  $C_S$  through the SR output filter.

The proposed inverter exhibits robustness against resistive load variations. Namely, the ZCS is maintained regardless of the load resistance, resulting in high-efficiency operation over the wide load range. Also, the amplitude and phase shift of the output current is independent of the load resistance. The output currents for  $R/R_r = 1$  and  $R/R_r = 0.1$  are completely overlapped in Fig. 3.2(b).

The proposed inverter no longer requires a high- $Q$  SR filter because  $v_{C_S}$  exhibits inherently close to the sinusoidal waveform. Also, a sufficiently pure sinusoidal output can be obtained even without the SR filter. In the design without the SR filter,  $C_0$  only works as a DC blocking with a large capacitance, while  $L_0$  works as the phase-shift inductance required for the load-independent design. One major advantage of applying the low- $Q$  SR filter is that the proposed inverter obtains robustness against reactance component variations.

### 3.3 Analysis of Proposed Inverter

This chapter provides the waveform expressions, inverter characteristics, and design equations of the proposed inverter. The analysis is conducted under the following assumptions.

1. The choke inductance  $L_C$  is large enough so that the input current  $I_I$  can be regarded as DC.
2. The switching device operates ideally. Namely, the switching time, parasitic capacitances, on-resistance, and threshold voltage are zero, and off-resistance is infinite. Besides, the switch turns on during  $0 \leq \theta < 2\pi D$ , and turns off during  $2\pi D \leq \theta < 2\pi$ .
3. The resonant inductance  $L_0$  is divided into a resonant component  $L_a$  and an extra-inductive component  $L_b$ . The  $L_a$  and  $C_0$  resonate at the switching frequency, namely

$$\frac{1}{\omega\sqrt{L_a C_0}} = 1. \quad (3.3)$$

Additionally, the quality factor of the SR output filter  $Q = \omega L_0/R$  is high enough so that the output current can be regarded as a pure sine wave as

$$i(\theta) = I_m \sin(\theta + \varphi), \quad (3.4)$$

where  $\varphi$  is the phase shift from gate-drive voltage defined as shown in Fig. 3.2(b), and  $I_m$  is the amplitude of the output current.

4. All the passive component works linearly with no parasitic components.

In the analysis, the dimensionless circuit parameters are used to provide a generalized discussion. The voltage and current are normalized by input voltage  $V_I$  and rated load resistance  $R_r$ , as like

$$v^* = \frac{v}{V_I}, \quad \text{and} \quad i^* = \frac{R_r i}{V_I}. \quad (3.5)$$

Besides, the component parameters are also normalized by  $\omega$  and  $R_r$ , as like

$$\lambda_S = \frac{\omega L_S}{R_r}, \quad \gamma_S = \frac{1}{\omega C_S R_r}, \quad \text{and} \quad \rho = \frac{R}{R_r}. \quad (3.6)$$

Fig. 3.3 shows the analytical model of the proposed inverter.

### 3.3.1 Waveform Derivation

During the switch turn-on period of  $0 \leq \theta < 2\pi D$ , a second-order differential equation for switch current  $i_S^*$  is obtained using KCL as

$$\frac{d^2 i_S^*(\theta)}{d\theta^2} + \omega_S^{*2} i_S^*(\theta) = \omega_S^{*2} [I_I^* - I_m^* \sin(\theta + \varphi)], \quad (3.7)$$

where  $I_I^*$  is the normalized input current and  $\omega_S^*$  is defined as

$$\omega_S^* = \sqrt{\frac{\gamma_S}{\lambda_S}}. \quad (3.8)$$

By solving (3.7), the switch current for  $0 \leq \theta < 2\pi D$  can be obtained as

$$\begin{aligned} i_S^*(\theta) = & A \cos(\omega_S^* \theta) + B \sin(\omega_S^* \theta) \\ & - \frac{\omega_S^{*2} I_m^*}{\omega_S^{*2} - 1} \sin(\theta + \varphi) + I_I^*, \quad \text{for } 0 \leq \theta < 2\pi D, \end{aligned} \quad (3.9)$$

where  $A$  and  $B$  are constants. Besides, the voltage across  $\gamma_S$  is derived by integrating the current flowing through it as

$$\begin{aligned} v_{C_S}^*(\theta) = & \gamma_S^* \int_0^\theta [I_I^* - i_S^*(\theta') - I_m^* \sin(\theta' + \varphi)] d\theta' \\ = & -\lambda_S \omega_S^* \left[ A \sin(\omega_S^* \theta) - B \cos(\omega_S^* \theta) \right. \\ & \left. + \frac{\omega_S^* I_m^*}{\omega_S^{*2} - 1} \cos(\theta + \varphi) \right], \quad \text{for } 0 \leq \theta < 2\pi D. \end{aligned} \quad (3.10)$$

During the switch turn-off period of  $2\pi D \leq \theta < 2\pi$ , the switch current becomes zero, namely

$$i_S^*(\theta) = 0, \quad \text{for } 2\pi D \leq \theta < 2\pi. \quad (3.11)$$

The expression of the voltage across shunt capacitance during the turn-off period, which is the same as the switch voltage, can be given by integrating the current flowing through  $\gamma_S$  as

$$\begin{aligned} v_{C_S}^*(\theta) = v_S^*(\theta) &= \gamma_S \int_{2\pi D}^{\theta} I_I^* - I_m^* \sin(\theta' + \varphi) d\theta'. \\ &= \gamma_S \{ I_I^*(\theta - 2\pi D) + I_m^* [\cos(\theta + \varphi) - \cos(2\pi D + \varphi)] \} \\ &\quad - \lambda_S \omega_S^* \left[ A \sin(2\pi D \omega_S^*) - B \cos(2\pi D \omega_S^*) \right. \\ &\quad \left. + \frac{\omega_S^* I_m^*}{\omega_S^{*2} - 1} \cos(2\pi D + \varphi) \right], \quad \text{for } 2\pi D \leq \theta < 2\pi. \end{aligned} \quad (3.12)$$

Note that the boundary condition at  $\theta = 2\pi D$  with (3.10) is taken into account in (3.12).

### 3.3.2 Boundary Condition

From the continuity of the current flowing through  $\lambda_S$  and the voltage across  $\gamma_S$ , we obtain the boundary conditions as

$$i_S^*(0) = i_S^*(2\pi), \quad (3.13)$$

and

$$v_{C_S}^*(0) = v_{C_S}^*(2\pi). \quad (3.14)$$

From (3.9)-(3.14), the constants  $A$  and  $B$  can be obtained as

$$A = \frac{\omega_S^{*2} I_m^*}{\omega_S^{*2} - 1} \sin \varphi - I_I^*, \quad (3.15)$$

and

$$B = \left\{ \frac{\omega_S^* [\cos(2\pi D \omega_S^*) - (1 - 2\omega_S^{*2}) \cos \varphi]}{(\omega_S^{*2} - 1)[1 - \cos(2\pi D \omega_S^*)]} - \frac{\omega_S^{*2} \sin \varphi \sin(2\pi D \omega_S^*)}{(\omega_S^{*2} - 1)[1 - \cos(2\pi D \omega_S^*)]} \right\} I_m^* + \frac{\pi \omega_S^* + \sin(2\pi D \omega_S^*)}{1 - \cos(2\pi D \omega_S^*)} I_I^*. \quad (3.16)$$

### 3.3.3 Load-Independent Condition

The proposed inverter achieves ZCS at the turn-off instant, namely

$$i_S^*(2\pi D) = 0. \quad (3.17)$$

There is no power-loss factor in this analysis. Therefore, the input and output powers are equal. Hence, we have

$$1 \times I_I^* = \frac{\rho I_m^{*2}}{2}. \quad (3.18)$$

From (3.9), (3.17), and (3.18), the relationship between  $I_m^*$  and  $\rho$  is obtained as

$$\begin{aligned} & [\pi(1 - D)\omega_S^* \sin(2\pi D \omega_S^*) + 1 - \cos(2\pi D \omega_S^*)] I_m^* \rho \\ & - \frac{4\omega_S^{*2} \sin(\pi D + \varphi) \sin(\pi D \omega_S^*) \sin[\pi D(1 - \omega_S^*)]}{\omega_S^{*2} - 1} = 0. \end{aligned} \quad (3.19)$$

For achieving the CC output,  $I_m^*$  must be independent from  $\rho$ . This means that the coefficient of  $\rho$  and the constant term in (3.19) must be both zero. Thus, we have the load-independent-design conditions as

$$\pi(1 - D)\omega_S^* \sin(2\pi D \omega_S^*) + 1 - \cos(2\pi D \omega_S^*) = 0, \quad (3.20)$$

and

$$\varphi = \pi(1 - D). \quad (3.21)$$

By satisfying (3.20) and (3.21), the proposed inverter attains the ZCS and CC output regardless of the load resistance. Fig. 3.4 shows the normalized resonant angular frequency  $\omega_S^*$  and phase shift  $\varphi$  that satisfy (3.20) and (3.21).

### 3.3.4 SR Output Filter

From the assumption, the SR output filter  $\lambda_0 - \gamma_0$  passes only a fundamental frequency component from the voltage across  $\gamma_S$ . Namely, we obtain

$$v_{C_{S1}}^*(\theta) = \rho I_m^* \sin(\theta + \varphi) + \lambda_b I_m^* \cos(\theta + \varphi). \quad (3.22)$$

where  $v_{C_{S1}}^*$  is the fundamental frequency component in  $v_{C_S}^*$ . By applying the Fourier Series Expansion for (3.22) and considering (3.20) and (3.21), we obtain

$$\begin{aligned} \rho I_m^* &= \frac{1}{\pi} \int_0^{2\pi} v_{C_S}^*(\theta) \sin(\theta + \varphi) d\theta \\ &= \frac{2\gamma_S \omega_S^{*2} [\pi(1 - D) \cos(\pi D) + \sin(\pi D)]}{\pi(\omega_S^{*2} - 1)} I_m^*, \end{aligned} \quad (3.23)$$

and

$$\begin{aligned} \lambda_b I_m^* &= \frac{1}{\pi} \int_0^{2\pi} v_{C_S}^*(\theta) \cos(\theta + \varphi) d\theta \\ &= \frac{\gamma_S \omega_S^{*2}}{\pi(\omega_S^{*2} - 1)} \left\{ \pi(1 - D) + \frac{\sin(\pi D)}{2} - \frac{\pi}{\omega_S^{*2}} \right. \\ &\quad \left. + \frac{2 \sin(\pi D) [\sin(\pi D) + \pi(1 - D) \cos(\pi D)]}{\pi(1 - D)(\omega_S^{*2} - 1)} \right\} I_m^*. \end{aligned} \quad (3.24)$$

### 3.3.5 Inverter Characteristics

Fig. 3.5(a) and (b) show the normalized maximum switch voltage  $V_{Smax}^*$  and current  $I_{Smax}^*$  as functions of duty ratio  $D$  and normalized shunt capacitance  $\gamma_S$ . The  $V_{Smax}^*$  and  $I_{Smax}^*$  are obtained by computing the maximum value against  $\theta$  using (3.12) and (3.9), respectively. It is seen from Fig. 3.5(a) that the normalized peak switch voltage decreases for lower  $D$ . Meanwhile, the low switch-current stress is attained for larger  $\gamma_S$ , as shown in Fig. 3.5(b).

Fig. 3.5(c) shows the power-output capability, which is defined as

$$c_p = \frac{\rho I_m^{*2}}{2V_{Smax}^* I_{Smax}^*}. \quad (3.25)$$

It is seen from Fig. 3.5(c) that the maximum power-output capability  $c_p = 0.102$  is obtained for  $D = 0.481$  and  $\gamma_S = 1.08$ .

Fig. 3.6 shows the normalized extra-inductance  $\lambda_b$  and output current amplitude  $I_m^*$  as functions of duty ratio for fixed  $\gamma_S$ , which is depicted using (3.23) and (3.24). It can be seen from Fig. 3.6(b) that the output current amplitude is adjustable depending on  $D$  and  $\gamma_S$ . The design point that achieves the maximum power-output capability is obtained as  $\lambda_b = 1.33$  and  $I_m^* = 1.15$ .

### 3.3.6 Circuit Design for Maximum Power-Output Capability

The proposed inverter is designed for given input voltage  $V_I$ , rated load resistance  $R_r$ , switching frequency  $f$ , and quality factor  $Q$ . The component values can be uniquely determined by satisfying (3.18), (3.20), (3.21), (3.23), and (3.24) for any  $D$

and  $\gamma_S$ . The design equations for any  $D$  and  $\gamma_S$ , and the specific case of maximum power-output capability are derived as

$$C_S = \frac{1}{\omega\gamma_S R_r} = \frac{0.147}{f R_r}, \quad (3.26)$$

$$L_S = \frac{1}{\omega_S^{*2} C_S} = \frac{0.0977 \times R_r}{f}, \quad (3.27)$$

$$L_0 = \frac{Q R_r}{\omega} = \frac{0.159 \times Q R_r}{f}, \quad (3.28)$$

$$\begin{aligned} L_b &= \frac{\gamma_S \omega_S^{*2} R_r}{\pi \omega (\omega_S^{*2} - 1)} \left\{ \pi(1 - D) + \frac{\sin(\pi D)}{2} - \frac{\pi}{\omega_S^{*2}} \right. \\ &\quad \left. + \frac{2 \sin(\pi D) [\sin(\pi D) + \pi(1 - D) \cos(\pi D)]}{\pi(1 - D)(\omega_S^{*2} - 1)} \right\} \\ &= \frac{0.212 \times R_r}{f}, \end{aligned} \quad (3.29)$$

and

$$C_0 = \frac{1}{\omega^2(L_0 - L_b)} = \frac{0.159}{f R_r(Q - 1.33)}. \quad (3.30)$$

The amplitude of the output current is derived from (3.23) as

$$\begin{aligned} I_m &= \frac{\pi(\omega_S^{*2} - 1)V_I}{\gamma_S \omega_S^{*2} R_r [\pi(1 - D) \cos(\pi D) + \sin(\pi D)]} \\ &= \frac{1.15 \times V_I}{R_r}. \end{aligned} \quad (3.31)$$

### 3.3.7 Circuit Design for Reducing Switching Loss

The proposed inverter achieves ZCS regardless of the load resistance, reducing the current-related turn-off losses. However, in high-frequency operations, voltage-related turn-on losses become dominant. Therefore, design methods to reduce turn-on losses is provided in this section.

The turn-on switching loss can be given as

$$P_{SW} = \frac{1}{2}C_{OSS}V_S^2f, \quad (3.32)$$

where  $C_{OSS}$  is the output capacitance of the switching device, and  $V_S$  is the switch voltage at turn-on instant. We can see from (3.32) that reducing  $V_S$  is effective for suppressing the turn-on loss.

Fig. 3.7 shows the example waveforms of the switch current and voltage. There are ringings in both switch current and voltage during the turn-off period, which is caused by the resonance between  $L_S$  and  $C_{OSS}$ . For reducing  $V_S$ , it is desirable to turn on the switch when the switch voltage drops completely, as shown in Fig. 3.7. Namely, the number of the ringings during the turn-off period should be an integer multiple as

$$n_S T_S = \frac{1-D}{f}, \quad (3.33)$$

where  $n_S$  is the number of the ringings, for example,  $n_S = 3$  in Fig. 3.7. Besides,  $T_S = 2\pi\sqrt{L_S C_{OSS}}$  represents a ringing period. From (3.33), the design value of the  $L_S$  can be obtained as

$$L_S = \frac{1}{C_{OSS}} \left( \frac{1-D}{\omega n_S} \right)^2. \quad (3.34)$$

The design equation of  $C_S$  can be

$$C_S = \frac{1}{\omega_S^{*2} L_S}. \quad (3.35)$$

The remaining component values can be determined using (3.28)-(3.30).

## 3.4 Application for WPT

This chapter introduces a WPT system using the proposed inverter as a concrete application example, along with a design procedure, power-loss analysis, and experiment. Furthermore, this chapter compares the performances of the proposed WPT system and the WPT system using the load-independent class-EF inverter [15].

### 3.4.1 System Configuration

Fig. 3.8 shows the circuit configurations of the WPT system with the load-independent class-EF and the proposed inverters, respectively. The load-independent class-EF and the proposed inverters are employed as transmitters. The current-driven class-D rectifier [29] is adopted for the receiver. The class-D rectifier consists of two diodes  $D_1$  and  $D_2$  with parasitic capacitances of  $C_{D1}$  and  $C_{D2}$ , smoothing capacitor  $C_f$  and load resistance  $R_L$ . The coupling section is of the series-to-series (S-S) type, and the transmitter coil  $L_1$  and receiver coil  $L_2$  are coupled with a coupling coefficient  $k$ .

### 3.4.2 Analytical Expressions of Proposed WPT System

The input impedance of the class-D rectifier is ideally pure resistive component [30]. However, in a high-frequency region, it becomes capacitive due to the parasitic capacitances of the diodes. When the parasitic capacitances  $C_{D1}$  and  $C_{D2}$  are considered, the input resistance and capacitance of the class-D rectifier can be

expressed as [31]

$$R_{rct} = \frac{[1 - \cos(2\pi D_{rct})]^2 R_L}{2\pi^2}, \quad (3.36)$$

and

$$C_{rct} = \frac{2\pi(C_{D1} + C_{D2})}{\sin(4\pi D_{rct}) + 2\pi(1 - 2D_{rct})}, \quad (3.37)$$

respectively, where

$$D_{rct} = \frac{1}{2\pi} \cos^{-1} \left[ \frac{\omega(C_{D1} + C_{D2})R_L - 2\pi}{\omega(C_{D1} + C_{D2})R_L + 2\pi} \right], \quad (3.38)$$

is the diode on-duty ratio.

The impedance seen from the inverter is obtained as

$$Z_{inv} = \frac{\omega^2 k^2 L_1 L_2 R_{rct}}{R_{rct}^2 + \frac{1}{\omega^2 C_{rct}^2}} + j\omega \left[ L_1 + \frac{k^2 L_1 L_2}{C_{rct} \left( R_{rct}^2 + \frac{1}{\omega^2 C_{rct}^2} \right)} \right], \quad (3.39)$$

under the complete resonance in the secondary side as

$$\frac{1}{\omega \sqrt{L_2 C_2}} = 1. \quad (3.40)$$

It can be seen from (3.39) that both the resistive and reactive parts depend on the load resistance  $R_L$ . Meanwhile, the proposed inverter has robustness even against reactive-component variations due to the low- $Q$  SR filter.

From (3.39), the DC-output voltage of the WPT system with the proposed inverter is expressed as

$$V_O = \omega k I_m \sqrt{\frac{L_1 L_2 R_{rct} R_L}{2 \left( R_{rct}^2 + \frac{1}{\omega^2 C_{rct}^2} \right)}} \quad (3.41)$$

We can see from (3.41) that the output voltage depends on the load resistance  $R_L$ . When we consider the case that the effect of the parasitic capacitance of the diode can be ignored, namely  $R_{rct} \gg 1/(\omega C_{rct})$ , the output voltage is derived from (5.7) and (3.41) as

$$V_O = \frac{\pi k \omega \sqrt{L_1 L_2}}{2} I_m = \frac{0.0677 \times R_{Lr} V_I}{k f \sqrt{L_1 L_2}}. \quad (3.42)$$

The parameter  $R_{Lr}$  in (3.42) represents the rated load resistance, which is the fixed value and is given as a design specification. Although the output voltage  $V_O$  depends on the initial design value of the load resistance  $R_{Lr}$ , the output voltage keeps a constant value against the changes in the load resistance  $R_L$ .

## 3.5 Experimental Results

The circuit experiment was conducted for the WPT system with the load-independent class-EF and the proposed inverters, shown in Fig. 3.8(a) and 3.8(b).

### 3.5.1 Experimental Prototype

The design specification of the WPT system with the proposed inverter was given as:  $f = 3.39$  MHz,  $V_I = 120$  V,  $R_{Lr} = 50$   $\Omega$ , and  $V_O = 65$  V. The coupling coils were solenoid-type and made with air core, having a transmission distance of  $d = 15$  mm. The geometric parameters of the coupling coils are given in Table 3.1, where  $h_{core}$  and  $d_{core}$  are the height and diameter of the coils, respectively. Additionally, the turn numbers  $N$  and wire diameters  $d_w$  in Table 3.1 are determined to obtain the desired output voltage from (3.42).

The implemented coupling coils had inductances of  $L_1 = 5.24 \mu\text{H}$  and  $L_2 = 5.93 \mu\text{H}$  with ESRs of  $r_{L_1} = 0.342 \Omega$  and  $r_{L_2} = 0.488 \Omega$ , respectively. Besides, a measured coupling coefficient between  $L_1$  and  $L_2$  was  $k = 0.224$ . From the measured parameters, the equivalent resistance  $R_{inv} = 56.5 \Omega$  was obtained. The proposed inverter can provide a sinusoidal output current even without the SR filter. Therefore, we used sufficiently large capacitance for  $C_0$ , which only works as a DC blocking. Table 3.2 gives the component values of the WPT system with proposed and load-independent class-EF inverters, which were obtained by following the design in Section 5.3 and 3.3.7.

The WPT system with the load-independent class-EF inverter shown in Fig. 3.8(a) was also designed with the same coupling coils and the receiver circuit as the proposed WPT system. However, there is a difference in the voltage gain between the load-independent class-EF and the proposed inverters. Therefore, the input voltage of the WPT system with the load-independent class-EF inverter was set to  $V_I = 180 \text{ V}$  to obtain the same output voltage as the proposed WPT system. Table 3.2 gives the component values of the WPT system with the load-independent class-EF inverter, which were designed with the on-duty ratio of  $D = 0.3$  [15].

For implementing the WPT system, we selected GS-065-004-1-L GaN E-HEMT from GaN Systems for the switching device, whose on-resistance was  $r_S = 0.45 \Omega$ . Fig. 3.9 shows the output capacitance of the selected GaN E-HEMT as a function of the switch voltage. It is essential for the proposed inverter to select the switching device whose output capacitance is sufficiently low. This is because the analysis given in Section 6.4 does not consider the output capacitance. The T68-6 iron-powder toroidal core from Micrometals was used to implement the series inductance

$L_S$ . The STPS5H100 Schottky Rectifier from STMicroelectronics was adopted for the diode  $D_1$  and  $D_2$ , whose on-resistance, forward voltage, and parasitic capacitance were 0.024  $\Omega$ , 0.49 V, and 90 pF, respectively. The experimental component values are given in Table 3.2, which were measured by E4990A Impedance Analyzer from Keysight Technologies. Fig. 3.10 shows a photograph of the implemented WPT system with the proposed inverter and the class-D rectifier.

### 3.5.2 Operating Waveform

Fig. 7.4(a)-(c) shows the experimental waveforms of the WPT system with the load-independent class-EF inverter. It is seen from Fig. 7.4(a)-(c) that the switch voltage  $v_S$  achieved the ZVS regardless of the load resistance. In addition, the amplitude and the phase shift of the transmission current  $i_1$  were constant even for different load resistances due to the load-independent design. However, the current  $i_1$  comprises significant harmonics due to the specific tuning of the  $L_h$ - $C_h$  for the load-independent design.

Fig. 7.4(d)-(f) shows the experimental waveforms of the WPT system with the proposed inverter. We can see from Fig. 7.4(d)-(f) that the switch current  $i_S$  achieved the ZCS, and the amplitude of current  $i_1$  was constant regardless of the load resistance. The switch voltage at the turn-on moment was reduced, effectively suppressing the turn-on switching loss, as described in Section 3.3.7. Besides, the current  $i_1$  became a sinusoidal waveform despite the absence of the SR filter. The voltage across the diode  $D_1$  was strongly influenced by parasitic capacitance, resulting in long rise and fall times for light load conditions, as given in (3.38). Also, the reac-

tance component seen from the inverter changes with DC load variations due to the parasitic capacitances of the diodes. Nevertheless, the proposed inverter achieves consistent CC operation. This is because the proposed inverter did not use the SR filter and was less sensitive against reactance component variations. These results demonstrate the effectiveness of the proposed inverter.

Fig. 7.4(g)-(i) show the numerical waveforms of the WPT system with the proposed inverter for  $R_L = 100 \Omega$  and  $R_L = 1 \text{ k}\Omega$ . The waveforms are derived using the numerical analysis [32], which considers parasitic components, including the non-linear output capacitance shown in Fig. 3.9, the on-resistances of the switch and diodes, and ESRs of the inductances. We can see from Fig. 7.4(d)-(f) and 7.4(g)-(i) that the experimental and numerical waveforms showed good agreement, which demonstrates the validity of the experimental results.

### 3.5.3 Circuit Characteristics

Fig. 7.5 shows the experimental characteristics of the WPT system with the proposed and load-independent class-EF inverters as a function of normalized load resistance. The experimental power-delivery efficiency was calculated as

$$\eta = \frac{P_O^2}{V_I I_I}, \quad (3.43)$$

where  $P_O$  is the DC-output power.

We can see from Fig. 7.5(a) that the transmission current amplitude of the load-independent class-EF inverter changed at the small load resistance. On the other hand, the proposed inverter maintained consistent CC operation. This is because the proposed inverter exhibits robustness even against reactive-component variations

due to the low- $Q$  output filter. Although relatively large ESRs exist in the coupling coils, they are absorbed by the equivalent resistance seen from the inverter in the S-S coupling. Therefore, the CC operation of the proposed inverter was not significantly affected by the ESRs.

We can see from Fig. 7.5(a) that the output voltage of both WPT systems increased as the load resistance. The output voltage can be constant against load variations in an ideal case where the diodes have no parasitic capacitance, as given in (3.42). However, the effects of the parasitic capacitances appear at high-frequency operations. As a result, the output voltage varied depending on the load resistance, as given in (3.41). The weak output-voltage regulation is an essential issue in the load-independent inverters [11–19]. Therefore, the DC-DC converter is typically added after the rectifier stage [16] for further accuracy of the output regulation. Also, the numerical design method, which can consider the parasitic components of the devices, has been proposed [33]. Although the method has a high computational cost, it is effective for the WPT system with the proposed inverter to increase the accuracy of the output-voltage regulation.

Fig.7.5(b) demonstrates that the WPT system with the proposed inverter achieved the same level of efficiency at heavy load as the WPT system with the load-independent class-EF inverter. However, the efficiency of the proposed inverter decreased at light load. This is because the proposed inverter had a turn-on switching loss, which cannot be negligible at light load. The peak DC-to-DC efficiency 88 % was achieved for 60 W output power in the proposed WPT system.

Fig. 3.13 shows the power-loss breakdown of the WPT system with the proposed inverter, where the subscript of the symbol indicates the power-loss factor. The

power losses are calculated by using the numerical analysis [32], which considers the ESR of inductors, on resistances of the switching device and diodes, the forward voltage of the diodes, and turn-on switching loss as power-loss factors. We can see from Fig. 3.13 that the power-loss due to the ESR of  $L_2$  and the turn-on switching loss are the dominant factors at heavy load. Meanwhile, the power loss due to the ESR of  $L_1$  becomes dominant at the light load. This is because the power loss in the transmitter coil is constant against load variations due to the CC operation, which is the major challenge for the CC inverters. Although CC inverters are naturally inefficient at light loads, they are appropriate for the transmitter of the WPT systems from the perspective of overcurrent protection. The predicted power-delivery efficiency for  $R_L = 100 \Omega$  and  $R_L = 1 \text{ k}\Omega$  are 88.3% and 41.7%, which are quantitatively agrees with the experimental efficiency of 88.0% and 41.3%, respectively.

Fig. 3.14 shows the THD of transmission current  $i_1$  in the WPT system with the class-EF and the proposed inverters. The THD of the transmission current is defined as

$$\text{THD} = \frac{\sqrt{\sum_{n=2}^{\infty} I_{mn}^{*2}}}{I_m^*}, \quad (3.44)$$

where  $I_{mk}^*$  is the normalized amplitude of  $k$ -th harmonic current flowing through transmitter coil. We can see from Fig. 3.14 that the proposed inverter achieved lower THD than the load-independent class-EF inverter over the entire load range. The THD of the load-independent class-EF inverter increases, especially for the small load resistance, because the loaded quality factor of the SR filter becomes small. On the other hand, the proposed inverter inherently outputs a sinusoidal waveform without the SR filter. Therefore, the THD of the output current is almost

constant against load variations.

Based on the experimental results, we can verify that the proposed inverter mitigated harmonic currents in the coupling part of the WPT system. Furthermore, the WPT system incorporating the proposed inverter achieved superior consistency of the CC operation compared to the WPT system with the load-independent class-EF inverter. These results substantiate the effectiveness of the proposed inverter.

### 3.6 Comparison With Previous Works

Table 3.3 gives the load-independent inverters with CC output characteristics proposed so far. The load-independent class-EF inverter [15] has the SR-CC feature, which is suitable for the transmitter of the WPT system. Furthermore, the switch-voltage stress is suppressed by utilizing the harmonic resonant filter. However, the output current suffers from harmonic distortion. The load-independent class-E inverter [14] achieves CC output with a PR output filter. Although the inverter has a floating load, it consists of only four passive elements, contributing to circuit miniaturization. The load-independent push-pull class-E and class- $\Phi$  inverters [19,27] apply the LCCL filter to attain the CC output. The inverters introduce a three-winding coupled inductor, reducing harmonics in the input current. The load-independent class-F/E inverter [21] has a dual topology with the load-independent class-EF inverter [15] and achieves ZCS and CC output regardless of the load resistance with the PR filter.

The proposed inverter has the switch voltage and current waveforms, which are less sensitive against load variations compared with the original class-E inverters.

Moreover, the proposed load-independent inverter can inherently produce a purely sinusoidal output even with a low- $Q$  output filter. Consequently, it exhibits lower sensitivity to component variations in the resonant filter. This unique characteristic represents an advantage of the proposed inverter.

### 3.7 Conclusion

This chapter has presented the analysis and design of the load-independent SR inverter with CC output, along with its WPT system application. The proposed inverter inherently achieves ZCS and a CC output regardless of the load resistance. Furthermore, the proposed inverter can generate a sufficiently pure sinusoidal output even with a low- $Q$  SR filter. In the experiment, the WPT system that incorporates the proposed inverter as the transmitter was implemented. The experimental results demonstrated that the proposed inverter achieved superior consistency of the CC operation and reduced THD of current flowing through the transmitter coil compared with the WPT system employing the load-independent class-EF inverter. The experimental results showed the validity of the inverter design and analysis.

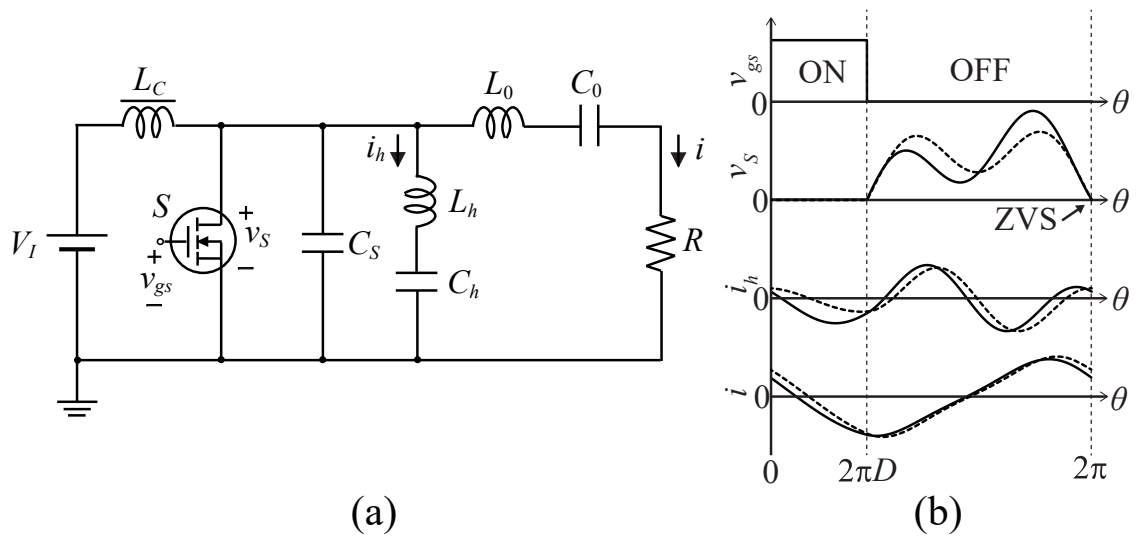


Fig. 3.1: The load-independent class-EF inverter. (a) Circuit topology. (b) Example waveforms at fixed load resistances (solid line:  $R/R_r = 1$ , dashed line:  $R/R_r = 0.1$ .)

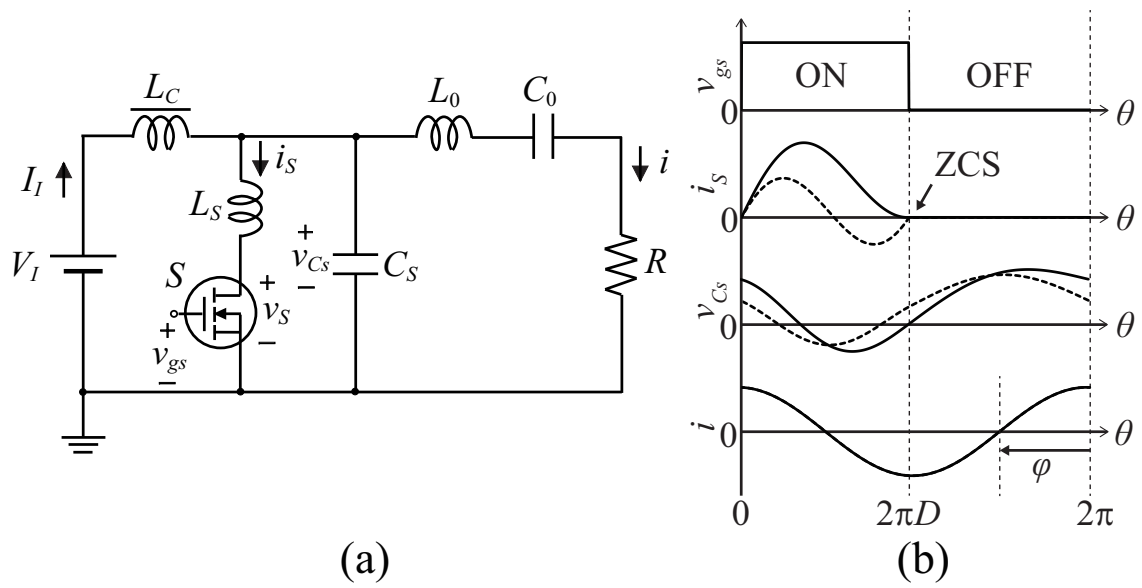


Fig. 3.2: Proposed inverter. (a) Circuit topology. (b) Example waveforms for fixed load resistances (solid line:  $R/R_r = 1$ , dashed line:  $R/R_r = 0.1$ .)

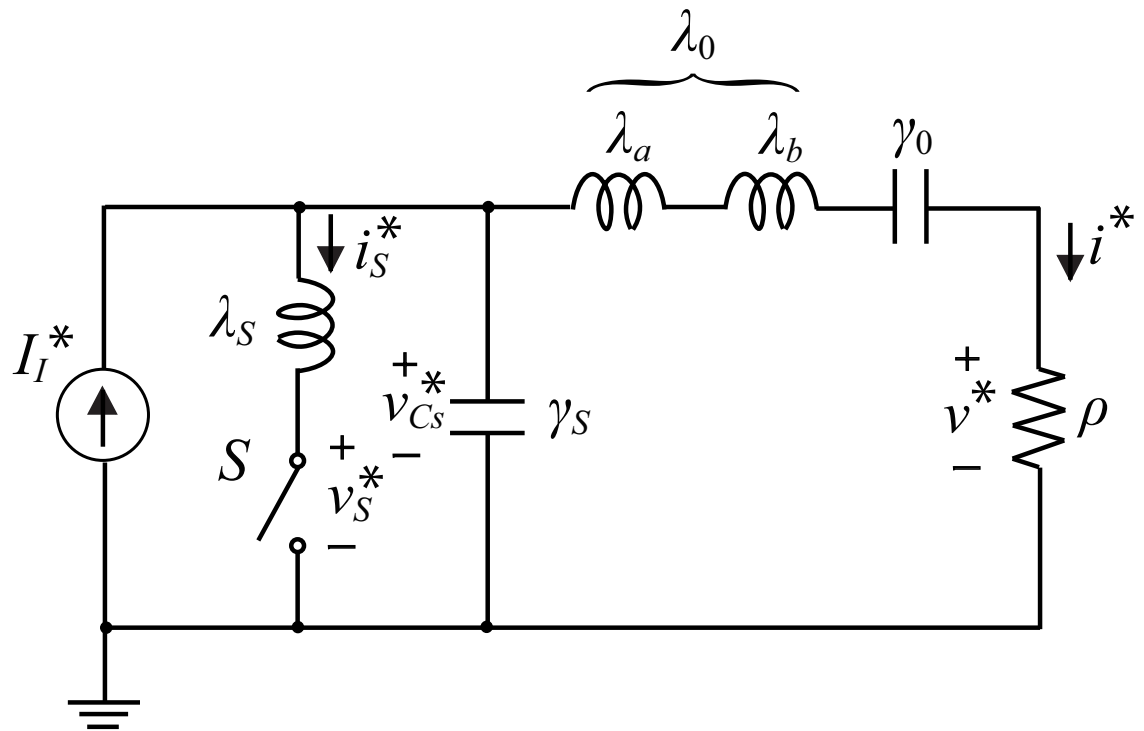


Fig. 3.3: Analytical model of the proposed inverter.

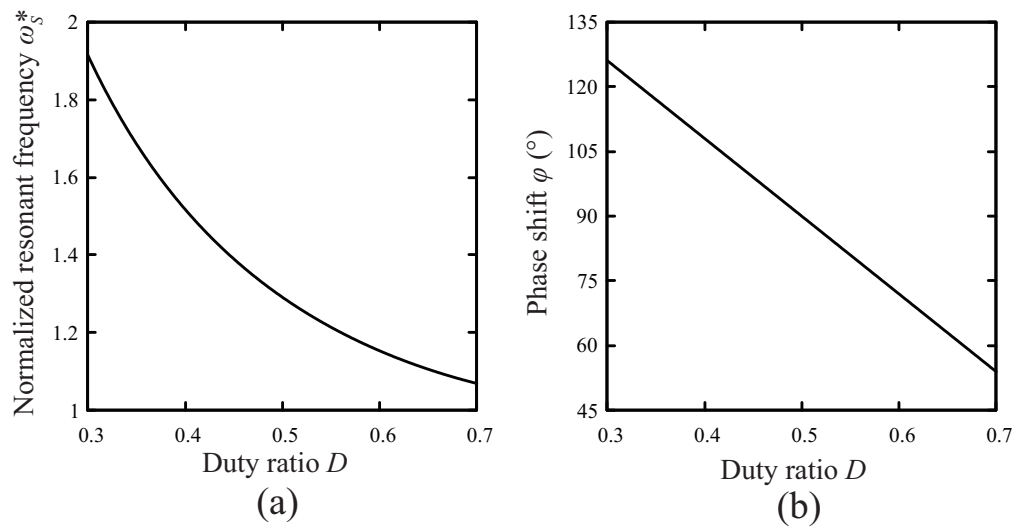


Fig. 3.4: The circuit parameters that satisfy the load-independent conditions as functions of duty ratio  $D$ . (a) The normalized resonant angular frequency  $\omega_s^*$ . (b) The phase shift between output current and gate-drive voltage.

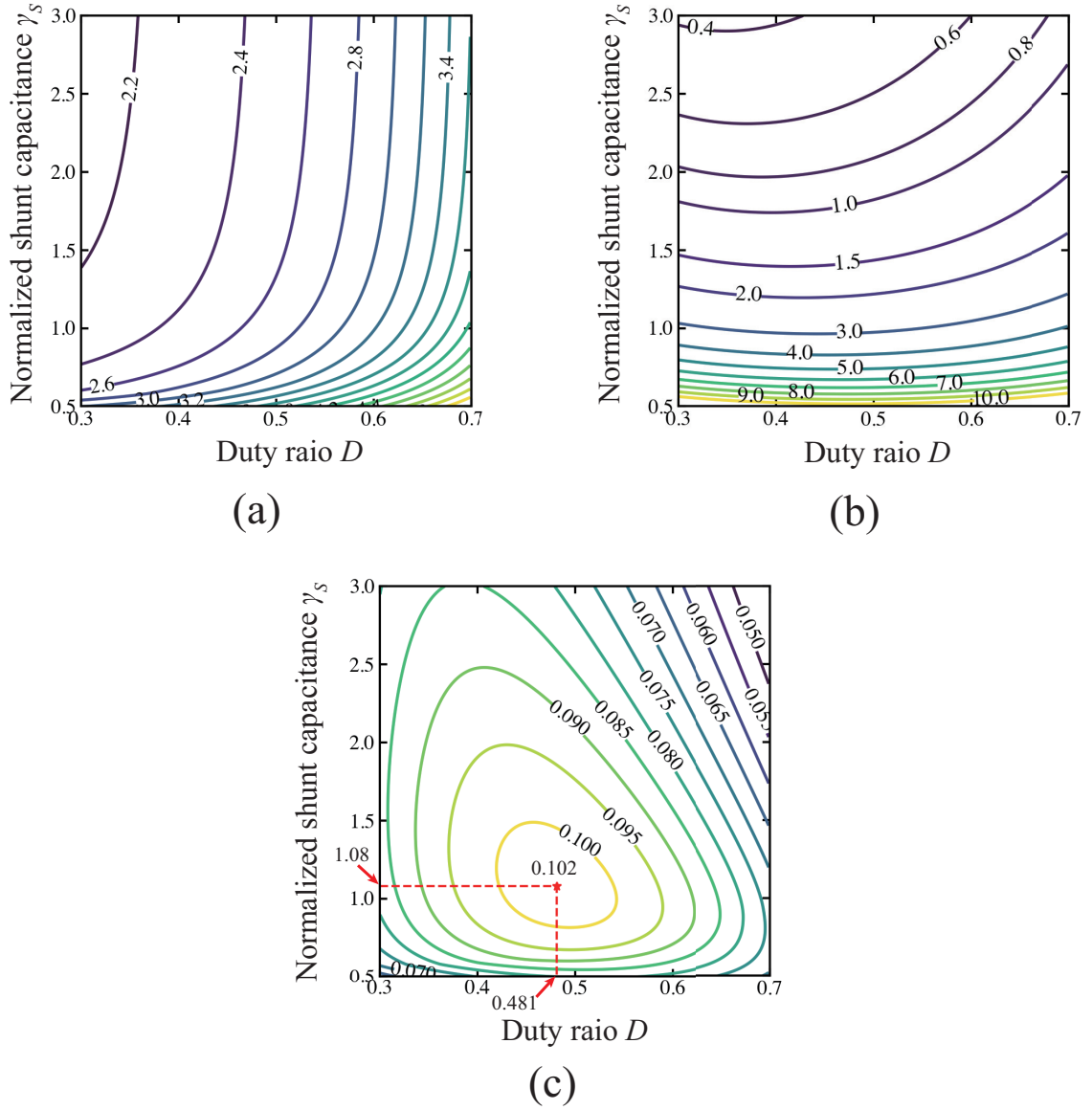


Fig. 3.5: Inverter characteristics as functions of duty ratio  $D$  and normalized shunt capacitance  $\gamma_s$ . (a) Switch-voltage stress  $V_{Smax}^*$ . (b) Switch-current stress  $I_{Smax}^*$ . (c) Power-output capability.

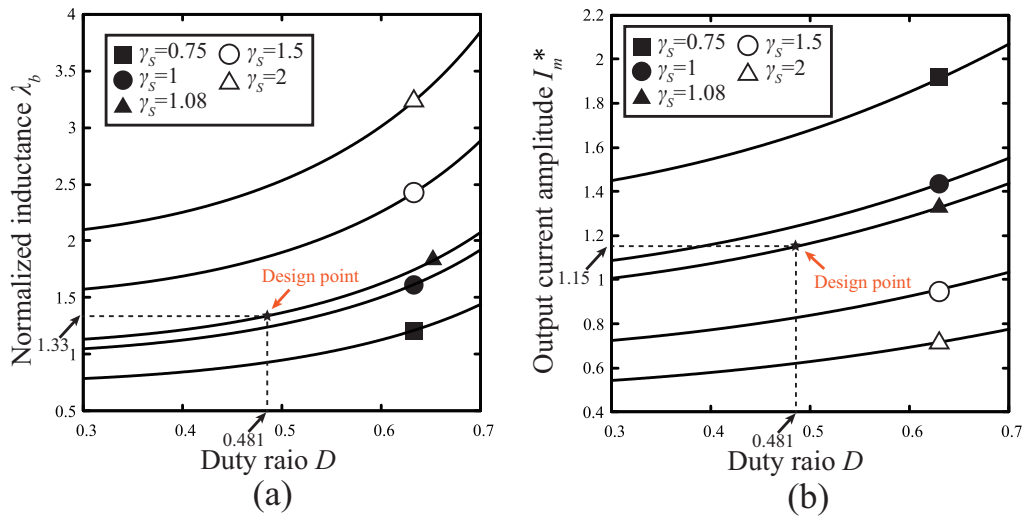


Fig. 3.6: Design curves of the proposed inverter as functions of duty ratio  $D$ . (a) Normalized inductance  $\lambda_b$ . (b) Normalized output-current amplitude  $I_m^*$ .

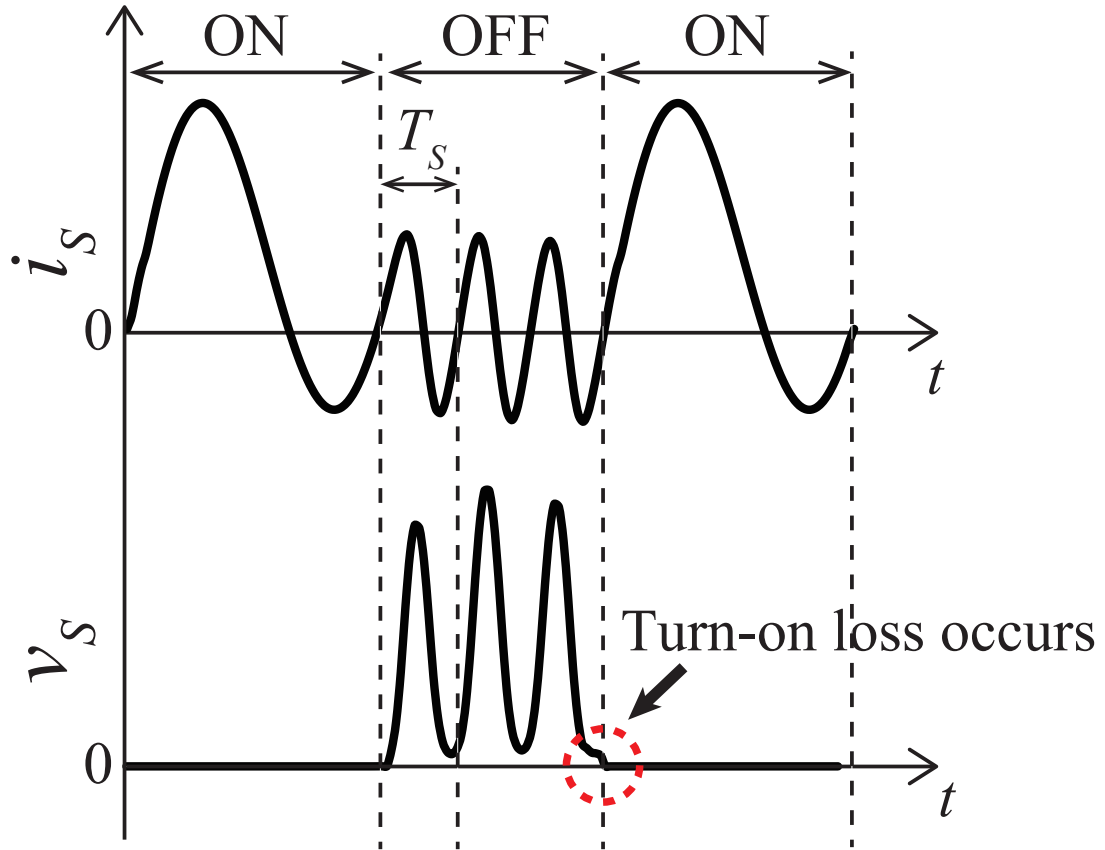


Fig. 3.7: The example waveforms of switch current and voltage of the proposed inverter.

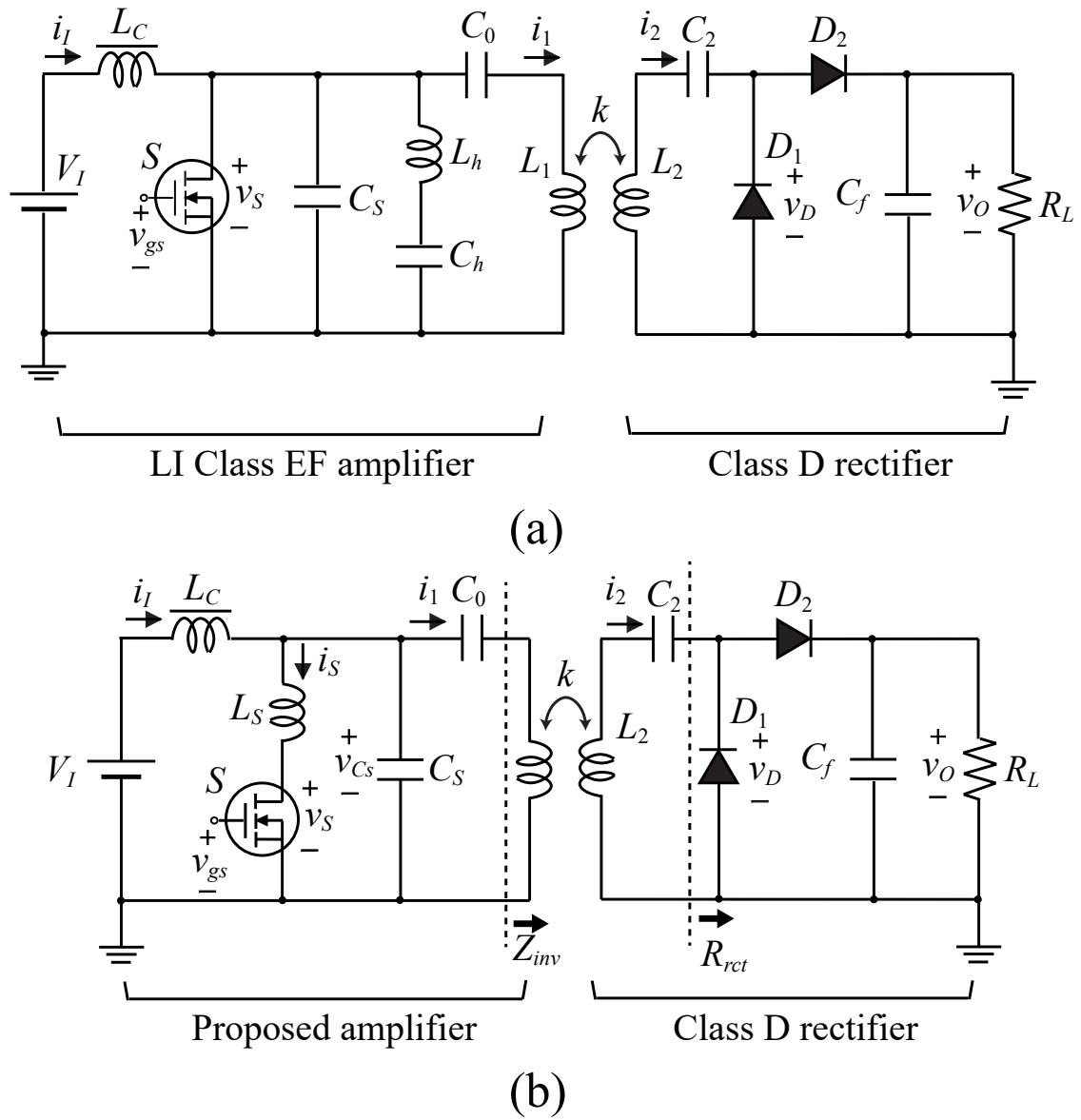


Fig. 3.8: The circuit configurations of the WPT system. (a) With the load-independent class-EF inverter. (b) With the proposed inverter.

Table 3.1: Geometric parameters of transmitter and receiver coils.

	$h_{core}$	$d_{core}$	$N$	$d_w$
Transmitter coil	15 mm	60 mm	6	1.2 mm
Receiver coil	12 mm		6	1.2 mm

Table 3.2: Analytical and measured component values of the WPT systems.

Load-Independent class-EF WPT system			WPT system with proposed inverter		
	Analytical	Experiment		Analytical	Experiment
$L_C$	-	150 $\mu\text{H}$	$L_C$	-	150 $\mu\text{H}$
$L_h$	7.07 $\mu\text{H}$	7.04 $\mu\text{H}$	$L_S$	2.42 $\mu\text{H}$	2.42 $\mu\text{H}$
$C_S$	147 pF	100 pF	$C_S$	519 pF	519 pF
$C_0$	20.4 nF	19.8 nF	$C_0$	-	1.0 $\mu\text{F}$
$C_h$	112 pF	111 pF	$C_2$	372 pF	371 pF
$C_2$	372 pF	371 pF	$C_f$	-	1.0 $\mu\text{F}$
$C_f$	-	1.0 $\mu\text{F}$	$r_{L_C}$	-	100 m $\Omega$
$r_{L_C}$	-	100 m $\Omega$	$r_{L_S}$	-	178 m $\Omega$
$r_{L_h}$	-	304 m $\Omega$			

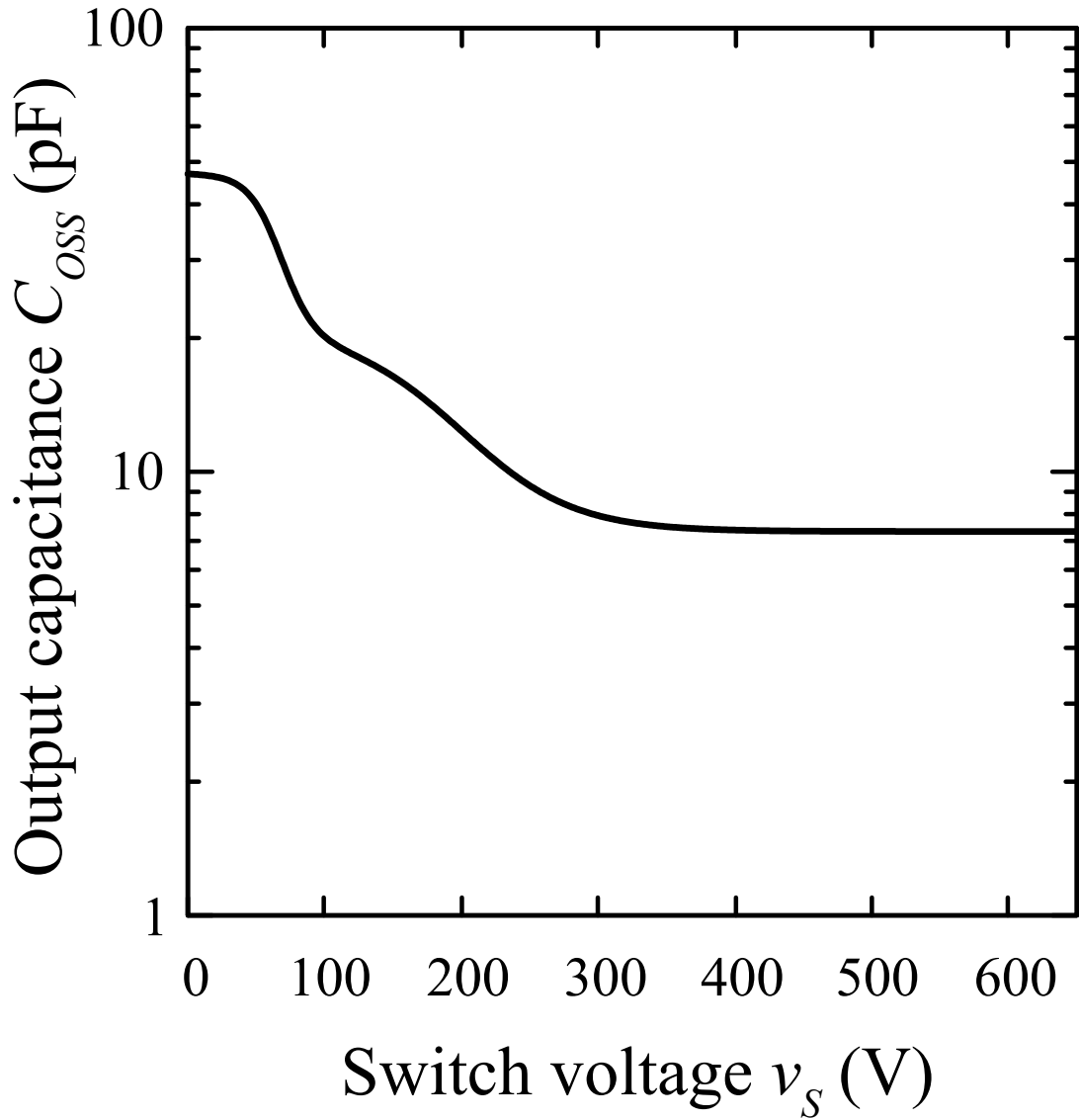


Fig. 3.9: The output capacitance of the selected GaN E-HEMT as a function of the switch voltage.

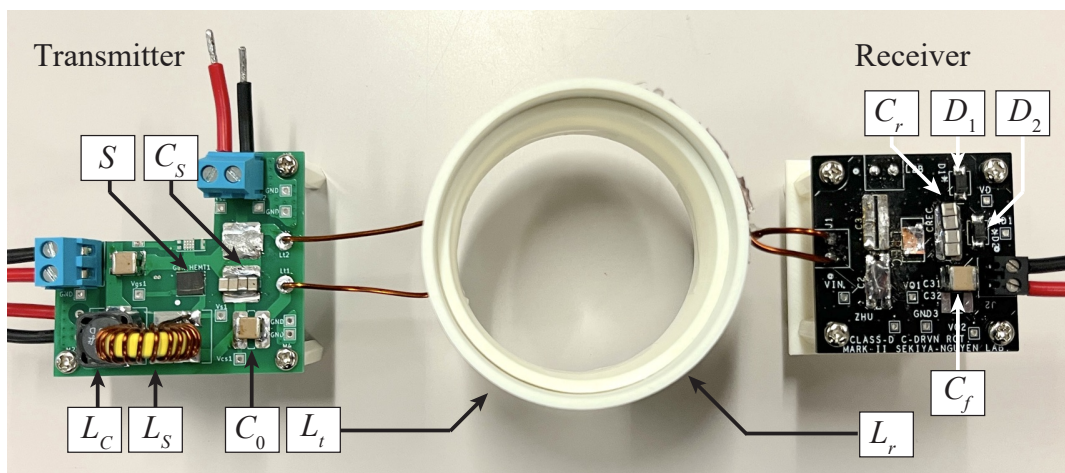


Fig. 3.10: Photograph of the implemented proposed WPT system.

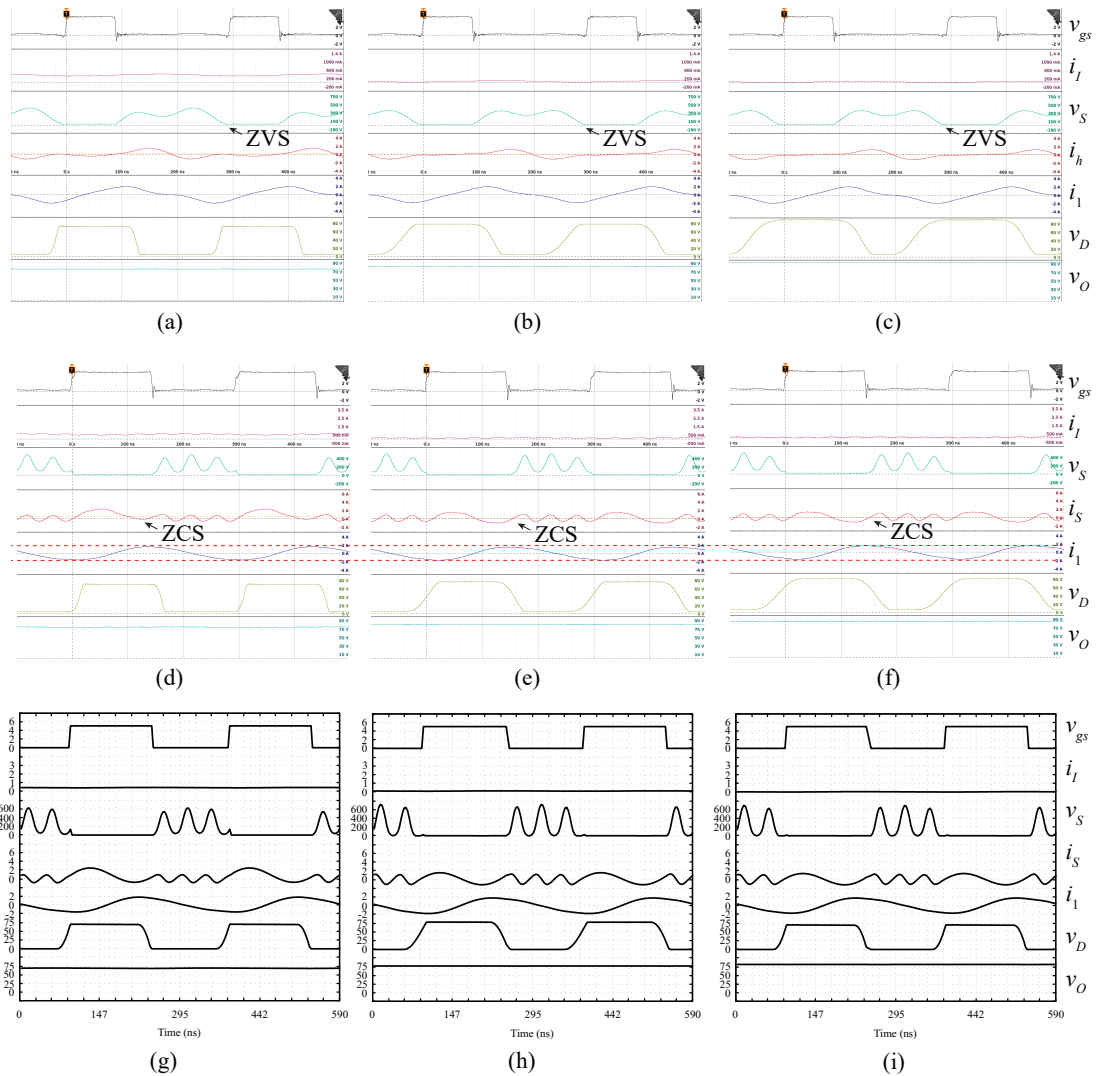


Fig. 3.11: Experimental and numerical waveforms of the WPT systems. (a) With the load-independent class-EF inverter for  $R_L = 100 \Omega$  (Experiment). (b) With the load-independent class-EF inverter for  $R_L = 1 \text{ k}\Omega$  (Experiment). (c) With the load-independent class-EF inverter for open load (Experiment). (d) With the proposed inverter for  $R_L = 100 \Omega$  (Experiment). (e) With the proposed inverter for  $R_L = 1 \text{ k}\Omega$  (Experiment). (f) With the proposed inverter for open load (Experiment). (g) With the proposed inverter for  $R_L = 100 \Omega$  (Numerical). (h) With the proposed inverter for  $R_L = 1 \text{ k}\Omega$  (Numerical). (i) With the proposed inverter for open load (Numerical).

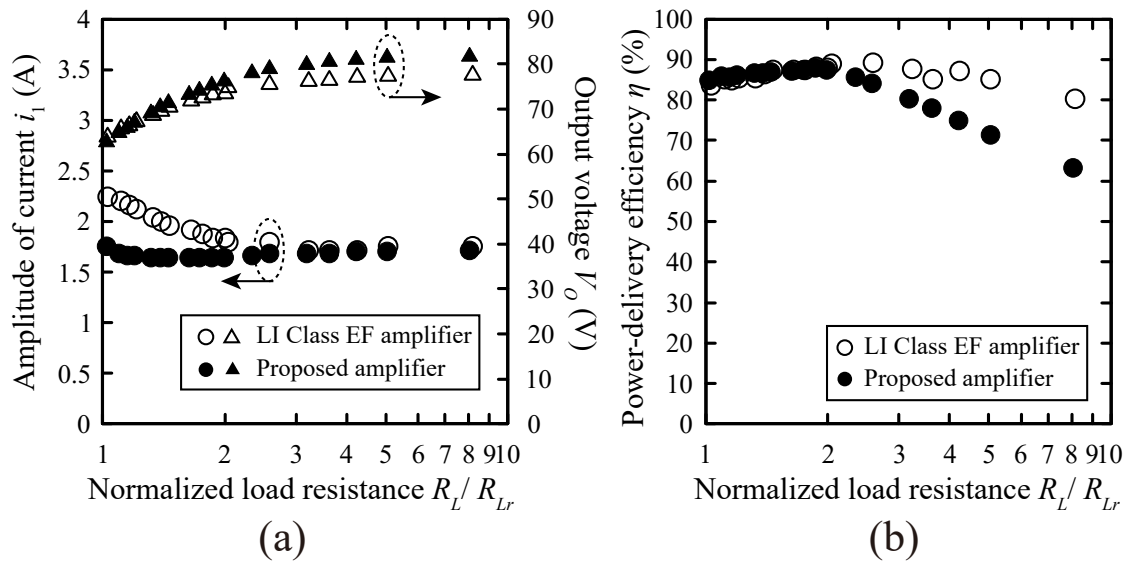


Fig. 3.12: Experimental characteristics of the WPT system with the load-independent class-EF and the proposed inverters as a function of normalized load resistance. (a) Amplitude of the current  $i_1$  and output voltage  $V_O$ . (b) Power-delivery efficiency  $\eta$ .

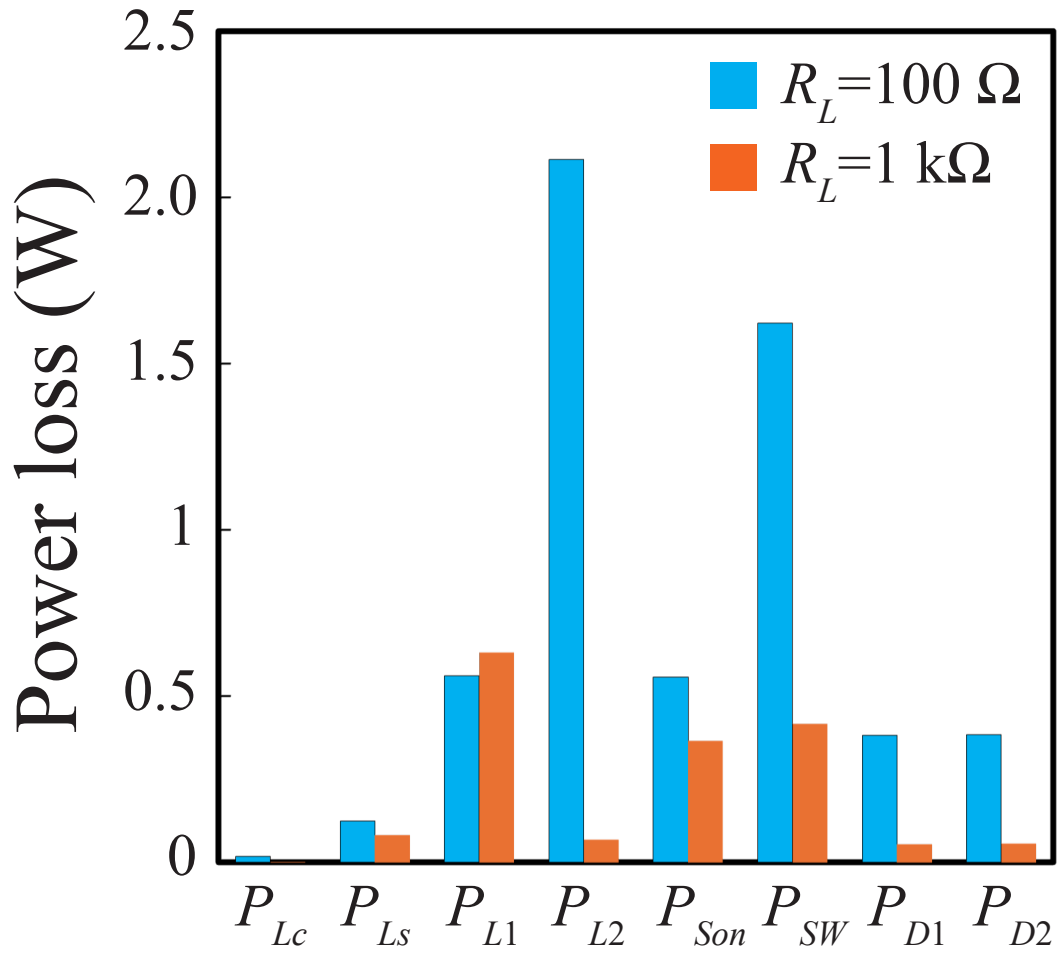


Fig. 3.13: Power-loss breakdown of the WPT system with the proposed inverter for  $R_L = 100 \Omega$  and  $R_L = 1 \text{ k}\Omega$ .

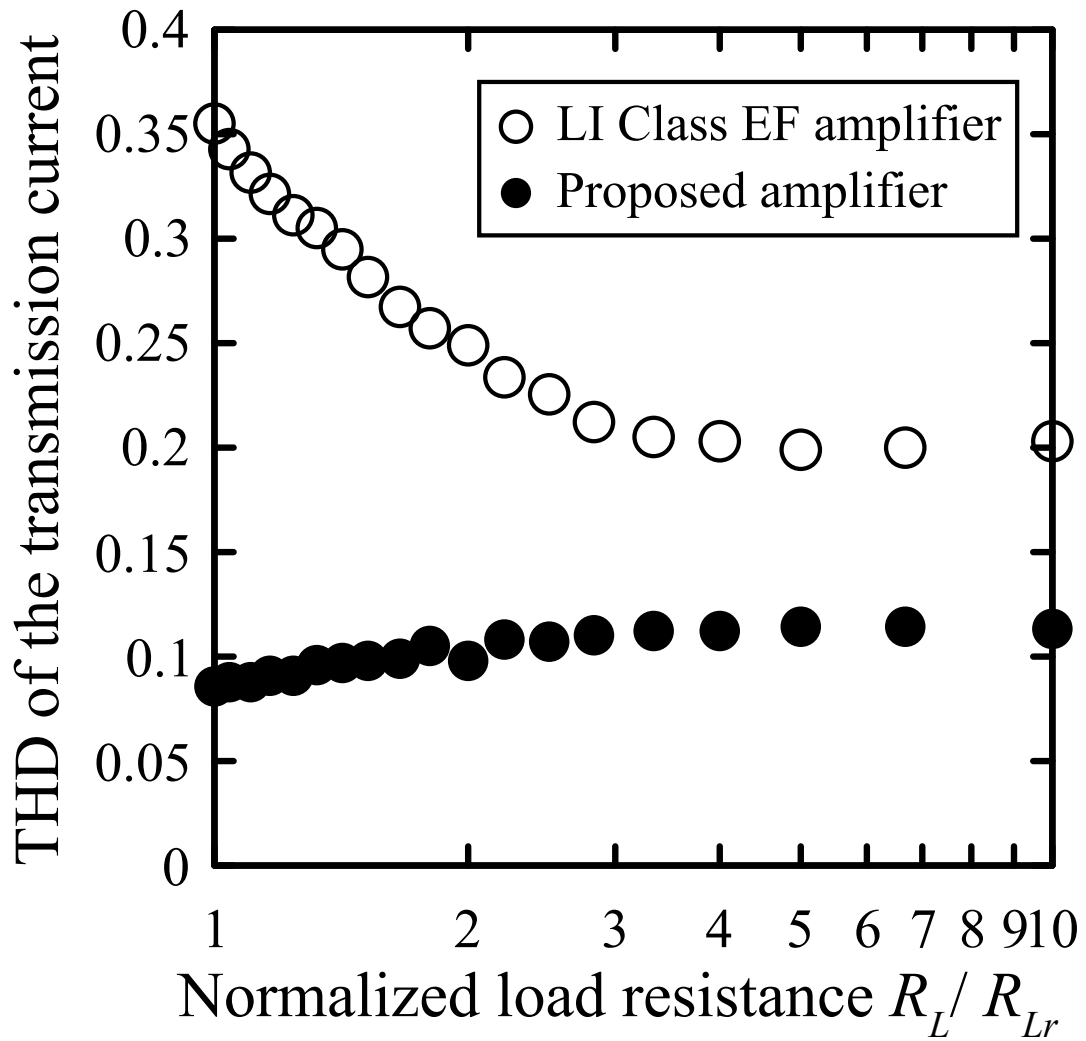


Fig. 3.14: The THD of the output current as a function of normalized load resistance.

Table 3.3: Load-independent inverters with CC output feature.

	Aldhaher [15]	Tomohiro [14]	Huang [27]	Huang [19]	Zhu [21]	This work
Circuit topology	class-EF	class-E	Push-pull class-E	Push-pull class- $\Phi$	class-F/E	Inverse class-E
Output resonant filter	Series	Parallel	LCCL	LCCL	Parallel	Series
Component number	6	4	7	8	5 or 7	5
Switching type	ZVS	ZVS	ZVS	ZVS	ZCS	ZCS
Output	CC	CC	CC	CC	CC	CC
Power-output capability	0.0882	0.101	-	-	0.085	0.102
Frequency (MHz)	13.56	1	6.78	6.78	1	3.39
Output power (W)	14-150	0.3-11.5	0-320	70-320	2.5-25	0-75
Efficiency	94.4% (DC/AC)	89.3% (DC/AC)	89.3% (DC/DC)	91% (DC/DC)	94.2% (DC/AC)	88.0% (DC/DC)

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## Chapter 4

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# Load-Independent Class- $\Phi_3$ Inverter

### 4.1 Introduction

Wide-bandgap semiconductor devices such as GaN and SiC expand the operating range of power electronic circuits, especially in the high-frequency regime [1]. In high-frequency operation, the energy-storage requirement of the circuit can be reduced, which reduces the physical size of passive components. As a result, the power density of the circuits can be increased. However, the high-frequency operation increases the switching losses proportionally. Therefore, high-frequency inverters are mandatory to achieve ZVS to suppress the switching losses [2, 3].

The circuit design that accounts for load variations is also a critical challenge for power electronics circuits. A specific control is typically applied to maintain high power-conversion efficiency and output regulation against the load variations [4, 5]. However, the requirements for PWM resolution become more stringent in high-frequency regimes, leading to the difficulty in maintaining control accuracy and stability. Hence, a fundamental solution to load variations in high-frequency power

electronics circuits at the megahertz band has been strongly demanded. Recently, the load-independent inverters [6–13], which exhibit robustness against load variations, have attracted much attention. The load-independent inverters inherently achieve the ZVS and a constant AC output against the load variations. Therefore, the load-independent inverters eliminate the need for applying controls, paving a new way to address load variations.

The load-independent designs have been realized in various circuit topologies so far [6–13]. Among them, the load-independent class- $\Phi_2$  inverter [9–13] has been widely studied aiming at applications such as wireless power transfer systems [9] and inverters for plasma generation [10]. The load-independent class- $\Phi_2$  inverter achieves the ZVS against load variations. Additionally, it maintains the constant amplitude of the output AC voltage regardless of the load resistance. The load-independent operation can be realized by tuning the component values properly, whose design conditions are clarified analytically [9]. Another essential aspect of the load-independent class- $\Phi_2$  inverter is its reduced switch-voltage stress. The load-independent class- $\Phi_2$  inverter has a harmonic series-resonant filter parallel to the switch, which is tuned at twice the switching frequency. As a result, the peak switch voltage is effectively reduced, allowing wider device selection.

The class- $\Phi_3$  inverter [14–16] has another operating mode in the same circuit topology as the class- $\Phi_2$  inverter. The class- $\Phi_3$  inverter tunes the harmonic resonant filter at three times the switching frequency. Compared with the class- $\Phi_2$  inverter, the class- $\Phi_3$  inverter reduces the peak switch voltage at OFF-duty ratios of 50 % or less [15]. Moreover, the class- $\Phi_3$  inverter has a larger input-output voltage gain, achieving higher power-output capability [16]. However, the feasibility of achieving

the load-independent operation in the class- $\Phi_3$  inverter has never been explored. The class- $\Phi_3$  inverter boasts superior power-output capability, suggesting a potential for enhancing the power-conversion efficiency.

This chapter proposes the design of the load-independent class- $\Phi_3$  resonant inverter. We analyze the class- $\Phi_3$  inverter and reveal that the load-independent operation is feasible in the class- $\Phi_3$  operation. Namely, the load-independent class- $\Phi_3$  inverter achieves the ZVS and a constant output-voltage amplitude regardless of the load resistance. The design conditions for achieving the load-independent operation are analytically described in this chapter. The experiment verifications were carried out to confirm the validity of the proposed design. In the experiment, the load-independent class- $\Phi_3$  inverter achieved higher power-conversion efficiency over a wide range of load variations compared with the load-independent class- $\Phi_2$  inverter, which substantiates the effectiveness of the proposed inverter.

## 4.2 Load-Independent Inverters

Fig. 4.1 shows the circuit topology of the load-independent class- $\Phi_2$  and class- $\Phi_3$  inverters, which have identical circuit topology. The circuit is composed of input finite-inductor  $L_1$ , shunt capacitor  $C_1$ , harmonic resonant filter  $L_2$ - $C_2$ , series resonant filter  $L_3$ - $C_3$ , and load resistance  $R_L$ . The harmonic resonant filter  $L_2$ - $C_2$  is tuned at twice and three times the switching frequency in the load-independent class- $\Phi_2$  and class- $\Phi_3$  inverters, respectively. Accordingly, the sets of component values for achieving the load-independent operation are totally different between the load-independent class- $\Phi_2$  and class- $\Phi_3$  inverters.

### 4.2.1 Load-Independent Class- $\Phi_2$ Inverter

Fig. 4.2(a) shows the example waveforms of the load-independent class- $\Phi_2$  inverter for fixed load resistances, where  $\theta = \omega t = 2\pi ft$  is the phase angle,  $\omega$  represents the switching angular frequency,  $f$  indicates the switching frequency, and  $D$  is the OFF-duty ratio. Besides, the subscript ‘ $r$ ’ means its rated value. We can see from Fig. 4.2(a) that the frequency of current  $i_2$  is twice higher than the output voltage. Owing to the harmonic current, the switch voltage is in a trapezoidal shape, effectively suppressing the voltage stress. The output sinusoidal voltage is obtained by extracting the fundamental frequency component from the switch voltage through the series resonant filter  $L_3$ - $C_3$ .

The load-independent class- $\Phi_2$  inverter achieves the ZVS regardless of the load resistance  $R_L$ , as shown in Fig. 4.2(a). Additionally, the amplitude of the output AC voltage is also independent of the load. The load-independent operation can be obtained by tuning the component values properly. Therefore, additional controls and circuits are not required to achieve high efficiency and output regulation against load variations.

### 4.2.2 Load-Independent Class- $\Phi_3$ Inverter

Fig. 4.2(b) shows the example waveforms of the load-independent class- $\Phi_3$  inverter for fixed load resistances. The load-independent class- $\Phi_3$  inverter achieves the ZVS and constant output voltage regardless of the load resistance, the same as the class- $\Phi_2$  inverter. In the class- $\Phi_3$  operation, the third-harmonic current flows through  $L_2$ - $C_2$ . The harmonic current suppresses the peak switch voltage and current si-

multaneously, as shown in Fig. 4.2(b). Additionally, the output voltage is larger than the class- $\Phi_2$  inverter for the same input voltage. As a result, the power-output capability is improved compared with the class- $\Phi_2$  inverter.

### 4.3 Circuit Analysis

Circuit analysis for the load-independent class- $\Phi_3$  inverter is performed based on the following assumptions.

1. The quality factor of the harmonic resonant filter  $L_2$ - $C_2$  and the series resonant filter  $L_3$ - $C_3$  are sufficiently high so that the currents flowing through these branches can be regarded as pure sinusoidal waves as

$$i_2(\theta) = I_2 \sin(3\theta + \varphi_2), \quad (4.1)$$

and

$$i_O(\theta) = I_m \sin(\theta + \varphi), \quad (4.2)$$

where  $I_2$  and  $I_m$  are the amplitudes, and  $\varphi_2$  and  $\varphi$  are the phase shifts from the turn-OFF timing of the switch.

2. The resonant inductor  $L_3$  is divided into the resonant component  $L_R$  and extra inductance  $L_X$ . The  $L_R$  and  $C_3$  is resonate with the switching frequency as

$$\omega = \frac{1}{\sqrt{L_R C_3}}. \quad (4.3)$$

3. The switching device is modeled as an ideal switch, which turns OFF during  $0 \leq \theta < 2\pi D$  and turns ON during  $2\pi D \leq \theta < 2\pi$ . Besides, the output capacitance of the switching device is absorbed into the shunt capacitance  $C_1$ .

4. Each passive component works linearly with no parasitic components.

Fig. 4.3 shows the analytical circuit model, which is derived from the above assumptions.

### 4.3.1 Waveform equations

For the switch turn-OFF period, a differential equation can be obtained from KCL as

$$\begin{aligned} \frac{d^2 v_S(\theta)}{d\theta^2} + \omega_1^2 v_S(\theta) = \omega_1^2 [V_I - \omega L_1 I_m \cos(\theta + \varphi) \\ - 3\omega L_1 I_2 \cos(3\theta + \varphi_2)], \end{aligned} \quad (4.4)$$

where

$$\omega_1 = \frac{1}{\omega \sqrt{L_1 C_1}}, \quad (4.5)$$

is the normalized resonant frequency between  $L_1$  and  $C_1$ . By solving (6.15), the analytical expression of the switch voltage during the turn-OFF period can be obtained as

$$\begin{aligned} v_S(\theta) = A \cos(\omega_1 \theta) + B \sin(\omega_1 \theta) + V_I \\ - \frac{\omega L_1 \omega_1^2 I_m}{\omega_1^2 - 1} \cos(\theta + \varphi) - \frac{3\omega L_1 \omega_1^2 I_2}{\omega_1^2 - 9} \cos(3\theta + \varphi_2), \end{aligned} \quad (4.6)$$

where  $A$  and  $B$  are constants.

From KVL, we obtain

$$\frac{di_1(\theta)}{d\theta} = \frac{1}{\omega L_1} [V_I - v_S(\theta)]. \quad (4.7)$$

By using (6.17) and (6.18), we obtain the expression of current  $i_1$  during turn-OFF period as

$$i_1(\theta) = -\frac{\omega_1[A \sin(\omega_1\theta) - B \cos(\omega_1\theta)]}{\omega L_1} + \frac{\omega_1^2 I_m \sin(\theta + \varphi)}{\omega_1^2 - 1} + \frac{\omega_1^2 I_2 \sin(3\theta + \varphi_2)}{\omega_1^2 - 9} \quad (4.8)$$

For the switch turn-ON period, the switch voltage becomes zero as

$$v_S(\theta) = 0. \quad (4.9)$$

From KVL, we obtain

$$\frac{di_1(\theta)}{d\theta} = \frac{V_I}{\omega L_1}. \quad (4.10)$$

From (6.19) and (6.21), we obtain the expression of  $i_1$  during turn-ON period as

$$i_1(\theta) = \frac{V_I(\theta - 2\pi D) - \omega_1[A \sin(2\pi D\omega_1) - B \cos(2\pi D\omega_1)]}{\omega L_1} + \frac{\omega_1^2 I_m \sin(2\pi D + \varphi)}{\omega_1^2 - 1} + \frac{\omega_1^2 I_2 \sin(6\pi D + \varphi_2)}{\omega_1^2 - 9} \quad (4.11)$$

### 4.3.2 Boundary Conditions

The unknown constants  $A$  and  $B$  can be obtained from the boundary conditions of the waveform equations, which can be described as

$$i_1(0) = i_1(2\pi), \quad (4.12)$$

and

$$\left. \frac{di_1(\theta)}{d\theta} \right|_{\theta=0} = \left. \frac{di_1(\theta)}{d\theta} \right|_{\theta=2\pi}. \quad (4.13)$$

From (6.19) and (6.24)-(6.26), we obtain

$$A = \frac{1}{\omega C_1} \left( \frac{I_m \cos \varphi}{\omega_1^2 - 1} + \frac{3I_2 \cos \varphi_2}{\omega_1^2 - 9} - \frac{V_I}{\omega L_1 \omega_1^2} \right), \quad (4.14)$$

and

$$B = \frac{1}{\omega C_1 \omega_1 [1 - \cos(2\pi D \omega_1)]} \left\{ \frac{2\pi(1-D)V_I}{\omega L_1} - \omega_1 \left( \frac{I_m \cos \varphi}{\omega_1^2 - 1} + \frac{3I_2 \cos \varphi_2}{\omega_1^2 - 9} - \frac{V_I}{\omega L_1 \omega_1^2} \right) \sin(2\pi D \omega_1) + \frac{\omega_1^2 I_m [\sin(2\pi D + \varphi) - \sin \varphi]}{\omega_2 - 1} + \frac{\omega_1^2 I_2 [\sin(2\pi D + \varphi_2) - \sin \varphi_2]}{\omega_2 - 9} \right\}, \quad (4.15)$$

### 4.3.3 Design Conditions

The  $L_2$  and  $C_2$  are in complete resonance with the resonant frequency of  $3f$ , shorting out the third harmonic current. Therefore, the third harmonic component in the switch voltage is eliminated. From the Fourier series expansion, we obtain

$$\frac{1}{\pi} \int_0^{2\pi} v_S(\theta) \sin(3\theta + \varphi_2) = 0, \quad (4.16)$$

and

$$\frac{1}{\pi} \int_0^{2\pi} v_S(\theta) \cos(3\theta + \varphi_2) = 0, \quad (4.17)$$

The  $L_3$  and  $C_3$  are tuned to pass only the fundamental frequency component but are designed to be slightly inductive to achieve the ZVS. Namely, from the Fourier series expansion, we obtain

$$\frac{1}{\pi} \int_0^{2\pi} v_S(\theta) \sin(\theta + \varphi) = R_L I_m = V_m, \quad (4.18)$$

and

$$\frac{1}{\pi} \int_0^{2\pi} v_S(\theta) \cos(\theta + \varphi) = \omega L_X I_m, \quad (4.19)$$

where  $V_m$  is the amplitude of the output voltage, and  $L_X$  is the extra inductive component.

To achieve the load-independent operation, the amplitude of the output voltage must be independent of the load resistance. Besides, the ZVS should be achieved at the turn-ON instant. Therefore, the following conditions must be simultaneously achieved.

$$\frac{dV_m}{dR_L} = 0, \quad (4.20)$$

and

$$v_S(2\pi D) = 0, \quad (4.21)$$

From (6.17), (6.20), and (6.27)-(6.31), values of  $I_m$ ,  $I_2$ ,  $\omega_1$ ,  $\varphi$ ,  $\varphi_2$ , and  $L_X$  that achieves the load-independent operation are determined for fixed shunt capacitance  $C_1$  and duty ratio  $D$ .

## 4.4 Experimental Verification

The design specifications of the load-independent class- $\Phi_3$  inverter is given as switching frequency  $f = 6.78$  MHz, input voltage  $V_I = 25$  V, rated load resistance  $R_{Lr} = 10 \Omega$ , and quality factor  $Q_r = \omega L_3 / R_{Lr} = 10$ . The shunt capacitance  $C_1$  and the OFF-duty ratio of the class- $\Phi_3$  inverter were obtained as  $C_1 = 222$  pF

and  $D = 0.41$ , respectively, for maximizing the power-output capability. Also, we experimented with the load-independent class- $\Phi_2$  inverter in the same specifications for comparison.

Table 4.1 gives the component values, which are determined from the analysis provided in Section 6.4. Based on the design specifications and component values, we selected the passive component and devices, as given in Table 4.3. The selected switching device of GS61004B has an output capacitance of 110 pF with non-linearity. Therefore, the component values of the shunt capacitance  $C_1$  in Table 4.1 have a relatively large difference between analytical and measured values. Fig. 4.4 shows an implemented class- $\Phi_3$  inverter.

Fig. 6.11 shows the experimental and analytical waveforms of the load-independent class- $\Phi_2$  and class- $\Phi_3$  inverters for fixed load resistances. We can see that the experimental and analytical waveforms are in good agreement, confirming the validity of the analysis given in Section 6.4. We can see from Figs. 6.11(a)-(c) and 6.11(d)-(f) that both the load-independent class- $\Phi_2$  and class- $\Phi_3$  inverters achieved the ZVS and constant output-voltage amplitude against load variations. From these results, we confirmed that the load-independent design can also be realized in the class- $\Phi_3$  inverter. The measured output powers of the load-independent class- $\Phi_2$  and class- $\Phi_3$  inverters at the rated condition were 42.4 W and 75.2 W, respectively. Namely, higher output power can be obtained in the load-independent class- $\Phi_3$  at the same input voltage.

Fig. 6.6 shows the experimental and analytical characteristics of the load-independent class- $\Phi_2$  and class- $\Phi_3$  inverters as a function of normalized load resistance. The analytical power-conversion efficiency is derived considering the equivalent series resis-

tance of the inductors and ON-resistance of the switching device as the power-loss factors. We can see from Fig. 6.6(a) that the amplitude of the output voltage is constant against load variations in both the load-independent class- $\Phi_2$  and class- $\Phi_3$  inverters. Meanwhile, from Fig. 6.6(b), we can see that the load-independent class- $\Phi_3$  inverter achieved higher efficiency than the load-independent class- $\Phi_2$  inverter. This is because the power loss in the ESR of  $L_2$  was higher in the load-independent class- $\Phi_2$  design.

These results confirm that the load-independent class- $\Phi_3$  inverter achieved the load-independent operation and improved efficiency than the load-independent class- $\Phi_2$  inverter, demonstrating the effectiveness of the proposed design.

## 4.5 Performance Comparison

Table 4.3 gives the comparison between the load-independent class- $\Phi_2$  and  $\Phi_3$  inverters. We can see from Table 4.3 that the class- $\Phi_2$  inverter has lower switch-voltage stress for a given input voltage. The switch-current stresses are comparable for the two inverters. Meanwhile, the load-independent class- $\Phi_3$  inverter has a larger output voltage for the same input voltage than the load-independent class- $\Phi_2$  inverter. Consequently, the load-independent class- $\Phi_3$  inverter achieves an improved power-output capability of 0.137.

## 4.6 Conclusion

This chapter has proposed the design of the load-independent class- $\Phi_3$  inverter. The load-independent class- $\Phi_3$  inverter achieves the ZVS and constant AC output voltage regardless of the load resistance. Additionally, it achieves higher efficiency and power-output capability than the load-independent class- $\Phi_2$  inverter. In the experiment, the load-independent class- $\Phi_3$  inverter achieved 87.5 %-95.9 % power-conversion efficiency within a tenfold change in the load resistance, showing the effectiveness of the proposed inverter.

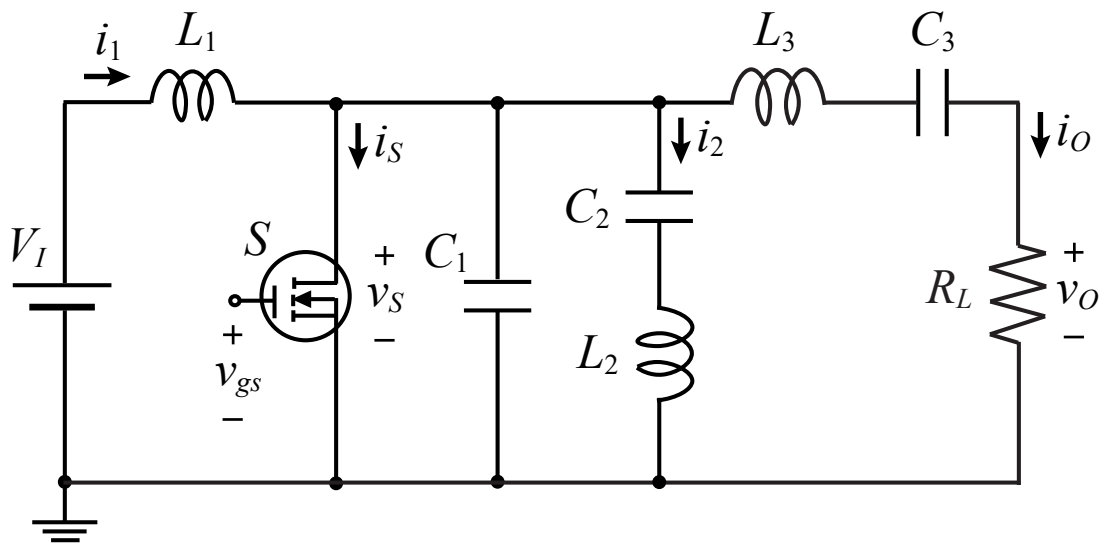


Fig. 4.1: Circuit topology of the load-independent class- $\Phi_2$  and class- $\Phi_3$  inverters.

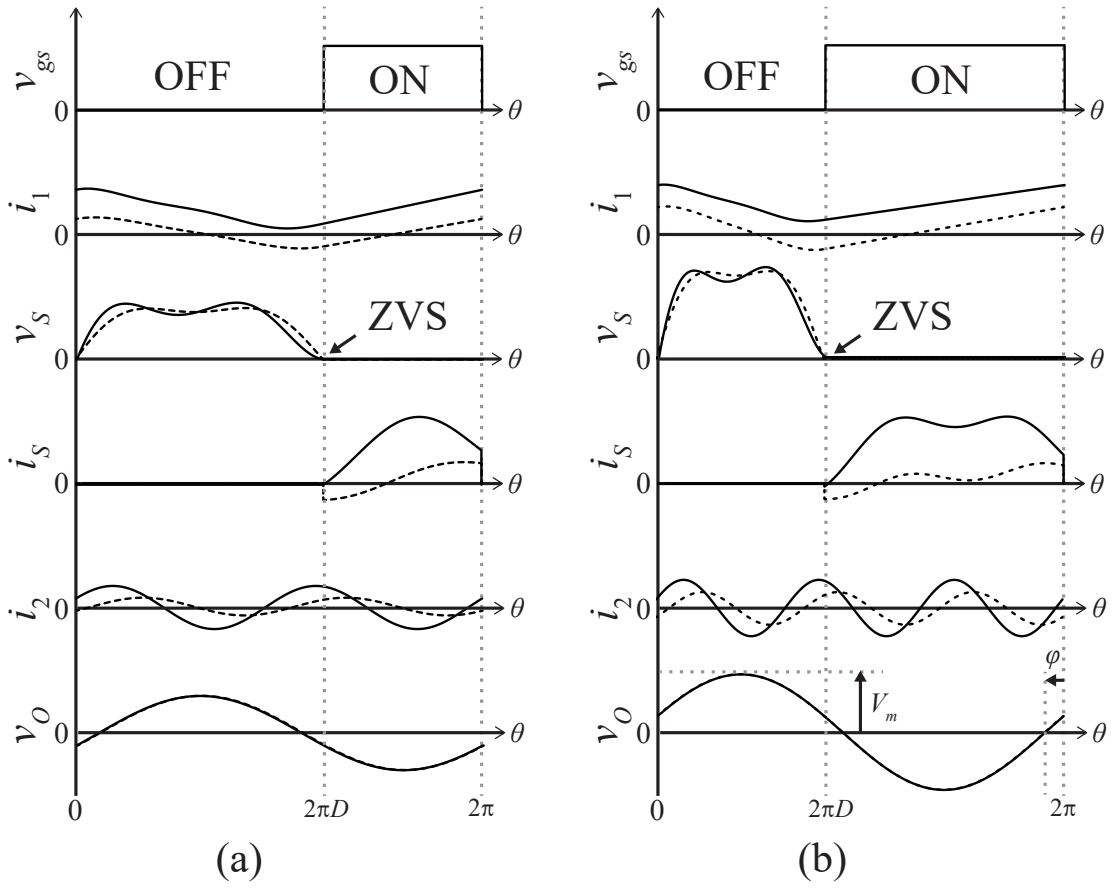


Fig. 4.2: Example waveforms for fixed load resistance (solid line:  $R_L/R_{Lr} = 1$ , dashed line:  $R_L/R_{Lr} = 10$ ). (a) Load-independent class- $\Phi_2$  inverter. (b) Load-independent class- $\Phi_3$  inverter.

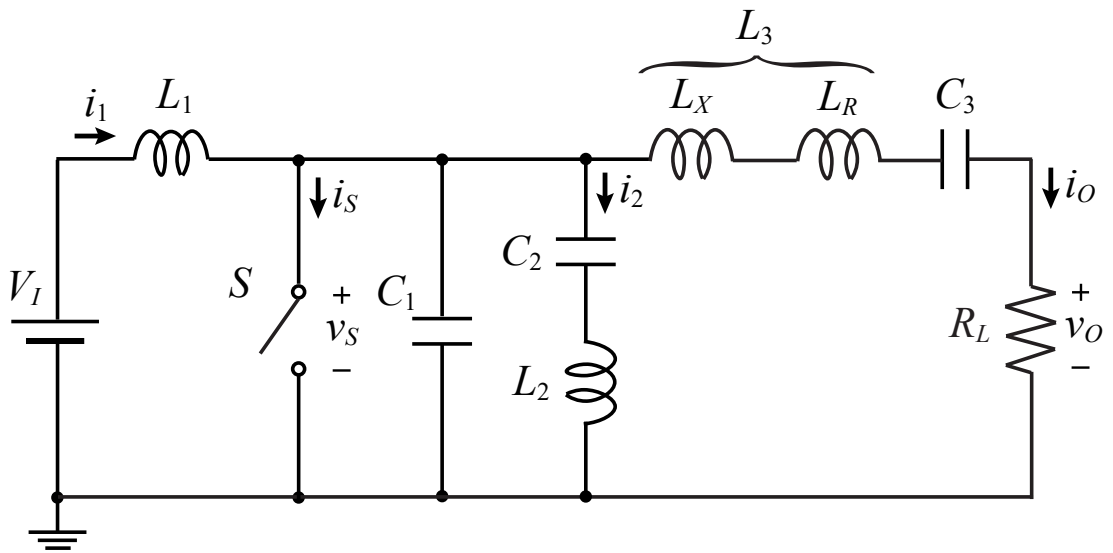
Fig. 4.3: Analytical circuit model of the class- $\Phi_3$  inverter.

Table 4.1: Analytical and experimental component values.

	Class- $\Phi_2$ inverter		Class- $\Phi_3$ inverter	
	Analytical	Measured	Analytical	Measured
$L_1$	532 nH	534 nH	834 nH	832 nH
$L_2$	1761 nH	1770 nH	1174 nH	1170 nH
$L_3$	2347 nH	2333 nH	2347 nH	2333 nH
$C_1$	535 pF	222 pF	222 pF	0 pF
$C_2$	78 pF	52 pF	52 pF	46 pF
$C_3$	239 pF	237 pF	237 pF	233 pF

Table 4.2: Components and devices used on the PCB.

	Parts number	Manufacturer
Switching device	GS61004B	GaN Systems
Load resistance	TEH100	Ohmite
Resonant capacitors	S111DUE	Johanson Technology
Magnetic core for $L_1$	T50-6	Micrometals
Magnetic core for $L_2$	T50-6	Micrometals
Magnetic core for $L_2$	T80-6	Micrometals

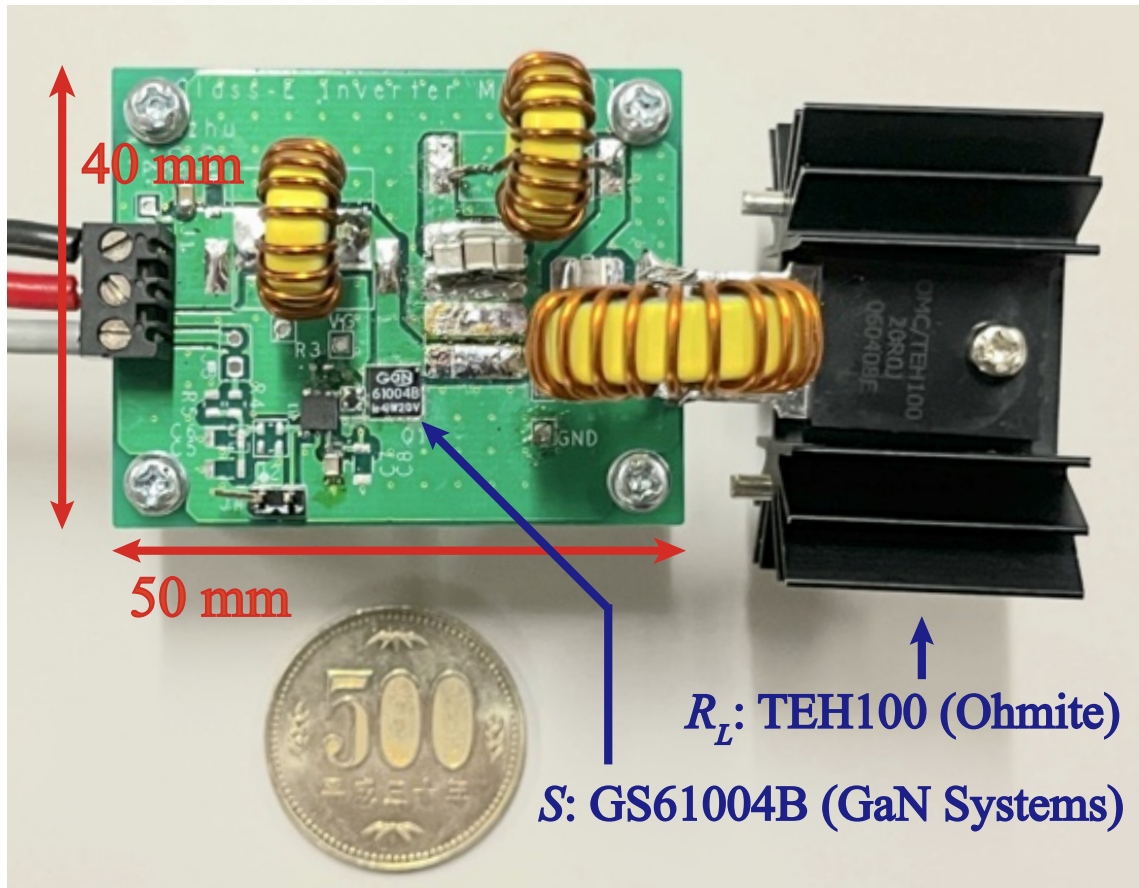


Fig. 4.4: Photo of the implemented load-independent class- $\Phi_3$  inverter.

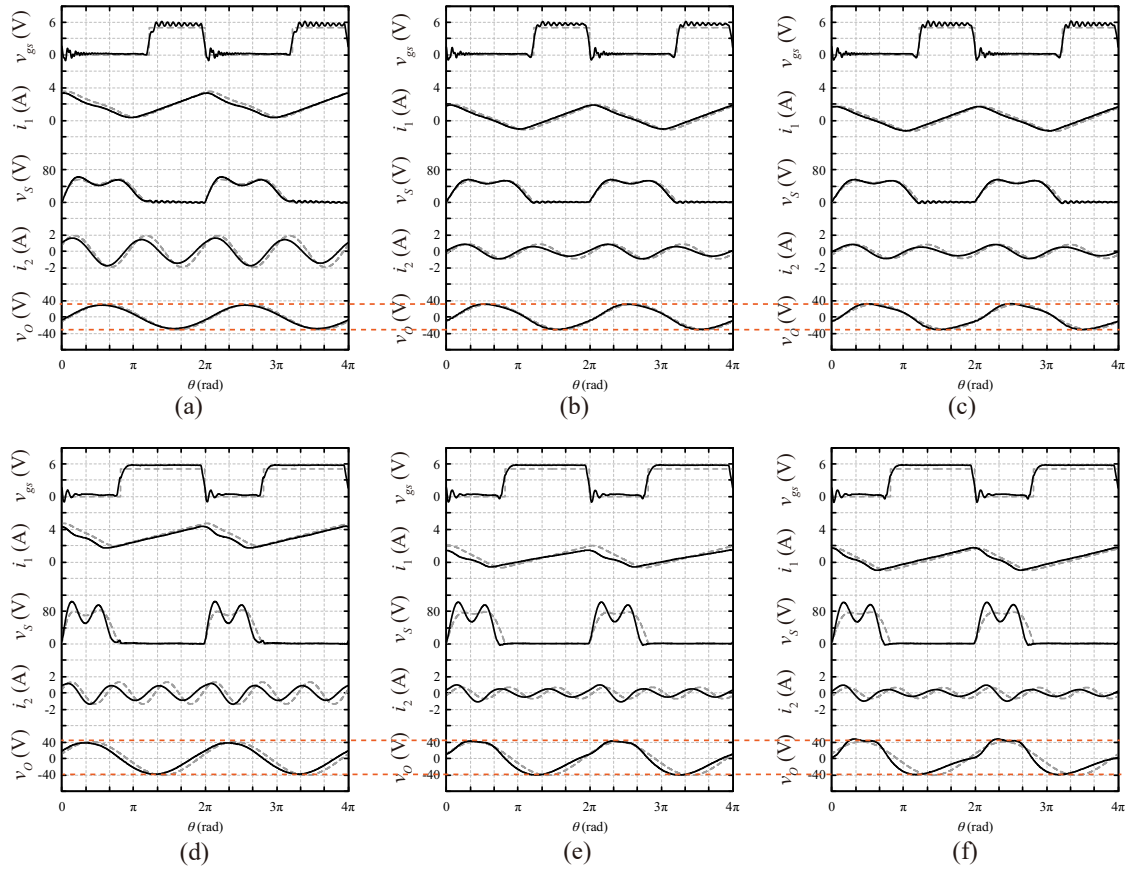


Fig. 4.5: Superimposed experimental and analytical waveforms for fixed load resistance (solid line: experiment, dashed line: analytical). (a)-(c) Load-independent class- $\Phi_2$  inverter. (d)-(f) Load-independent class- $\Phi_3$  inverter. (a) and (d) For  $R_L/R_{Lr} = 1$ . (b) and (e) For  $R_L/R_{Lr} = 5$ . (c) and (f) For  $R_L/R_{Lr} = 10$ .

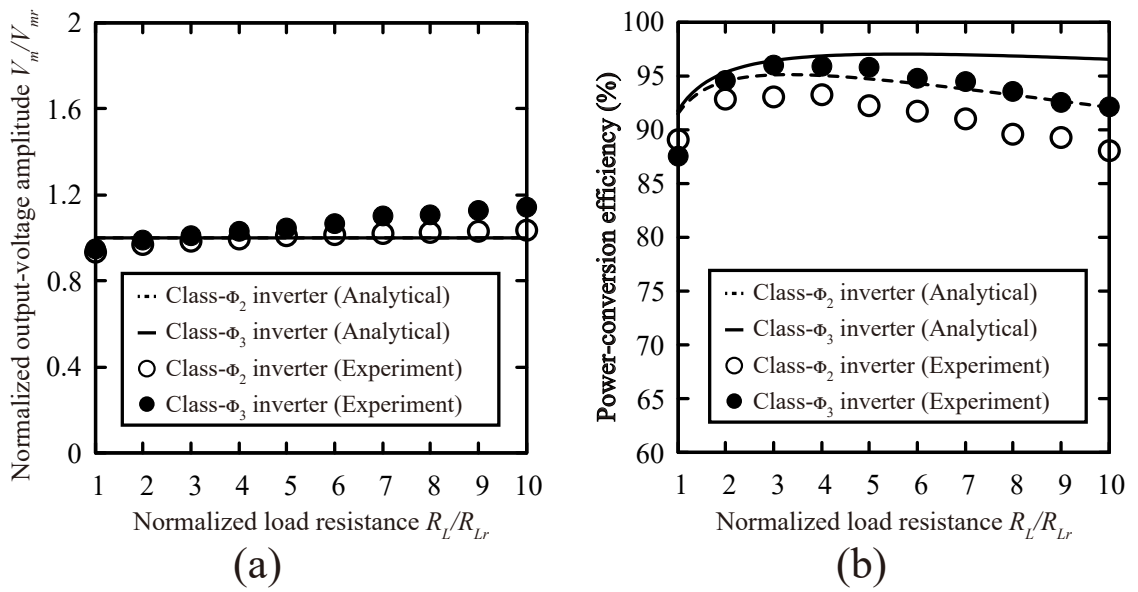


Fig. 4.6: Circuit characteristics as a function of normalized load resistance. (a) Normalized output-voltage amplitude. (b) Power-conversion efficiency.

Table 4.3: Comparison between the load-independent class- $\Phi_2$  and class- $\Phi_3$  inverters.

	Switch-voltage stress	Switch-current stress	Output-voltage amplitude	Power-output capability	Power-conversion efficiency
Load-independent class- $\Phi_2$ inverter	$2.27 V_I$	$2.94 R_{Lr}/V_I$	$1.24 V_I$	0.116	88.0%-93.2%
Load-independent class- $\Phi_3$ inverter	$3.31 V_I$	$2.95 R_{Lr}/V_I$	$1.63 V_I$	0.137	87.5%-95.9%

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## Chapter 5

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# Load-Independent Class-E<sup>-1</sup> Power Oscillator

The class-E inverter is used in an extensive range of applications, such as induction heatings [1], DC-DC converters [2], and WPT systems [3]. The class-E inverter has only one switch with a grounded source terminal, which allows high-frequency operation in the megahertz band. However, the class-E inverter is highly sensitive to component values [4, 5], which means that it cannot maintain high efficiency and constant output for variations, including component tolerances and load variations.

For obtaining the robustness against component tolerances in the resonant filter, the frequency-modulation control is applied to the class-E inverter [6]. The class-E inverter improves the efficiency against the component tolerances by tuning the operating frequency. However, it requires a digital control system, which increases the cost and complexity. The self-tuned oscillator [7] realizes the frequency tuning without external digital controls. The self-tuning feedback loop provides the gate-driving voltage with almost the constant phase shift, realizing the same function as the frequency-modulation control [6] without control. Although the self-tuned oscillator has solved the problem of resonant-component tolerances, it is still sensitive

to load-resistance variations.

The load-independent class-E inverter [8–11] is a simple solution for maintaining high efficiency and constant output against load-resistance variations without any control. The class-E inverter can acquire robustness to load-resistance variations by designing specific component values to satisfy the load-independent conditions [8–10]. For obtaining the robustness against both the resistive and reactance component variations in the resonant filter, the load-independent-designed self-tuned oscillator is proposed [12,13]. These oscillators provide constant gate-driving voltage against load variations, keeping the load-independent operation even with the component tolerances. Although the self-tuned load-independent oscillator is robust to both resistive and reactance component variations, there is no series-resonant-type oscillator that is suitable for the transmitter circuit of the WPT systems.

This chapter proposes the self-tuned series resonant power oscillator with load-independent operation. The proposed circuit is the first self-tuned load-independent oscillator with a series resonant filter. The proposed power oscillator is derived from the load-independent CC/ZCS inverter [10]. The proposed circuit achieves CC output and high efficiency against load-resistance variations and component tolerances by adding the self-tuned feedback network. The design method of the proposed oscillator is presented in this chapter. The experimental results show the effectiveness of the proposed power oscillator.

## 5.1 Load-Independent CC/ZCS inverter

Fig. 5.1 shows the circuit topology and operating waveforms of the load-independent CC/ZCS inverter [10] with duty ratio  $D = 0.5$ . The load-independent CC/ZCS inverter is composed of the voltage source  $V_I$ , choke coil  $L_C$ , switching device  $S$ , series inductance  $L_S$ , shunt capacitance  $C_S$ , and series resonant filter  $L_0 - C_0 - R_L$ . The load-independent CC/ZCS inverter achieves the ZCS and constant CC output regardless of the load resistance, as shown in Fig. 5.1(b), where  $\theta = \omega t = 2\pi ft$  is the angular displacement and  $f$  is the operating frequency, and the subscript 'r' in  $R_{Lr}$  indicates the rated value. For achieving the load-independent operation [8–11], the inverter must satisfy

$$\varphi = \pi - \pi D, \quad (5.1)$$

and

$$1 - \cos\left(\frac{2\pi D}{\omega\sqrt{L_S C_S}}\right) + \frac{\pi(1-D)}{\omega\sqrt{L_S C_S}} \sin\left(\frac{2\pi D}{\omega\sqrt{L_S C_S}}\right) = 0, \quad (5.2)$$

where  $\varphi$  is the phase shift between the output current and gate-drive voltage. Namely, the load-independent CC/ZCS inverter has a phase shift  $\varphi = \pi/2$  for  $D = 0.5$ , as shown in Fig. 5.1(b).

Although the load-independent CC/ZCS inverter has excellent robustness for load-resistance variations, it has a high sensitivity for component tolerances in the resonant filter due to a high-quality factor defined as  $Q = \omega L_0/R_L$ . Fig. 5.2(a) and (b) shows the switch-current waveforms of the load-independent CC/ZCS inverter against variations in resonant inductance for fixed load resistance. We can see that the non-ZCS waveforms appeared when  $L_0/L_{0r} = 0.9$ . Besides, the reverse cur-

rent increases for  $L_0/L_{0r} = 1.1$ , especially at light load. These deteriorations in switch-current waveform decrease the power-conversion efficiency.

## 5.2 Proposed oscillator

Fig. 5.3 shows the circuit topology and operating waveforms of the proposed oscillator. The proposed oscillator consists of the load-independent CC/ZCS inverter [10] with an additional self-tuned feedback network, as shown in Fig. 5.3(a). The feedback network is composed of a blocking capacitance  $C_B$  and voltage-dividing resistances  $R_{d1}$  and  $R_{d2}$  for generating the bias voltage of the switch  $V_{th}$ . In the load-independent CC/ZCS inverter, the voltage across the resonant capacitance  $v_{C2}$  is in the same phase as the gate-drive voltage because the output current has a phase shift of  $\varphi = \pi/2$  for  $D = 0.5$ . The proposed oscillator uses this property to produce the gate-driving voltage by feeding back the voltage across the resonant capacitance, as shown in Fig. 5.3(b).

Based on the proposed feedback network, the proposed oscillator autonomously tunes the operating frequency to the resonant one. The self-tuning can be realized because the phase shift of the feedback voltage is independent of the operating frequency. Therefore, the proposed oscillator has robustness against the component tolerances in the resonant filter. Moreover, self-tuning can be achieved even when load-resistance variations occur. This is because the phase shift of the feedback voltage is fixed for load-resistance variations due to the load-independent operation [8–11]. Namely, the proposed oscillator is robust to simultaneous variations in load resistance and component tolerances.

Fig. 5.2(c) and (d) show the example waveforms of the proposed oscillator against variations in resonant inductance for fixed load resistance. We can see that the non-ZCS waveforms in Fig. 5.2(a) and (b) are mitigated in Fig. 5.2(c) and (d) by the self-tuning. Also, the reverse current is suppressed in Fig. 5.2(c) and (d). The switch-current waveform of the proposed oscillator has small changes against  $L_0$  variations, resulting in stable circuit operation. Therefore, it can be said that the proposed oscillator overcomes the sensitivity problem in the component tolerances through the self-tuning feedback network.

### 5.3 Circuit design

In this chapter, we design the proposed oscillator from the given specification of input voltage  $V_I$ , rated load resistance  $R_{Lr}$ , operating frequency  $f$ , and quality factor  $Q$ . Firstly, the load-independent CC/ZCS inverter with  $D = 0.5$  is designed for the proposed oscillator. From [10], the component values are derived as

$$C_S = \frac{0.96424}{\omega R_{Lr}}, \quad (5.3)$$

$$L_S = \frac{0.62172R_{Lr}}{\omega}, \quad (5.4)$$

$$L_0 = \frac{QR_{Lr}}{\omega}, \quad (5.5)$$

and

$$C_0 = \frac{1}{\omega R_{Lr}(Q - 1.3132)}. \quad (5.6)$$

The amplitude of the output current  $I_m$  is

$$I_m = \frac{1.2133V_I}{R_{Lr}}. \quad (5.7)$$

Second, the component value in the feedback network is derived. The resistances  $R_{d1}$  and  $R_{d2}$  are used for producing the bias voltage for the switch. Namely, they satisfy

$$V_{th} = \frac{R_{d2}V_I}{R_{d1} + R_{d2}}. \quad (5.8)$$

Besides,  $R_{d1}$  and  $R_{d2}$  need to be large enough so that the current flowing through them can be ignored. Also,  $C_B$  should be large enough to block the DC. The capacitance  $C_1$  and  $C_2$  are divided to adjust the amplitude of the gate-driving voltage. By considering the maximum absolute of the gate-driving voltage  $V_{gsmax}$ ,  $C_2$  and  $C_1$  are designed as

$$C_2 \geq \frac{I_m}{\omega(V_{gsmax} - V_{th})}, \quad (5.9)$$

and

$$C_1 = \frac{C_0 C_2}{C_2 - C_0}. \quad (5.10)$$

## 5.4 Experimental verifications

The design specifications of the proposed oscillator were given as  $V_I = 30$  V,  $R_{Lr} = 50$   $\Omega$ ,  $f = 1$  MHz, and  $Q = 5$ . We chose the GS66504B from GaN Systems as the switching device, whose threshold voltage  $V_{th} = 1.7$  V and ON resistance  $r_{ON} = 0.16$   $\Omega$ . The powder iron core T106-2 and T200-2 from Micrometals were used

for series inductance  $L_S$  and resonant inductance  $L_0$ , whose ESR were  $r_{L_S} = 0.118 \Omega$  and  $r_{L_0} = 0.306 \Omega$ , respectively. Also, the shielded power inductor MSS1210H from Coilcraft was used as the choke coil  $L_C$ . Table 7.1 shows the component values of the implemented oscillator. Fig. 5.4 shows the photo of the experimental prototype. In this chapter, we also conducted the experiment for the load-independent CC/ZCS inverter with the same specifications for comparison.

Fig. 5.5 shows the experimental waveforms of the load-independent CC/ZCS inverter against load-resistance variations for fixed resonant inductance. We can see from Fig. 5.5(b) that the switch current achieved ZCS and the output-current amplitude was constant against load-resistance variations. However, the non-ZCS waveforms appeared in Fig. 5.5(a), and the reverse current increased in Fig. 5.5(c). We can state that the load-independent CC/ZCS inverter has high sensitivity against  $L_0$  variations.

Fig. 5.6 shows the analytical and experimental waveforms of the proposed oscillator against load-resistance variations for fixed resonant inductance. The analytical waveforms are derived based on the circuit analysis in [8]. We can see from Fig. 5.6(b) and (e) that the load-independent ZCS and CC output were achieved for the rated resonant inductance. Moreover, we can see from Fig. 5.6(a) and (d) that the ZCS was achieved even with the  $L_0$  variations. Besides, the reverse current in Fig. 5.5(c) was suppressed in Fig. 5.6(c) and (f). The measured operating frequency in the rated load was  $f = 1.003$  MHz at  $L_0/L_{0r} = 1$ ,  $f = 1.052$  MHz at  $L_0/L_{0r} = 0.9$ , and  $f = 0.9708$  MHz at  $L_0/L_{0r} = 1.1$ . Thus, we can say that the self-tuning worked well in the proposed oscillator, improving the characteristics against component tolerances in the resonant filter. The agreement of the analytical

and experimental waveforms showed the validity of the proposed design method.

Fig. 7.5 shows the normalized output-current amplitude and the power-conversion efficiency as a function of the load resistance. The analytical efficiency is calculated by using the power-loss analysis in [14]. We consider the power loss, including the ESRs of  $L_C$ ,  $L_S$  and  $L_0$ , switch ON-resistance, and switching loss caused by the non-ZCS. We can see from Fig. 7.5(b) that the flat characteristics of the output-current amplitude and high efficiency against load-resistance variations were obtained in both the load-independent CC/ZCS inverter and the proposed oscillator. In addition, we can see from Fig. 7.5(a) and (c) that the proposed oscillator kept high efficiency even with the deviations in  $L_0$ , especially at light load compared with the load-independent CC/ZCS inverter. We can conclude that the proposed oscillator has excellent load characteristics even with the variations in the resonant component, showing the effectiveness of the proposed topology. The proposed oscillator achieved 95.0 % efficiency with 12 W output power in 1MHz operation.

## 5.5 Conclusion

This chapter has proposed the self-tuned series resonant power oscillator with load-independent operation. The proposed oscillator maintains high efficiency and constant AC output even with load variations and component tolerances. The experimental results show the effectiveness of the proposed power oscillator.

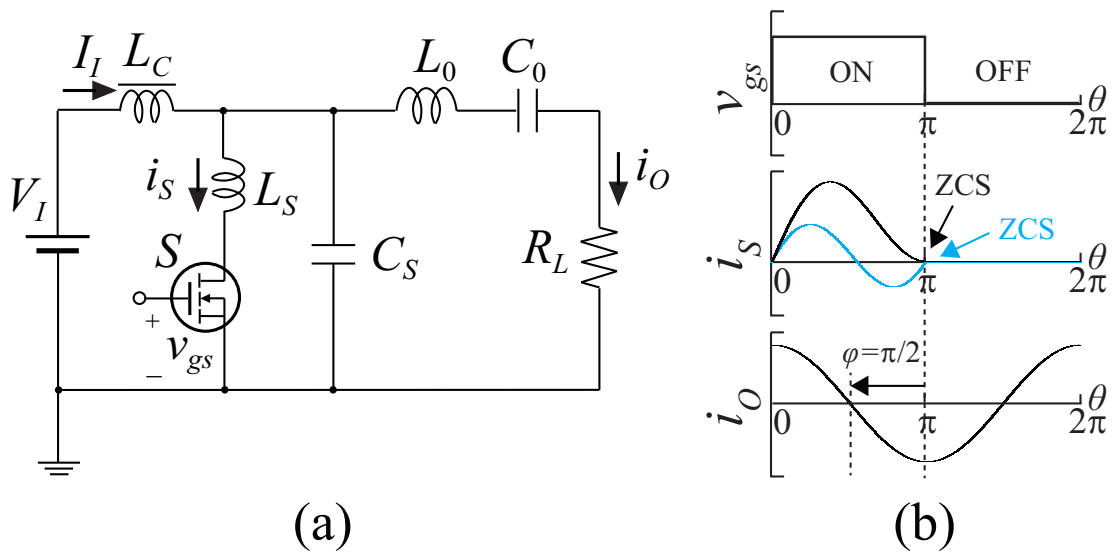


Fig. 5.1: The load-independent CC/ZCS inverter. (a) Circuit topology. (b) Operating waveforms. (Black line:  $R_L/R_{Lr} = 1$  and blue line:  $R_L/R_{Lr} = 0.1$ .)

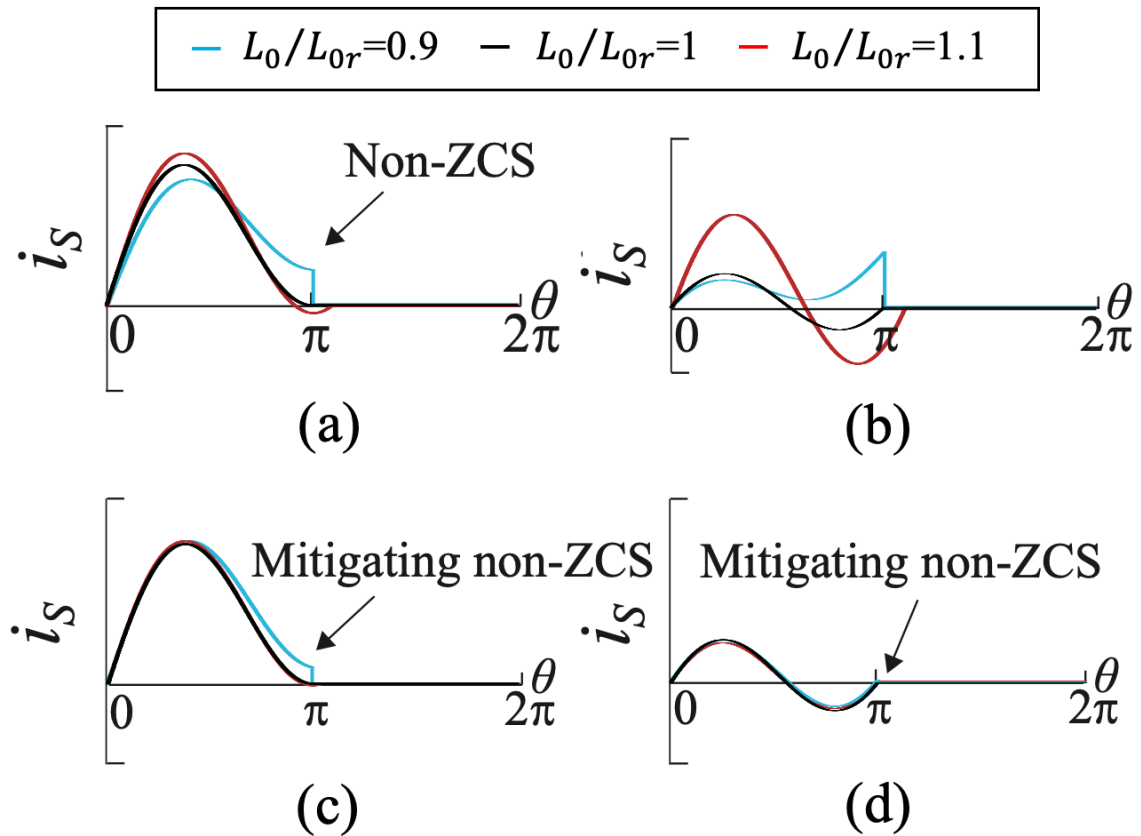


Fig. 5.2: The switch-current waveforms against variations in resonant inductance for fixed load resistance. (a) For load-independent CC/ZCS inverter at  $R_L/R_{Lr} = 1$ . (b) For load-independent CC/ZCS inverter at  $R_L/R_{Lr} = 0.1$ . (c) For proposed oscillator at  $R_L/R_{Lr} = 1$ . (d) For proposed oscillator at  $R_L/R_{Lr} = 0.1$ .

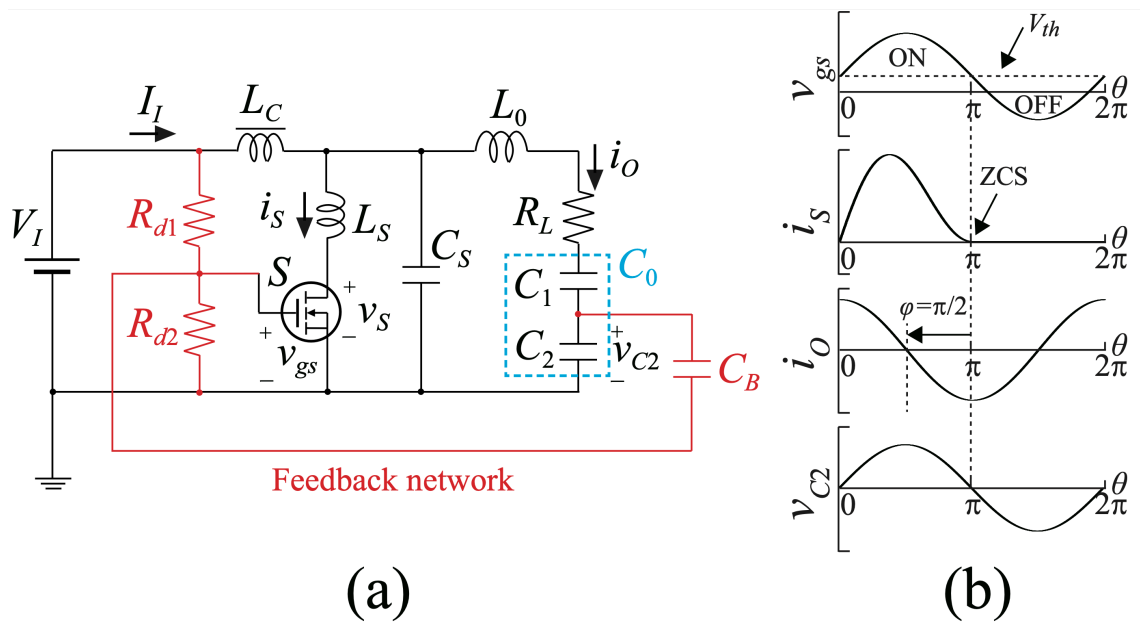


Fig. 5.3: The proposed oscillator. (a) Circuit topology. (b) Operating waveforms.

Table 5.1: Analytical and measured component values.

	Analytical	Measured		Analytical	Measured
$L_C$	-	154.0 $\mu\text{H}$	$C_S$	3069 pF	3066 pF
$L_S$	4.947 $\mu\text{H}$	4.994 $\mu\text{H}$	$C_B$	-	1.014 $\mu\text{F}$
$L_0$	39.79 $\mu\text{H}$	39.89 $\mu\text{H}$	$R_{d1}$	10.00 k $\Omega$	10.12 k $\Omega$
$C_1$	886.5 pF	886.6 pF	$R_{d2}$	166.5 k $\Omega$	160.0 k $\Omega$
$C_2$	33.04 nF	36.04 nF	$R_{Lr}$	50.00 $\Omega$	50.10 $\Omega$

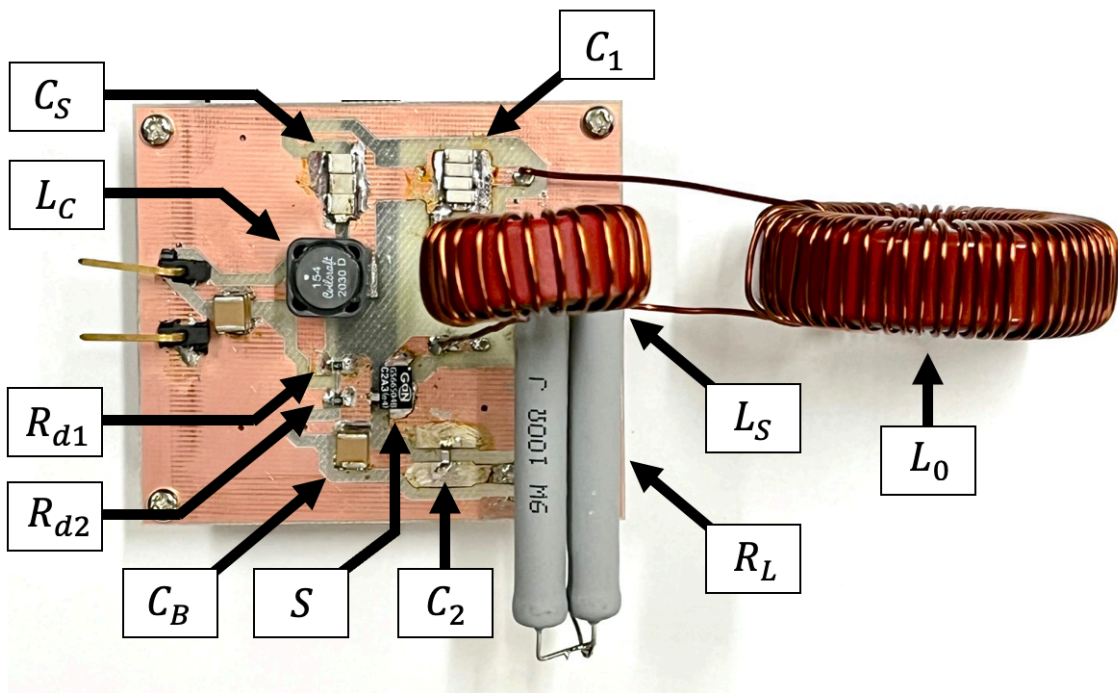


Fig. 5.4: Photo of the implemented proposed oscillator.

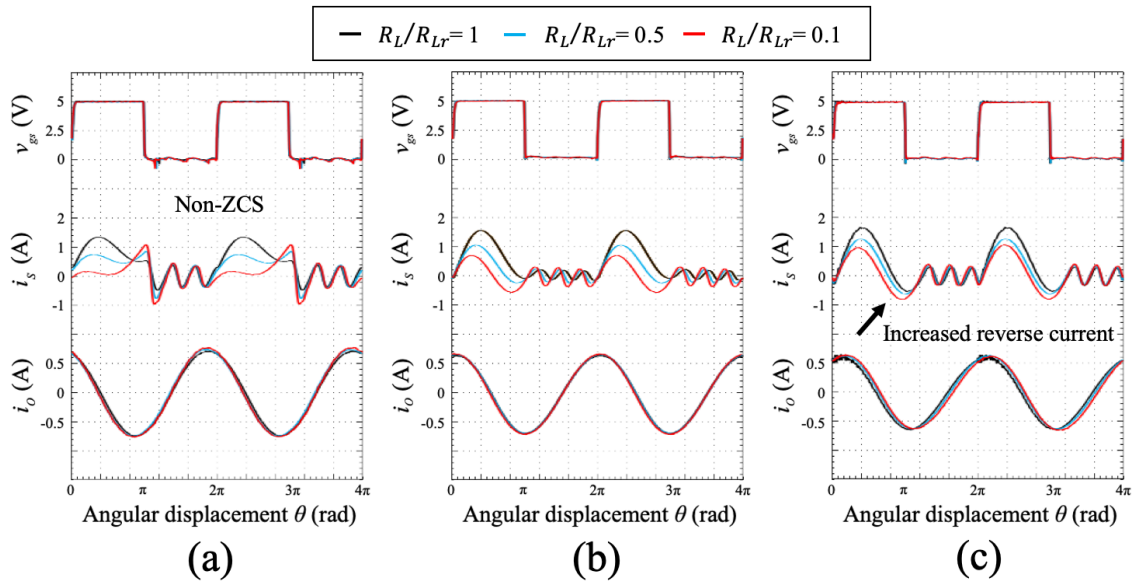


Fig. 5.5: The experimental waveforms of the load-independent CC/ZCS inverter against load-resistance variations for fixed resonant inductance. (a) For  $L_0/L_{0r} = 0.9$ . (b) For  $L_0/L_{0r} = 1$ . (c) For  $L_0/L_{0r} = 1.1$ .

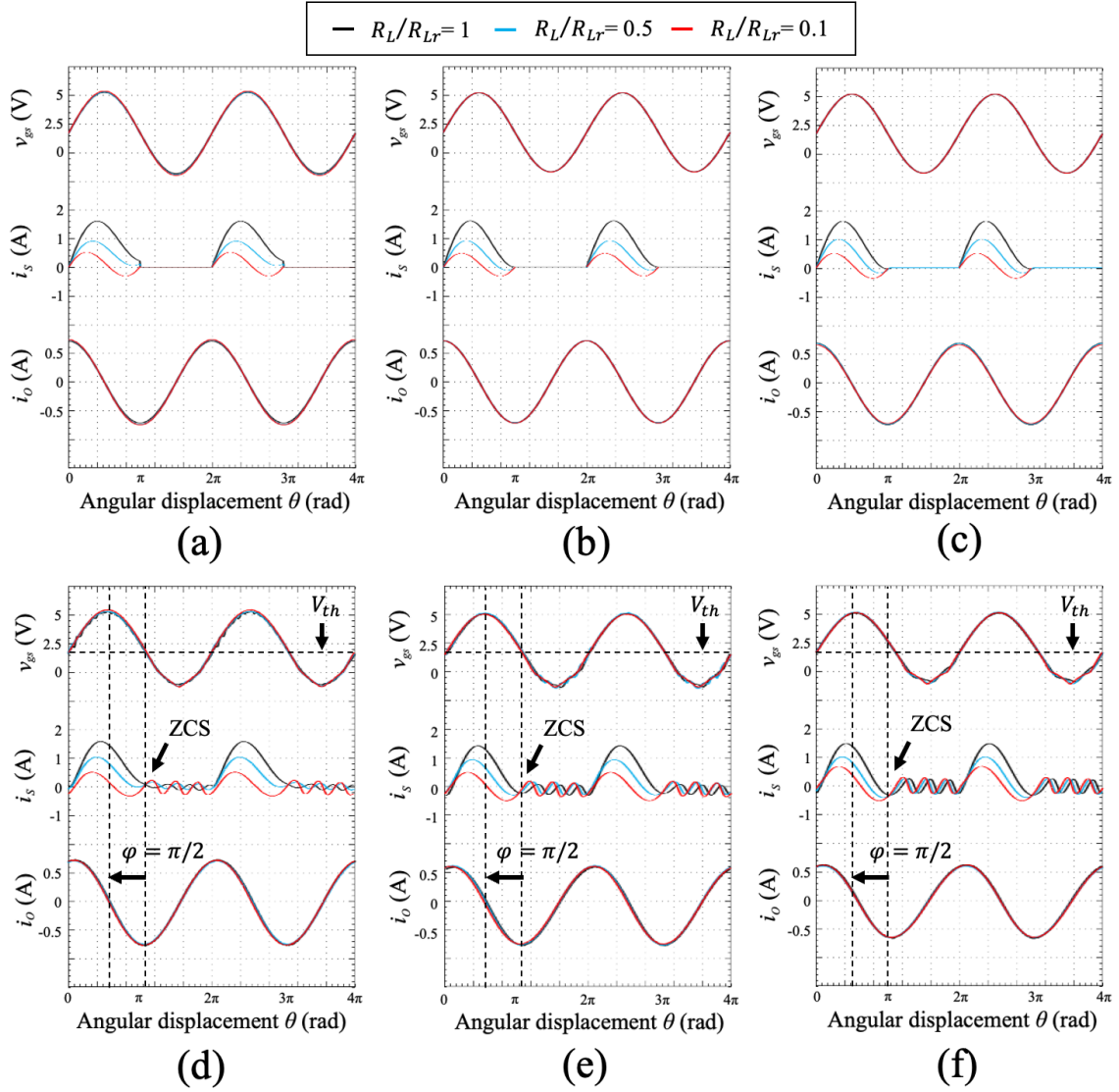


Fig. 5.6: The waveforms of the proposed oscillator against load-resistance variations for fixed resonant inductance. (a) Analytical waveforms for  $L_0/L_{0r} = 0.9$ . (b) Analytical waveforms for  $L_0/L_{0r} = 1$ . (c) Analytical waveforms for  $L_0/L_{0r} = 1.1$ . (d) Experimental waveforms for  $L_0/L_{0r} = 0.9$ . (e) Experimental waveforms for  $L_0/L_{0r} = 1$ . (f) Experimental waveforms for  $L_0/L_{0r} = 1.1$ .

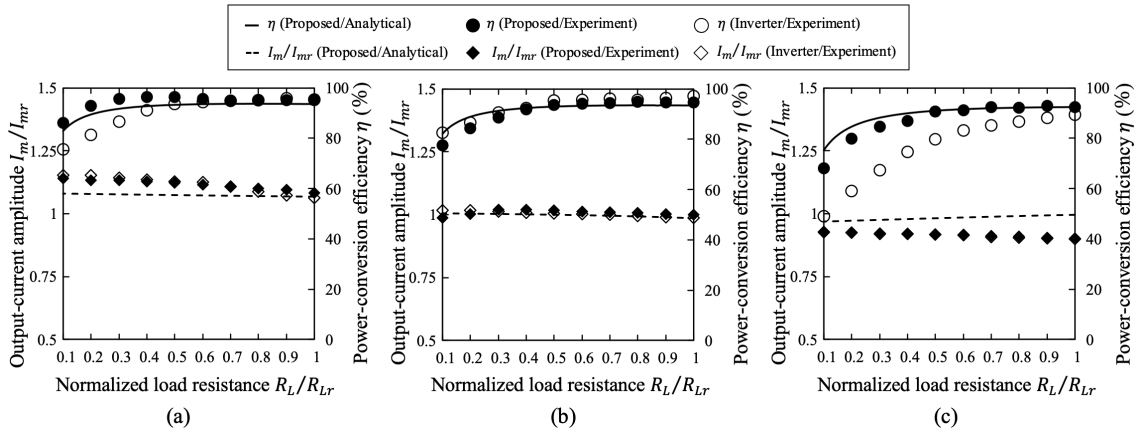


Fig. 5.7: The normalized output-current amplitude and the power-conversion efficiency as a function of the load resistance. (a) For  $L_0/L_{0r} = 0.9$ . (b) For  $L_0/L_{0r} = 1$ . (c) For  $L_0/L_{0r} = 1.1$ .

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## Chapter 6

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# Load-Independent Class-E Power Oscillator

### 6.1 Introduction

The development of wide-bandgap power semiconductor devices, such as GaN and SiC, have accelerated developments of high-frequency inverters [1]. The passive components require less energy storage in high-frequency operation, allowing for physical size and weight reduction. Accordingly, high-frequency inverters increase the power density of the overall circuit. However, the higher frequency causes larger switching losses, which impose the requirement for achieving ZVS. Additionally, in practical applications, such as WPT systems and DC/DC converters, the load variations should be considered in the design [2, 3].

Within the above context, the load-independent class-E inverter [4] has attracted attention. The load-independent class-E inverter inherently achieves the ZVS and constant amplitude of the output voltage against resistive load variations. Therefore, no additional circuits and controls are required to maintain the ZVS and output regulation, simplifying the overall circuit configuration. The load-independent oper-

ation can be attained using a specific set of component values. The design conditions to achieve the load-independent operation are analytically revealed [5], which enables implementation of the load-independent class-E inverter for a wide range of applications and specifications [6–8].

The class-E power oscillator [9–13] is a variant of the class-E inverter, which autonomously oscillates by adding a passive feedback network. The class-E power oscillator generates the gate-drive voltage using the output AC voltage. Therefore, the feedback network needs to compensate for the phase shift between the output and gate-drive voltages. The class-E power oscillator works without the gate-drive circuits, including a crystal oscillator, gate driver, and additional power supplies, which further promotes circuit simplification and cost reduction. Although the class-E power oscillator achieves high efficiency due to the ZVS at the nominal state, its performance seriously degrades against load variations [11]. The load variations affect overall circuit operation, including efficiency deterioration due to the non-ZVS, fluctuations in output voltage and current, and, to make matters worse, the oscillation stops. Various types of the power oscillators, such as class-E [9–13] and class-E/F [14, 15] power oscillators, have been proposed so far. Nevertheless, all these power oscillators achieve optimal performance only within an extremely narrow range of load variations. Addressing load variations is a critical issue for making power oscillators more practical, which motivates enhancing the robustness of the class-E power oscillator.

This chapter proposes the load-independent class-E power oscillator. The load-independent class-E inverter is incorporated into the power oscillator by introducing the feedback network using the LCCL filter. The LCCL filter compensates for the

phase shift between the output and gate-drive voltages of the load-independent class-E inverter. Furthermore, the input impedance of the LCCL filter becomes purely resistive, which does not interfere with the load-independent operation of the inverter. Consequently, the proposed power oscillator obtains load independence in ZVS, output current, and gate-drive voltage. The proposed circuit works with high stability and efficiency over a wide load range, overcoming the sensitivity issue against load variations in the power oscillator. An analytical investigation of the proposed power oscillator is provided to reveal design conditions for achieving the load-independent operation. This chapter also gives closed-form design equations of the load-independent class-E power oscillator. The experimental verifications were carried out at 6.78 MHz oscillation frequency. The measured waveforms were quantitatively agreed with the analytical one, confirming the validity of the experiment.

## 6.2 Conventional Class-E Power Oscillator

Fig. 6.1 shows the circuit topology of the class-E power oscillator, which consists of the class-E inverter and the feedback network. The class-E power oscillator forms a closed loop with the passive components, and an external oscillator is unnecessary to drive the switch.

Fig. 6.2 shows the example waveforms of the class-E power oscillator, where  $\theta = \omega_S t = 2\pi f_S t$  is the angular time,  $\omega_S$  denotes the angular oscillation frequency, and  $f_S$  represents oscillation frequency. The switch is driven by the excitation of the biased sinusoidal voltage  $v_{gs}$ , which is generated using the output AC voltage  $v_O$ . To induce the sustained oscillation, the total phase shift in the closed loop must be an integer

multiple of  $2\pi$ . Meanwhile, the nominal phase shift of the output voltage is  $0.82\pi$  in the class-E inverter [16]. Therefore, the feedback network  $C_3$ - $C_4$ - $L_3$  provides an additional phase shift, compensating the phase shift between the output and the gate-drive voltages. Additionally, the class-E power oscillator features to achieve the ZVS at the nominal state, which contributes to high-efficiency operation.

However, when load variations occur, the class-E power oscillator is unable to maintain the ZVS, and both the output voltage and current fluctuate. The high sensitivity to load variations is attributable to the class-E inverter. The class-E inverter not only causes non-ZVS against load variations but also experiences changes in the phase shift of the output voltage [17]. Consequently, the phase-shift requirement for the oscillation cannot be satisfied, changing the frequency to forcibly induce the oscillation. Therefore, even minor load variations can seriously affect the overall performance of the power oscillator.

### 6.3 Load-Independent Class-E Power Oscillator

To address the sensitivity of the power oscillator to load variations, the robustness of the inverter should be ensured. Accordingly, this chapter focuses on the load-independent class-E inverter [4]. The load-independent class-E inverter achieves the ZVS regardless of the load resistance without changing the circuit topology from the original class-E inverter. Moreover, another critical aspect is to provide a fixed phase shift in the output voltage against load variations. We found these features are highly suitable for power oscillators. However, the load-independent class-E inverter has a  $\pi$  phase shift between the output and the gate-drive voltages,

which cannot be compensated using the feedback network in the conventional class-E power oscillator. Therefore, the topological change is necessary to incorporate the load-independent class-E inverter into the power oscillator.

Fig. 6.3 shows the circuit topology of the proposed load-independent class-E power oscillator. The proposed power oscillator is composed of input DC-voltage source  $V_I$ , switching device  $S$ , finite inductor  $L_1$ , shunt capacitor  $C_1$ , LCCL filter  $L_2$ - $C_2$ - $C_3$ - $L_3$ , load resistance  $R_L$ , DC-blocking capacitor  $C_4$ , and voltage-divide resistances  $R_1$  and  $R_2$ . The capacitor  $C_3$  is divided into  $C_{31}$  and  $C_{32}$  to adjust the amplitude of the gate-drive voltage.

This chapter introduces an LCCL filter to provide an additional phase shift to the load-independent class-E inverter. Fig. 6.4 shows typical waveforms of the proposed power oscillator. The LCCL filter provides a  $\pi/2$  phase shift between the currents  $i_2$  and  $i_O$  under a specific resonant condition. Also, the phase shift of the voltage across the capacitor  $C_{32}$  leads  $\pi/2$  against the output current  $i_O$ . Consequently, the voltage  $v_{32}$  becomes in phase with the gate-drive voltage, satisfying the phase-shift condition necessary for the oscillation. Most notably, these phase shifts are fixed and independent of the load resistance. Besides, the input impedance of the LCCL filter becomes purely resistive in this particular resonant condition, which does not interfere with the load-independent operation of the inverter. Therefore, the proposed power oscillator successfully incorporates the load-independent operation in the power oscillator.

The proposed power oscillator exhibits the load-independent characteristics in ZVS, output current, and gate-drive voltage. Although the load-independent class-E inverter exhibits constant voltage gain against load variations, the proposed power

oscillator has a constant current gain due to the additional LCCL filter. The constant current characteristic makes the amplitude of the voltage  $v_{32}$  also constant. As a result, the amplitude of the gate-drive voltage becomes independent of the load resistance, which further improves the stability of the oscillation.

## 6.4 Circuit Analysis

This section provides the circuit analysis for the load-independent class-E power oscillator. The analysis gives design conditions, waveform equations, and an optimal design point. To perform the analysis for the proposed power oscillator, we put the following assumptions for simplification.

- (i) The resistances  $R_1$  and  $R_2$  are large enough so that these components are regarded not to conduct current. Also, they divide the input voltage to produce a bias voltage, which is equal to the threshold voltage of the switching device  $V_{th}$ . Namely,

$$V_{th} = \frac{R_1}{R_1 + R_2} V_I. \quad (6.1)$$

- (ii) The capacitor  $C_4$  works as a DC blocking and is large enough to be regarded as a DC-voltage source  $V_{th}$ .
- (iii) The LCCL filter only passes fundamental frequency current, and the output current can be expressed as purely sinusoid as

$$i_O(\theta) = I_O \cos \theta, \quad (6.2)$$

where  $I_O$  is the amplitude of the output current.

- (iv) The inductor  $L_2$  is divided into an extra-inductive component  $L_X$  and a resonant component  $L_R$ .
- (v) The switching device functions as an ideal switch, turning OFF when  $V_{th} > v_{gs}(\theta)$  and turning ON when  $V_{th} \leq v_{gs}(\theta)$ . Additionally, it possesses zero ON-resistance, zero gate resistance, and infinite OFF-resistance.
- (vi) The drain-source and gate parasitic capacitances of the switching device are absorbed into  $C_1$  and  $C_{32}$ , respectively.
- (vii) All the passive components operate linearly without parasitic components.

From the assumptions above, the equivalent circuit model of the proposed power oscillator is derived as shown in Fig. 6.5.

#### 6.4.1 LCCL filter

From the assumption (iii), the voltage across capacitor  $C_{32}$  can be expressed as

$$v_{32}(\theta) = -\frac{I_O}{\omega C_{32}} \sin \theta, \quad (6.3)$$

Accordingly, the gate-drive voltage  $v_{gs}$  can be obtained as

$$v_{gs}(\theta) = -\frac{I_O}{\omega C_{32}} \sin \theta + V_{th}. \quad (6.4)$$

The input impedance of the LCCL filter is obtained as

$$Z_{eq} = \frac{R_L}{\omega^2 C_2^2 (R_L^2 + H_2^2)} + j \left[ H_1 - \frac{H_2}{\omega^2 C_2^2 (R_L^2 + H_2^2)} \right], \quad (6.5)$$

where  $H_1$  and  $H_2$  are defined as

$$H_1 = \omega L_R - \frac{1}{\omega C_2}, \quad (6.6)$$

and

$$H_2 = \omega L_3 - \frac{1}{\omega C_2} - \frac{1}{\omega C_3}, \quad (6.7)$$

respectively.

For ensuring the load-independent operation, the input impedance of the LCCL filter is designed to be purely resistive. Namely, the resonant conditions should be  $H_1 = H_2 = 0$ , which determines the angular oscillation frequency  $\omega_S$  as

$$\omega_S = 2\pi f_S = \frac{1}{\sqrt{L_R C_2}} = \sqrt{\frac{1}{L_3} \left( \frac{1}{C_2} + \frac{1}{C_3} \right)}. \quad (6.8)$$

When (6.8) is satisfied, the input impedance in (6.5) becomes

$$Z_{eq} = R_{eq} = \frac{1}{\omega_S^2 C_2^2 R_L}. \quad (6.9)$$

We can see from (6.6)-(6.8) that the resonant conditions hold regardless of the load resistance  $R_L$ . Therefore, (6.9) indicates that the variations of load resistance can be seen as resistive variations for the class-E inverter.

The voltage gain  $G_f$  and phase shift  $\varphi_f$  between  $v_{eq}$  and  $v_O$  can be obtained as

$$G_f = \frac{V_O}{V_{eq}} = \sqrt{\frac{\omega^2 C_2^2 R_L (R_L^2 + H_2^2)}{\sqrt{R_L^2 + [\omega^2 C_2^2 (R_L^2 + H_2^2) H_1 - H_2]^2}}}, \quad (6.10)$$

and

$$\varphi_f = \begin{cases} \arctan \left( \frac{1}{\omega^2 C_1^2 R_L H_1} - \frac{H_2}{R_L} \right) & \text{for } H_1 < 0, \\ -\pi + \arctan \left( \frac{1}{\omega^2 C_1^2 R_L H_1} - \frac{H_2}{R_L} \right) & \text{for } H_1 \geq 0, \end{cases} \quad (6.11)$$

respectively, where  $V_{eq}$  and  $V_O$  are the amplitudes of the input and output voltages of the LCCL filter. From (6.10) and (6.11), the voltage gain and phase shift under

the resonant condition in (6.8) are derived as

$$G_f = \omega_S C_2 R_L = \frac{R_L}{\omega_S L_R}, \quad (6.12)$$

and

$$\varphi_f = -\frac{\pi}{2}, \quad (6.13)$$

respectively.

## 6.4.2 Equivalent Class-E Inverter

The voltage across the equivalent resistance  $R_{eq}$  is derived from (6.2), (6.12), and (6.13) as

$$v_{eq}(\theta) = V_{eq} \sin \theta = \omega_S L_R I_O \sin \theta. \quad (6.14)$$

Additionally, from (6.4) and the assumption (v), the switch turns OFF during  $0 \leq \theta < \pi$  and turns ON during  $\pi \leq \theta < 2\pi$ .

### 6.4.2.1 Waveform Equations

During the turn-OFF state, the differential equation for the switch voltage  $v_S$  is obtained from Kirchhoff's Voltage Law (KVL) as

$$\frac{d^2 v_S(\theta)}{d\theta^2} + \omega_1^2 v_S(\theta) = \omega_1^2 \left( V_I - \frac{\omega_S L_1 V_{eq} \cos \theta}{R_{eq}} \right), \quad (6.15)$$

where the normalized resonant frequency  $\omega_1$  is defined as

$$\omega_1 = \frac{1}{\omega_S \sqrt{L_1 C_1}}. \quad (6.16)$$

The solution to (6.15) yields the expression for the switch voltage in the turn-OFF period as

$$v_S(\theta) = \alpha \cos(\omega_1\theta) + \beta \sin(\omega_1\theta) + V_I - \frac{\omega_S L_1 \omega_1^2 V_{eq} \cos \theta}{R_{eq}(\omega_1^2 - 1)}, \quad (6.17)$$

where  $\alpha$  and  $\beta$  are constants.

From KVL, we obtain

$$\frac{di_1(\theta)}{d\theta} = \frac{1}{\omega_S L_1} [V_I - v_S(\theta)]. \quad (6.18)$$

By substituting (6.17) into (6.18) and solving the differential equation, we obtain the expression of current  $i_1$  during turn-OFF period as

$$i_1(\theta) = -\frac{\omega_1[\alpha \sin(\omega_1\theta) - \beta \cos(\omega_1\theta)]}{\omega_S L_1} + \frac{\omega_1^2 V_{eq} \sin \theta}{R_{eq}(\omega_1^2 - 1)} \quad (6.19)$$

During the turn-ON state, the switch is shorted out, making the switch voltage to be zero as

$$v_S(\theta) = 0. \quad (6.20)$$

From KVL, we obtain

$$\frac{di_1(\theta)}{d\theta} = \frac{V_I}{\omega_S L_1}. \quad (6.21)$$

By solving (6.21), we obtain

$$i_1(\theta) = \frac{V_I}{\omega_S L_1} \theta + \gamma, \quad (6.22)$$

where  $\gamma$  is a constant.

### 6.4.2.2 Boundary Condition

By considering the continuity of the current  $i_1$ , the boundary condition can be formulated as

$$i_1(\pi^-) = i_1(\pi^+). \quad (6.23)$$

From (6.19), (6.22), and (6.23), the unknown constant  $\gamma$  can be obtained, and the expression of  $i_1$  during turn-ON period becomes

$$i_1(\theta) = \frac{V_I(\theta - \pi) - \omega_1[\alpha \sin(\pi\omega_1) - \beta \cos(\pi\omega_1)]}{\omega_S L_1}, \quad (6.24)$$

The unknown constants  $\alpha$  and  $\beta$  can also be obtained from the boundary conditions of

$$i_1(0) = i_1(2\pi), \quad (6.25)$$

and

$$\left. \frac{di_1(\theta)}{d\theta} \right|_{\theta=0} = \left. \frac{di_1(\theta)}{d\theta} \right|_{\theta=2\pi}. \quad (6.26)$$

From (6.19) and (6.24)-(6.26), we obtain

$$\alpha = \frac{1}{\omega_S C_1} \left[ \frac{V_{eq}}{R_{eq}(\omega_1^2 - 1)} - \frac{V_I}{\omega_S L_1 \omega_1^2} \right], \quad (6.27)$$

and

$$\beta = \frac{\pi\omega_1 V_I - \left[ \frac{\omega_1^2 \omega_S L_1 V_{eq}}{R_{eq}(\omega_1^2 - 1)} - V_I \right] \sin(\pi\omega_1)}{1 - \cos(\pi\omega_1)}, \quad (6.28)$$

### 6.4.2.3 Design Condition

As the band-pass filter only passes the fundamental frequency component, the amplitude of the voltage across the equivalent resistance  $R_{eq}$  and the extra inductance  $L_X$  can be obtained from the first harmonic term of the Fourier Series Expansion as

$$V_{eq} = \frac{1}{\pi} \int_0^{2\pi} v_S(\theta) \sin \theta d\theta, \quad (6.29)$$

and

$$\frac{\omega_S L_X V_{eq}}{R_{eq}} = \frac{1}{\pi} \int_0^{2\pi} v_S(\theta) \cos \theta d\theta, \quad (6.30)$$

respectively.

We impose the switch voltage to achieve the turn-ON ZVS, which can be formulated as

$$v_S(\pi) = 0. \quad (6.31)$$

From (6.17), (6.27), (6.28), and (6.31), the design condition can be obtained as

$$\tan\left(\frac{\pi\omega_1}{2}\right) + \frac{\pi\omega_1}{2} = 0, \quad (6.32)$$

which can be numerically solved as

$$\omega_1 \approx 1.292. \quad (6.33)$$

From (6.17), (6.20), and (6.27)-(6.29), the amplitude of the voltage across the equivalent resistance  $R_{eq}$  becomes

$$V_{eq} = \frac{\omega_1^3 V_I}{(1 - \omega_1^2) \tan\left(\frac{\pi\omega_1}{2}\right)} \approx 1.590 V_I. \quad (6.34)$$

We can see from (6.34) that the amplitude of the voltage  $v_{eq}$  is independent of the load resistance. Accordingly, from (6.14), the amplitude of the output current can be derived as

$$I_O = \frac{\omega_1^3 V_I}{\omega_S L_1 (1 - \omega_1^2) \tan\left(\frac{\pi\omega_1}{2}\right)} \approx \frac{1.590 V_I}{\omega_S L_1}. \quad (6.35)$$

which is also unaffected by the load resistance.

From (6.17), (6.20), (6.27), (6.28), and (6.30), the ratio of  $L_X$  and  $L_1$  is determined uniquely as

$$\frac{L_X}{L_1} = -\frac{2\omega_1^3}{\pi(\omega_1^2 - 1)^2 \tan\left(\frac{\pi\omega_1}{2}\right)} - \frac{\omega_1}{2(\omega_1^2 - 1)} \approx 0.2662. \quad (6.36)$$

From the circuit analysis, it can be concluded that the design condition for the load-independent class-E power oscillator is to satisfy (6.8), (6.33), and (6.36). Also, the fact that the proposed power oscillator achieves the ZVS regardless of the load resistance can be verified using (6.17), (6.27), and (6.28) as

$$\begin{aligned} \frac{\partial v_S(\pi)}{\partial R_L} &= \frac{\partial v_S(\pi)}{\partial R_{eq}} \cdot \frac{\partial R_{eq}}{\partial R_L} \\ &= \frac{\partial}{\partial R_{eq}} \left\{ \left[ 2 + \frac{\pi\omega_1 \sin(\pi\omega_1)}{1 - \cos(\pi\omega_1)} \right] V_I \right\} \cdot \frac{\partial R_{eq}}{\partial R_L} \\ &= 0. \end{aligned} \quad (6.37)$$

#### 6.4.2.4 Circuit Characteristics

It is stated from (6.36) that the proposed power oscillator can be designed with arbitrary input inductance  $L_1$ . Therefore, a reasonable value of the inductance should be explored. Fig. 6.6 shows the circuit characteristics as functions of normalized inductance  $\omega_S L_1 / R_{Ld}$ , where  $R_{Ld}$  is the value of load resistance at the design point.

The power-output capability is calculated as

$$c_p = \frac{P_O}{V_{Smax} I_{Smax}} = \frac{V_{eq}^2}{2R_{eq} V_{Smax} I_{Smax}}, \quad (6.38)$$

where  $P_O$  is the output power, and  $V_{Smax}$  and  $I_{Smax}$  are peak values of the switch voltage and current, respectively. It can be seen from Fig. 6.6(a) that the maximum switch voltage monotonically decreases as the increase of  $L_1$ . Meanwhile, the maximum switch current monotonically decreases as the increase of  $L_1$ . Thus, we can find from (6.34) and (6.38) that certain  $L_1$  maximizes the power-output capability. We can see from Fig. 6.6(b) that the power-output capability is maximized to  $c_p = 1.02$  at  $\omega_S L_1 / R_{Ld} = 1.05$ .

## 6.5 Experimental Verification

The experimental verifications for the proposed power oscillator were performed under the specifications given in Table 6.1. We also conducted the experiment for the conventional class-E power oscillator under the same conditions. Based on the specifications, we selected GS61004B e-GaN HEMT from Infineon Technologies for the switching device  $S$ . From the datasheet, the maximum gate-to-source voltage and the threshold voltage were obtained as  $V_{Sm} = 7$  V and  $V_{th} = 1.7$  V, respectively. Thus, the amplitude of the gate-drive voltage was designed to be  $V_{gs} = 4$  V.

### 6.5.1 Circuit Design for Proposed Power Oscillator

The proposed power oscillator is designed based on the specifications. From the circuit analysis given in Section 6.4, closed-form design equations can be derived,

which determine all the component values uniquely. For designing the power oscillator to achieve the maximum power-output capability, the  $L_1$  should be determined as

$$L_1 = \frac{0.167R_{Ld}}{f_S} \approx 639 \text{ nH.} \quad (6.39)$$

From (6.33) and (6.39), the shunt capacitance  $C_1$  is obtained as

$$C_1 = \frac{0.0909}{f_S R_{Ld}} \approx 517 \text{ pF.} \quad (6.40)$$

From the specifications, we obtain

$$L_2 = \frac{Q_2 R_{Ld}}{f_S} \approx 1015 \text{ nH,} \quad (6.41)$$

and

$$L_3 = \frac{Q_3 R_{Ld}}{f_S} \approx 2347 \text{ nH.} \quad (6.42)$$

From (6.36) and (6.39), the extra inductance  $L_X$  is determined as

$$L_X = \frac{0.0445R_{Ld}}{f_S} \approx 170 \text{ nH.} \quad (6.43)$$

From (6.6) and (6.8), the capacitance  $C_2$  becomes

$$C_2 = \frac{0.0253}{f_S^2(L_2 - L_X)} \approx 652 \text{ pF.} \quad (6.44)$$

From (6.7) and (6.8), the capacitance  $C_3$  is

$$C_3 = \frac{0.0253}{f_S^2(L_3 - L_2 + L_X)} \approx 367 \text{ pF.} \quad (6.45)$$

From (6.2), (6.14), and (6.34), we obtain

$$C_{32} = \frac{0.0403V_I}{f_S^2 L_2 V_{gs}} \approx 6478 \text{ pF.} \quad (6.46)$$

As the capacitances  $C_{31}$  and  $C_{32}$  are connected in series, the capacitance  $C_{31}$  is obtained from (6.45) and (6.46) as

$$C_{31} = \frac{C_{32}C_3}{C_{32} - C_3} \approx 389 \text{ pF}. \quad (6.47)$$

Fig. 6.8 shows the bode plot of the LCCL filter obtained using (6.10) and (6.11), where the rated load resistance is specified as  $R_{Lr} = 25 \Omega$ . It can be seen that the filter can eliminate the harmonic frequencies, such as 13.56 MHz and 20.34 MHz, which is compatible with the assumption (iii) in the analysis. Additionally, the phase shift becomes  $-\pi/2$ , which is constant for different normalized load resistances at 6.78 MHz.

To implement the inductors, we used Mix 2 Iron-Powder Core from Micrometals. Fig. 6.9 shows the implemented load-independent class-E power oscillator. As seen from Fig. 6.9, the power oscillator requires only the main DC-supply voltage to perform DC to AC conversion, simplifying the implementation.

### 6.5.2 Experimental Results for Class-E Power Oscillator

Fig. 6.10 shows the experimental waveforms of the conventional class-E power oscillator, where the waveforms were measured by the MSO58 Mixed Signal Oscilloscope from Tektronix. We can see from Fig. 6.10 that the gate-drive voltage  $v_{gs}$  did not shape pure sinusoid, causing a voltage depression at the turn-OFF period. A similar observation has also been reported in [?] and is believed to be caused by the nonlinearity of the gate parasitic capacitance. As widely recognized, the allowable gate-voltage range of GaN e-HEMT is extremely narrow. Therefore, this operation could potentially damage the device. We can also observe that the switch voltage

achieved the ZVS for  $R_L/R_{Lr} = 1$ , as shown in Fig. 6.10(a). Although we tried to experiment with the operation for the case of  $R_L/R_{Lr} < 1$  a number of times, the waveforms could not be measured even at  $R_L/R_{Lr} = 0.9$  due to the instantaneous damage to the switching device. This is because a sudden reverse conduction occurred in the GaN e-HEMT at the turn-OFF period, which harmed the device. Therefore, we measured the operation for  $R_L/R_{Lr} = 2$ , as shown in Fig. 6.10(b). However, the switch voltage could not achieve the ZVS. Besides, the amplitude of the output current changed depending on the load resistance.

The experimental results show that the conventional class-E power oscillator cannot tolerate even small load variations, which significantly degrades the overall performance.

### 6.5.3 Experimental Results for Proposed Power Oscillator

Fig. 6.11 shows the superimposed experimental and analytical waveforms of the load-independent class-E power oscillator. We can see from Fig. 6.11 that the gate-drive voltage was purely sinusoid without the voltage depression compared with the conventional class-E power oscillator in Fig. 6.10. This is because the nonlinear gate capacitance was absorbed into the external capacitance  $C_{32}$ , mitigating the effect of the nonlinearity. We can also see that the ZVS was achieved regardless of the load resistance. Additionally, the output current maintained constant amplitude and phase shift. Moreover, the load-independent operation contributes to generating gate-drive voltage with constant amplitude and phase shift against load variations. Therefore, the proposed power oscillator maintained a stable oscillation against load

variations. The experimental and analytical waveforms were in good agreement, which demonstrated the validity of the experiment.

#### 6.5.4 Circuit Characteristics

Fig. 6.12 illustrates the output-current amplitude and efficiency as functions of load resistance for conventional and proposed power oscillator, where  $I_{mr}$  is the output-current amplitude in the rated condition. The power-conversion efficiency including the gate-drive losses was calculated as

$$\eta = \frac{P_O}{P_I} = \frac{R_L I_O^2}{2V_I I_I}, \quad (6.48)$$

where  $P_I$  and  $I_I$  are the input power and current, respectively.

It can be seen from Fig. 6.12 that the proposed power oscillator maintained a constant output-current amplitude against load variations. Additionally, the high power-conversion efficiency above 80 % was maintained within  $0.4 \leq R_L/R_{Lr} \leq 2$  due to the load-independent ZVS operation. The peak power-conversion efficiency was 87.4 % at  $R_L/R_{Lr} = 1.6$ .

The conventional power oscillator could not oscillate within  $R_L/R_{Lr} < 1$  due to the instantaneous damage of the switching device. Therefore, the circuit performance for  $1 \leq R_L/R_{Lr} \leq 2$  was evaluated. The output current fluctuated compared with the proposed power oscillator. Besides, the power-conversion efficiency was up to 82.8 % and decreased with the increase of load resistance.

From these results, we validated the load-independent operation of the proposed power oscillator, demonstrating its effectiveness.

## 6.6 Conclusion

This chapter has proposed the load-independent class-E power oscillator. The proposed power oscillator inherently achieves the ZVS regardless of the load resistance. Additionally, the amplitude and phase shift of both gate-drive voltage and output current are also independent of the load. These features enable the circuit to oscillate with high stability and efficiency over a wide range of load variations. The experimental results demonstrated the effectiveness of the proposed power oscillator.

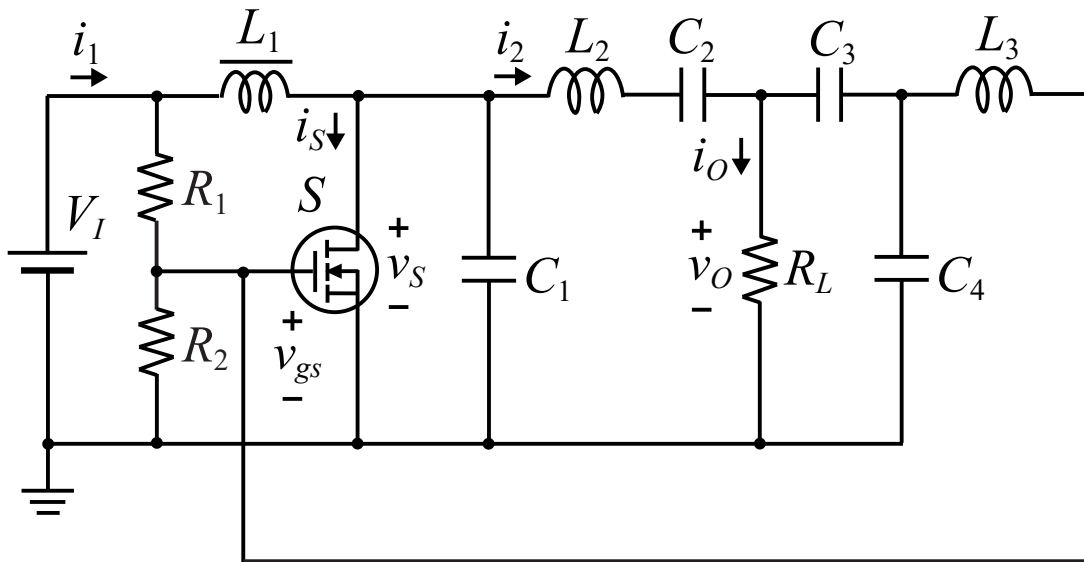


Fig. 6.1: Circuit topology of the conventional class-E power oscillator.

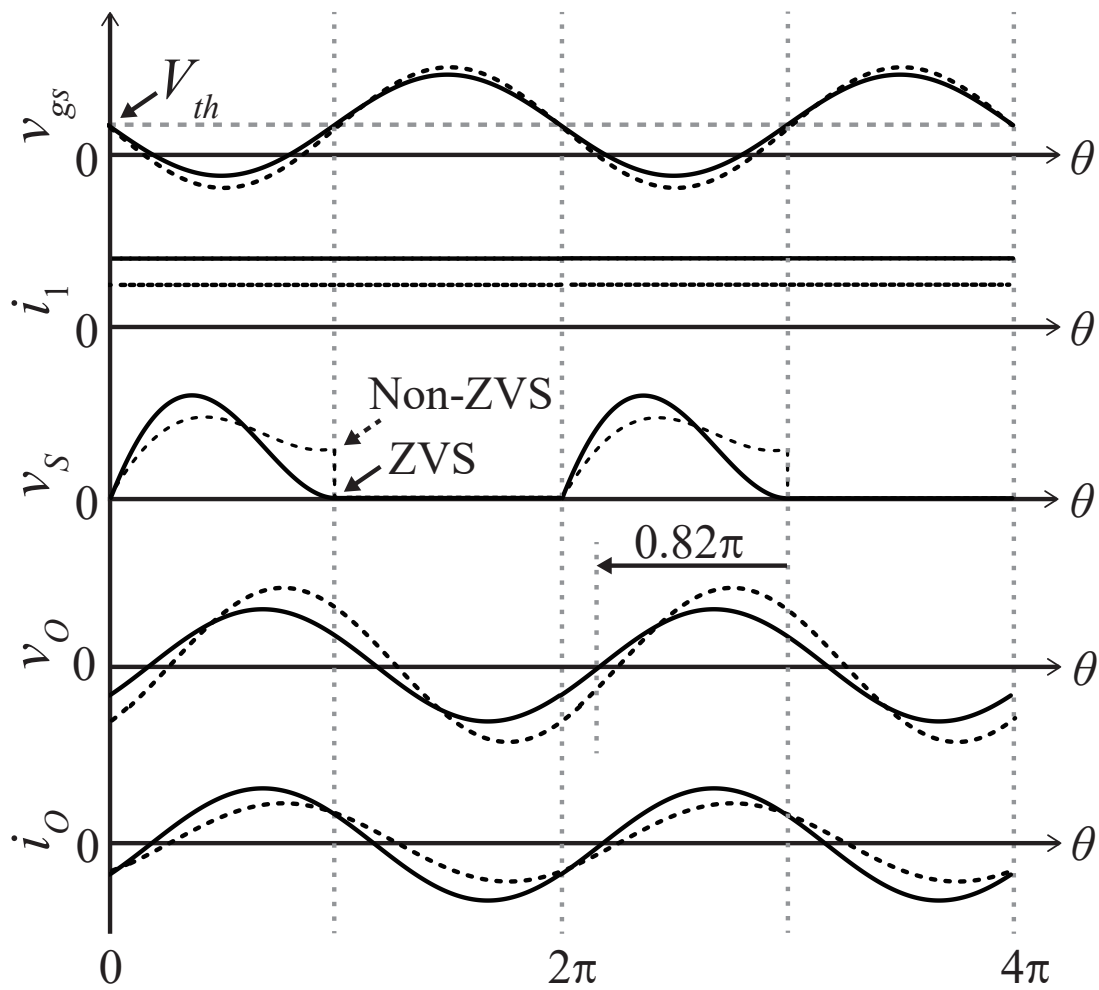


Fig. 6.2: Example waveforms of the conventional class-E power oscillator. (solid line: for the nominal state, dashed line: for load variations.)

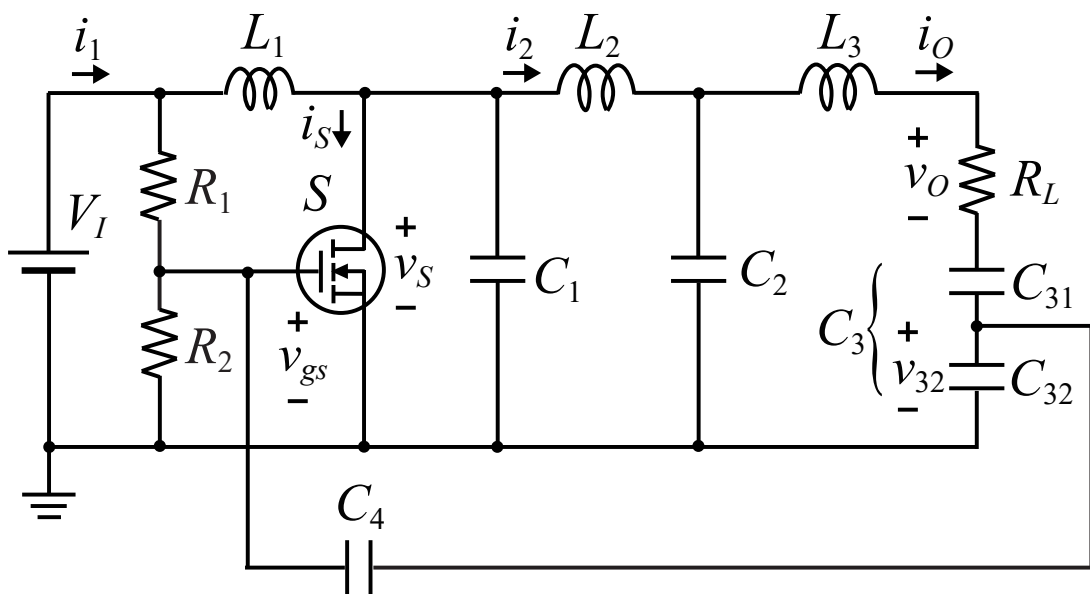


Fig. 6.3: Circuit topology of the load-independent class-E power oscillator.

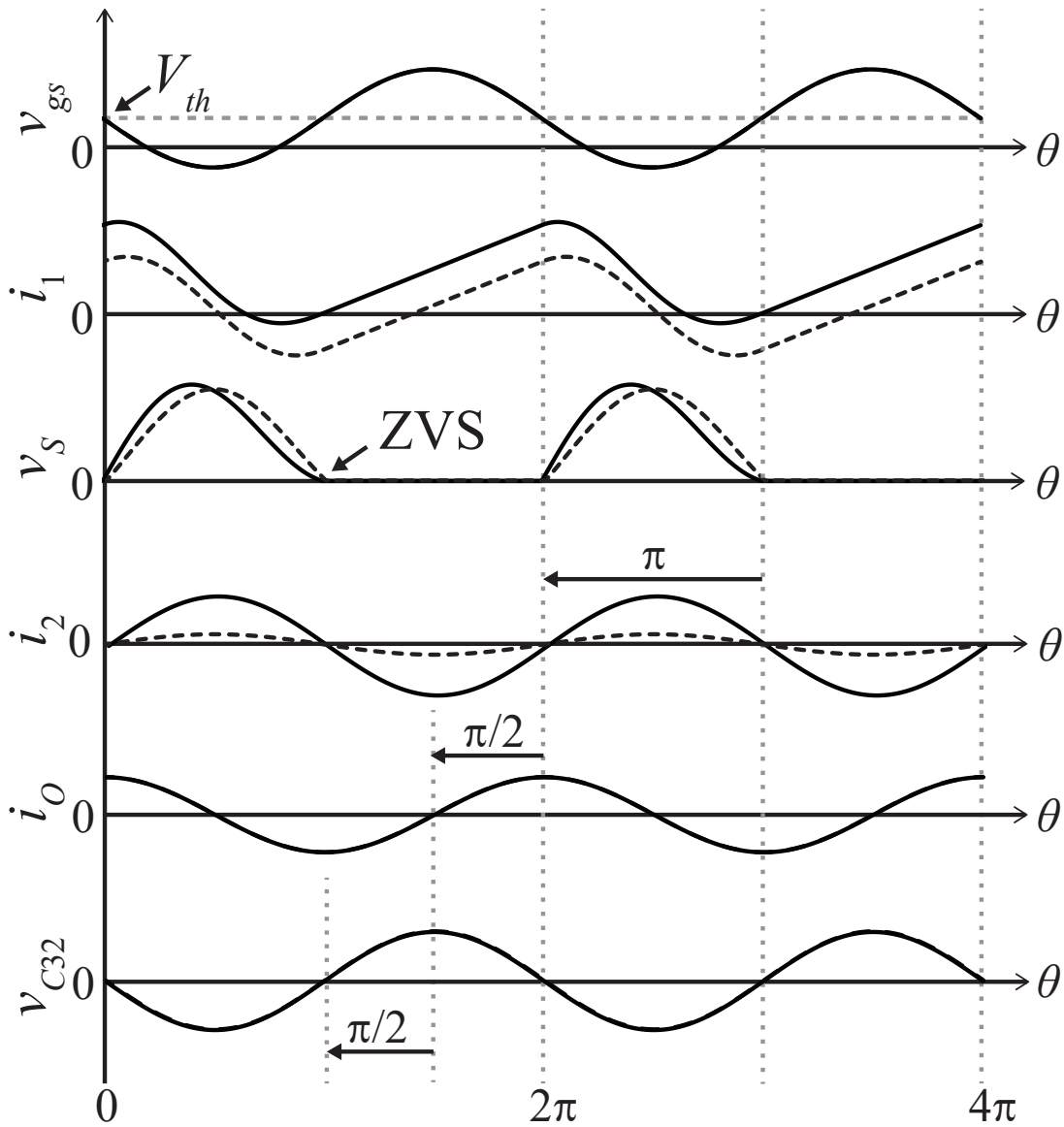


Fig. 6.4: Typical waveforms of the load-independent class-E power oscillator. (solid line:  $R_L/R_{Lr} = 1$ , dashed line:  $R_L/R_{Lr} = 0.1$ .)

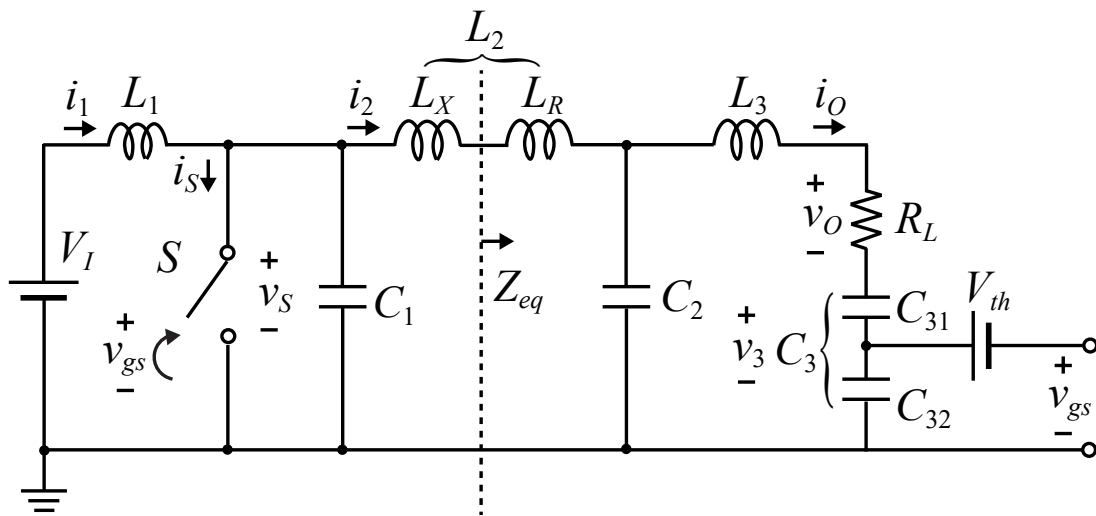


Fig. 6.5: Analytical circuit model of the proposed power oscillator. (a) Overall circuit. (b) Equivalent inverter model.

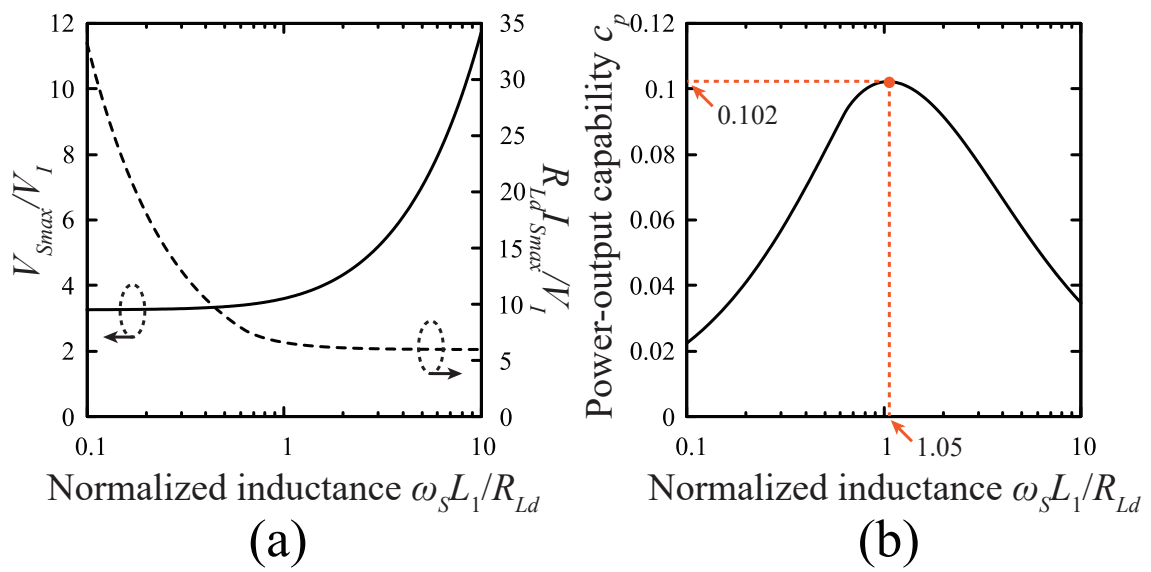


Fig. 6.6: Circuit characteristics as functions of normalized inductance  $\omega L_1 / R_{Lr}$ . (a) Normalized maximum switch voltage and current. (b) Power-output capability  $c_p$ .

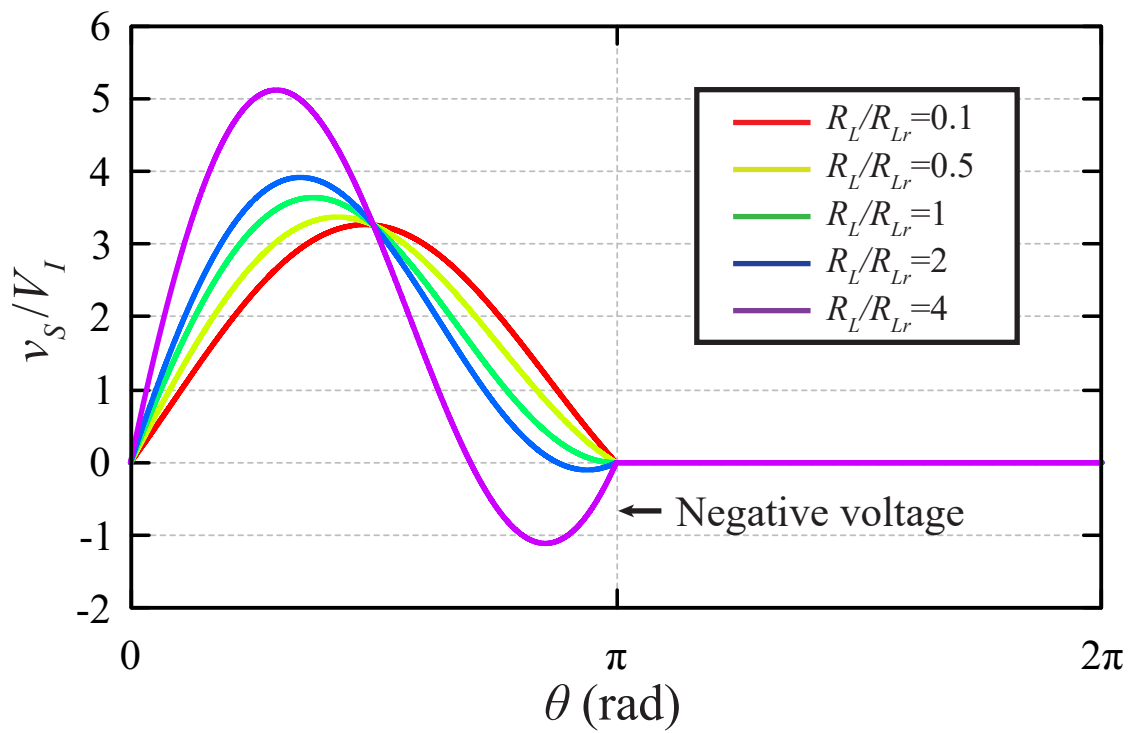


Fig. 6.7: Waveforms of the normalized switch voltage for fixed load resistances.

Table 6.1: The specifications for the experimental verifications.

Parameter	Specification
Input DC-voltage $V_I$	25 V
Oscillation frequency $f_S$	6.78 MHz
Load resistance at design point $R_{Ld}$	50 $\Omega$
Normalized inductance $\omega_S L_2 / R_{Ld}$	0.72
Normalized inductance $\omega_S L_3 / R_{Ld}$	5

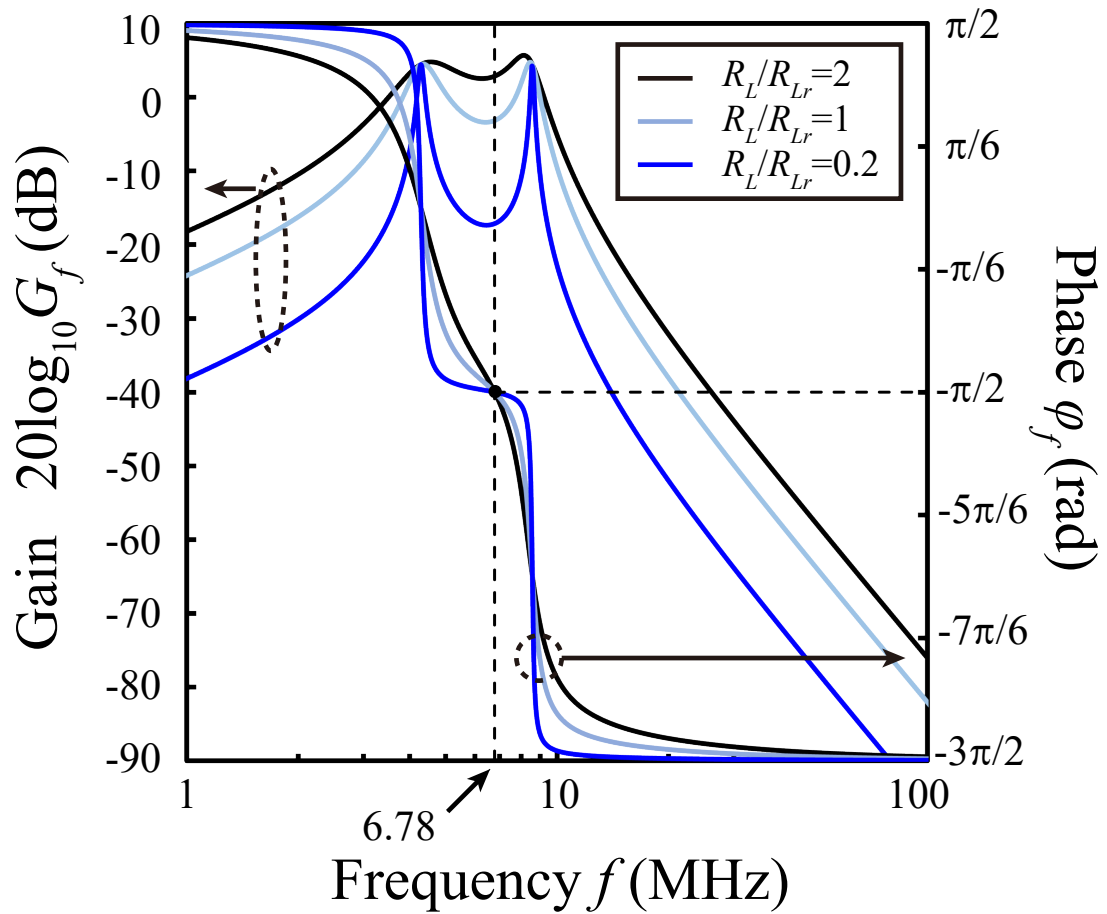


Fig. 6.8: Gain  $\log_{10} |I_O/V_{eq}|$  and phase of the LCCL filter as functions of the frequency.

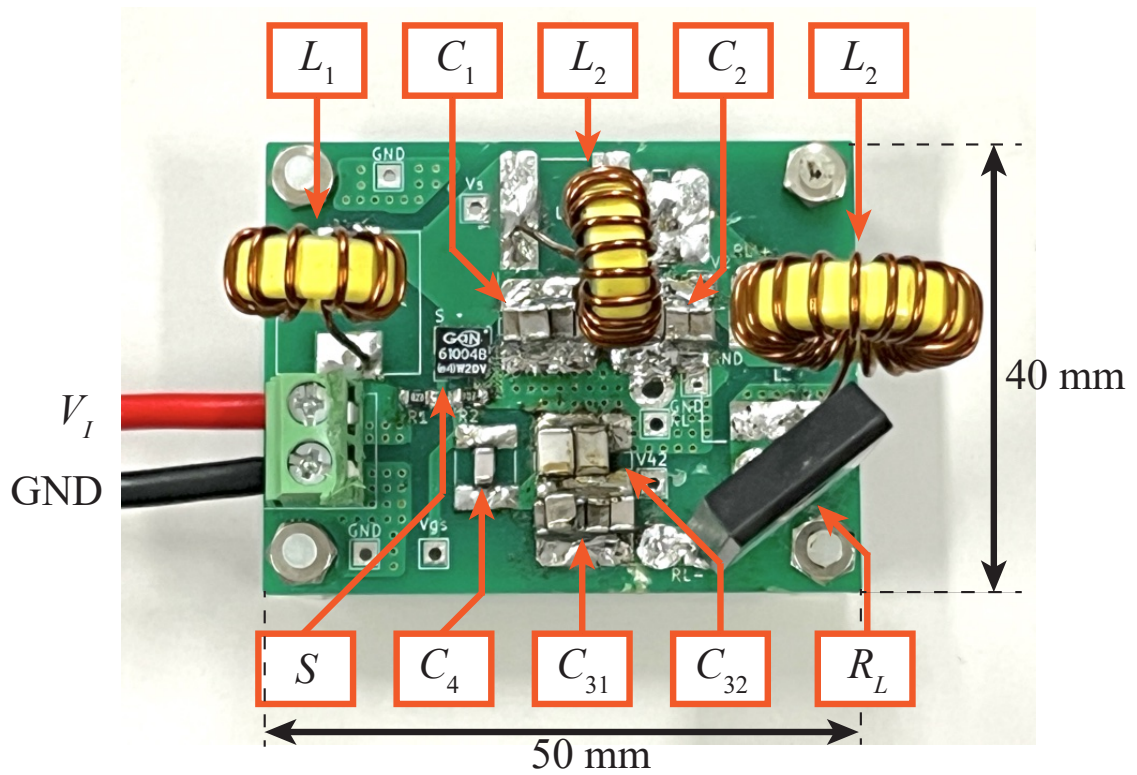


Fig. 6.9: Photo of the implemented load-independent class-E power oscillator.

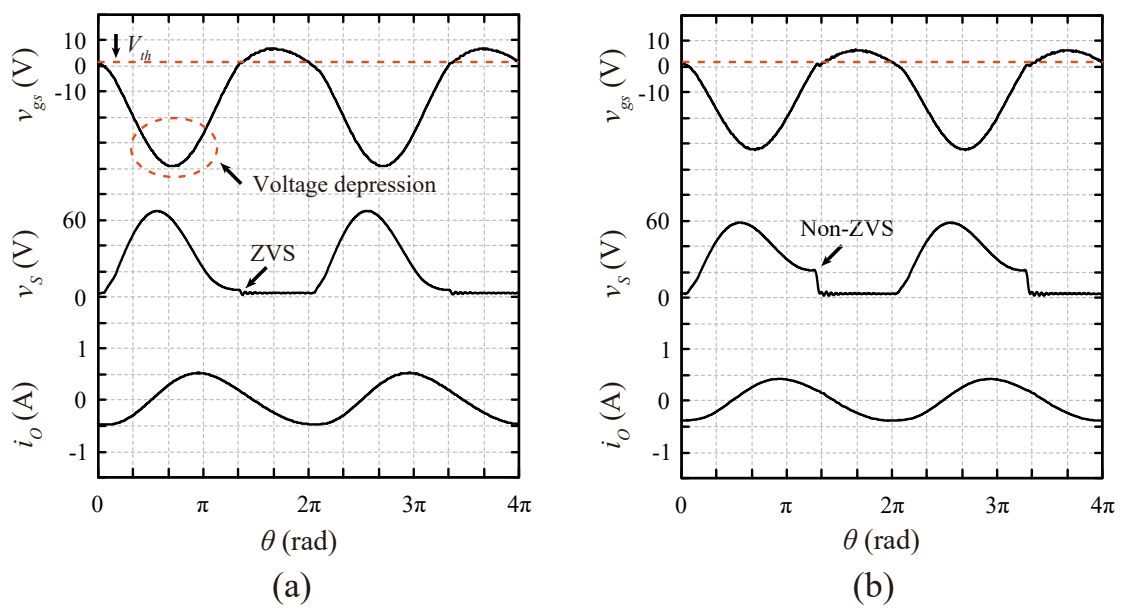


Fig. 6.10: Experimental waveforms of the conventional class-E power oscillator for fixed load resistance. (black:  $R_L/R_{Lr} = 1$ , blue:  $R_L/R_{Lr} = 1.2$ .)

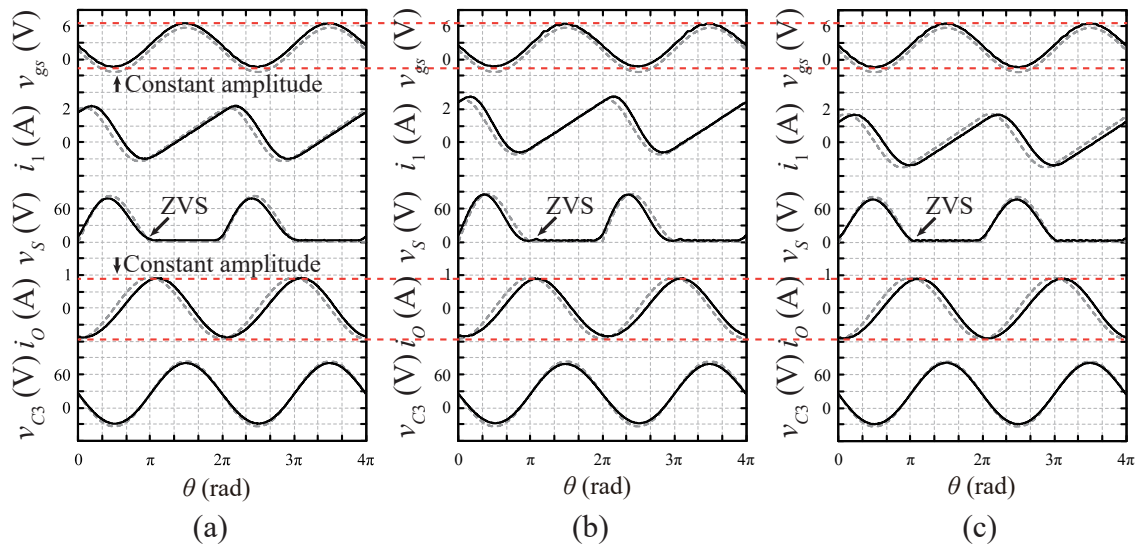


Fig. 6.11: Superimposed experimental and analytical waveforms of the load-independent class-E power oscillator for fixed load resistance. (solid line: experiment, dashed line: analytical.) (a)  $R_L/R_{Lr} = 1$ . (b)  $R_L/R_{Lr} = 0.5$ . (c)  $R_L/R_{Lr} = 0.1$ .

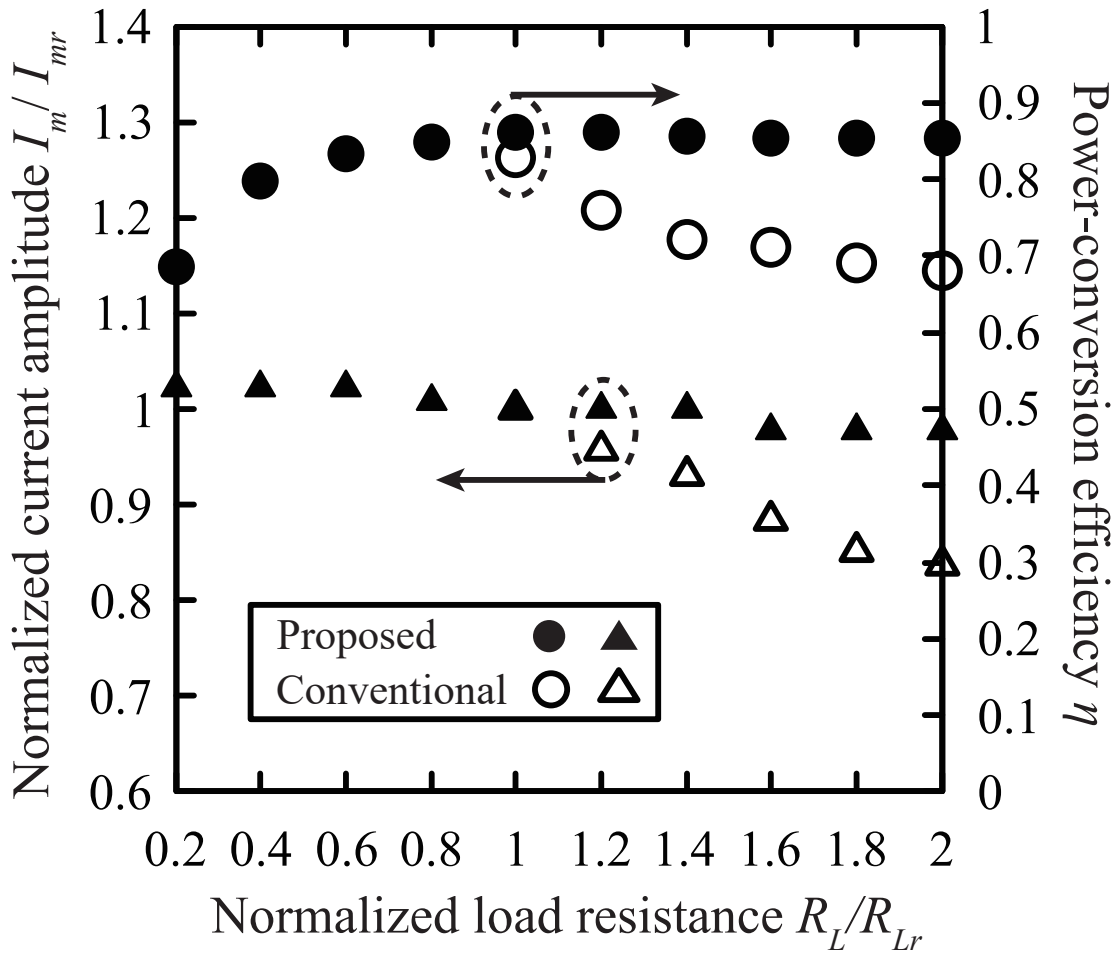


Fig. 6.12: Output-current amplitude  $I_m$  and power-conversion efficiency  $\eta$  as functions of load resistance  $R_L$ .

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## Chapter 7

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# Load-Independent Class-E Synchronous Rectifier

### 7.1 Introduction

The evolution in wide-bandgap power semiconductor devices has accelerated the development of power electronics circuits operating in the MHz regime. The high-frequency operation reduces the energy-storage requirements for the passive components, allowing the downsizing of the overall circuit. However, high-frequency operation increases the switching losses, making it essential to achieve ZVS. Furthermore, it is also crucial to address load variations in practical applications. Namely, the high-frequency circuits that satisfy the ZVS and the output regulation against load variations are in high demand.

The load-independent class-E rectifier [1–5] achieves the ZVS and constant output voltage against load variations without any specific control. The load-independent class-E rectifier exhibits a time-reversed dual operation with the load-independent class-E inverter [5–7]. Hence, in order to attain the load-independent operation in the rectifier, synchronous rectification with forced turn-off is required. However,

conventional load-independent class-E synchronous rectifiers [1–5] require accurate phase detection, which is challenging in the MHz operation. Besides, the additional digital devices cause propagation delay, complicating the circuit design. Therefore, this chapter aims to fundamentally address the challenges in high-frequency synchronous rectification by realizing synchronous rectification using only passive components.

This chapter proposes the load-independent class-E synchronous rectifier with a passive feedforward network. The proposed rectifier generates the synchronized drive voltage using the voltage across the resonant capacitor. Therefore, additional phase-detection circuits and digital devices are not required for the synchronous rectification. Moreover, the proposed synchronous rectifier achieves the ZVS and constant output voltage against load variations. The validity and effectiveness of the proposed rectifier are confirmed by the experiment.

## 7.2 Proposed Rectifier

Fig. 1(a) shows the circuit topology of the proposed rectifier, which is composed of the LCCL filter  $L_0 - C_0 - C_1 - L_1$ , shunt capacitor  $C_2$ , switching device  $S$ , finite inductor  $L_2$ , voltage-divide resistances  $R_1$  and  $R_2$ , filter capacitor  $C_f$ , DC-blocking capacitor  $C_3$ , and load resistance  $R_L$ . The capacitor  $C_0$  is divided into  $C_{01}$  and  $C_{02}$  to adjust the amplitude of the gate-drive voltage.

Fig. 1(b) shows the example waveforms for fixed load resistance, where  $\theta = 2\pi ft$  is the angular time and  $f$  is the operating frequency. Besides,  $R_{Lr}$  denotes the rated load resistance. The gate-drive voltage of the switching device is produced

using the voltage across the capacitor  $C_{02}$  for the phase information and the output voltage for the DC-bias voltage. The sinusoidal voltage across the capacitor  $C_{02}$  is delayed in phase by 90 degrees against the AC source. Also, the current  $i_1$  leads the AC source by 90 degrees. Therefore, the phase shift between the voltage across the capacitor  $C_{02}$  and the current  $i_1$  becomes just 180 degrees, which is consistent with the phase condition in the load-independent class-E rectifier [5]. Namely, the proposed rectifier realizes synchronous rectification using the phase information in the voltage across the capacitor  $C_{02}$ . The proposed rectifier realizes the synchronous rectification using only passive components, freeing it from accurate phase detection and consideration for the propagation delays caused by digital devices. Furthermore, the proposed rectifier achieves the ZVS and constant output voltage regardless of the load resistance when the current  $i_0$  is independent of the load, as shown in Fig.1 (b).

### 7.3 Circuit Analysis

The input resistance and capacitance of the load-independent class-E rectifier with a 50 % duty ratio can be obtained by applying the analysis in [1] as

$$R_E = 1.263R_L, \quad (7.1)$$

and

$$C_E = \frac{0.07155}{\omega}, \quad (7.2)$$

respectively. Hence, the proposed rectifier is transformed into the equivalent model, as shown in Fig. 2, where the feedforward network can be neglected to assume that

it has a high impedance at the operating frequency.

The input impedance of the proposed rectifier  $Z_{in}$  can be derived as

$$Z_{in} = \frac{R_E + j\{\omega C_1(\omega L_1 - \frac{1}{\omega C_E})[1 - \omega C_1(\omega L_1 - \frac{1}{\omega C_E})] - \omega C_1 R_E^2\}}{[1 - \omega C_1(\omega L_1 - \frac{1}{\omega C_E})]^2 + \omega^2 C_1^2 R_E^2} + j\left(\omega L_0 - \frac{1}{\omega C_0}\right). \quad (7.3)$$

The proposed rectifier is designed to have an input reactance which is independent of the load resistance. Therefore, the resonant conditions can be obtained as

$$\omega L_0 - \frac{1}{\omega C_0} - \frac{1}{\omega C_1} = 0, \quad (7.4)$$

and

$$\omega L_1 - \frac{1}{\omega C_1} = 0. \quad (7.5)$$

From (3) and (4), the input impedance of the proposed rectifier becomes

$$Z_{in} = \frac{1}{\omega C_1^2 (R_E + \frac{1}{j\omega C_E})}. \quad (7.6)$$

From (5), the output voltage of the proposed rectifier  $V_O$  can be obtained as

$$V_O = \omega C_1 \sqrt{\frac{R_E R_L}{2}} |\dot{V}_{in}| = 0.7948 \omega C_1 R_L |\dot{V}_{in}|. \quad (7.7)$$

## 7.4 Experimental Verifications

Fig.3 shows the circuit configuration of the WPT system using the proposed rectifier for experimental verification. We employ the load-independent class-E inverter for the transmitter and the proposed rectifier for the receiver. By using the load-independent class-E inverter and the S-S coupling, the amplitude and the phase

shift of current  $i_0$  can be independent of the load resistance [6]. The experimental specifications were given as  $V_I = 30$  V,  $f = 6.78$  MHz, and  $R_L r = 100\Omega$ . Table 1 gives the component values.

Fig. 4 shows the experimental waveforms of the proposed rectifier. We can see from Fig. 4(a) that the proposed rectifier was driven with the sinusoidal voltage, achieving synchronous rectification. We can also see from Fig. 4(a)-(c) that the voltage  $v_{S2}$  achieved the ZVS, and a constant output voltage was obtained against load variations.

Fig. 5 shows the output voltage and power-transfer efficiency as functions of the normalized load resistance. We can see that the consistent output voltage was obtained against a wide range of load variations. The maximum overall efficiency of 88.7 % was obtained at the rated condition.

## 7.5 Conclusion

This chapter has proposed the load-independent class-E synchronous rectifier with a passive feedforward network. The effectiveness of the proposed rectifier was confirmed by the experiment.

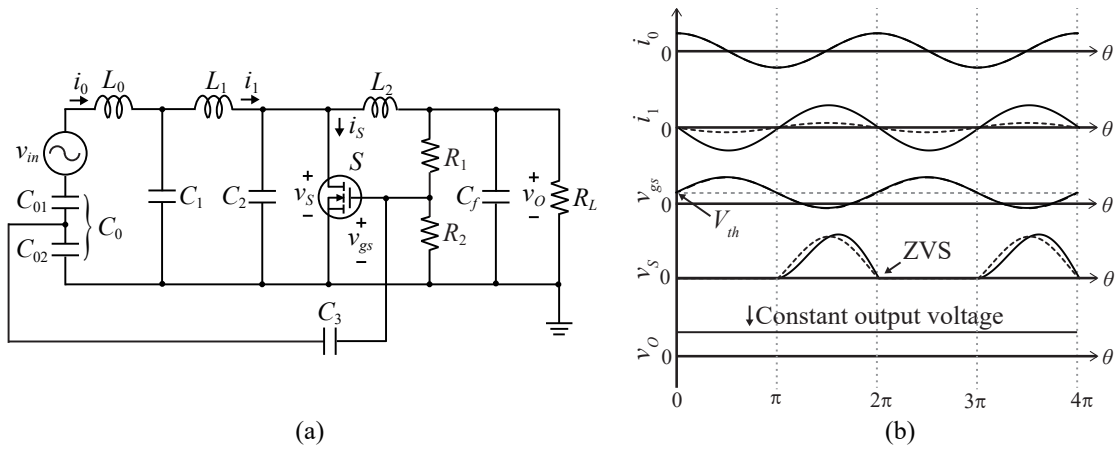


Fig. 7.1: Proposed rectifier. (a) Circuit topology. (b) Example waveforms for fixed load resistance (solid line:  $R_L/R_{Lr} = 1$ , dashed line:  $R_L/R_{Lr} = 10$ ).

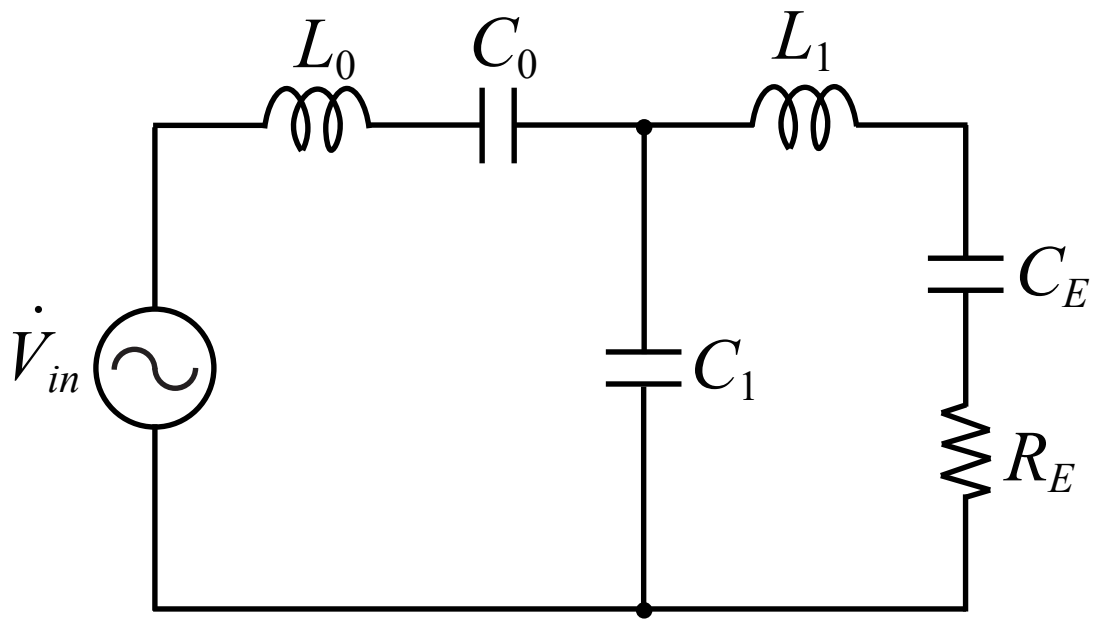


Fig. 7.2: Equivalent circuit model of the proposed rectifier.

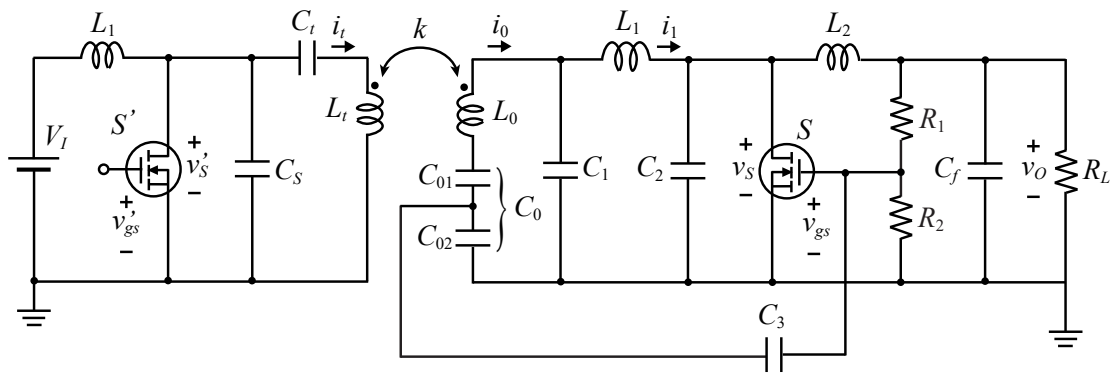


Fig. 7.3: Circuit configuration of the WPT system with the proposed rectifier for the experimental verifications.

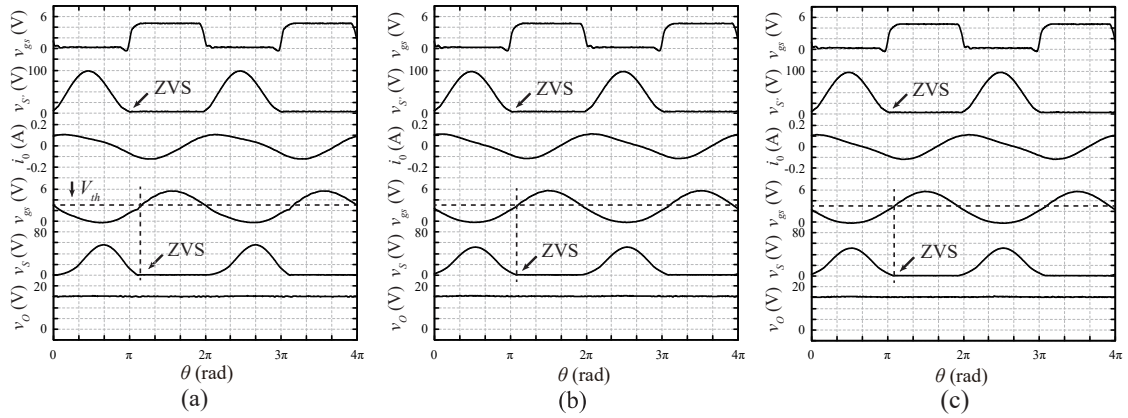


Fig. 7.4: Experimental waveforms of the WPT system with proposed rectifier for fixed load resistance. (a) For  $R_L/R_{Lr} = 1$ . (b) For  $R_L/R_{Lr} = 5$ . (c) For  $R_L/R_{Lr} = 10$ .

Table 7.1: Component values of the WPT system.

$L_I$	2.12 $\mu$ H	$C_t$	40.4pF
$L_t$	14.1 $\mu$ H	$C_{01}$	85.9pF
$L_0$	14.0 $\mu$ H	$C_{02}$	327pF
$L_1$	5.87 $\mu$ H	$C_1$	93.9pF
$L_2$	1.23 $\mu$ H	$C_2$	68.0pF
$k$	0.45	$C_3$	0.1 $\mu$ F
$C_S$	33.0pF	$C_f$	0.1 $\mu$ F

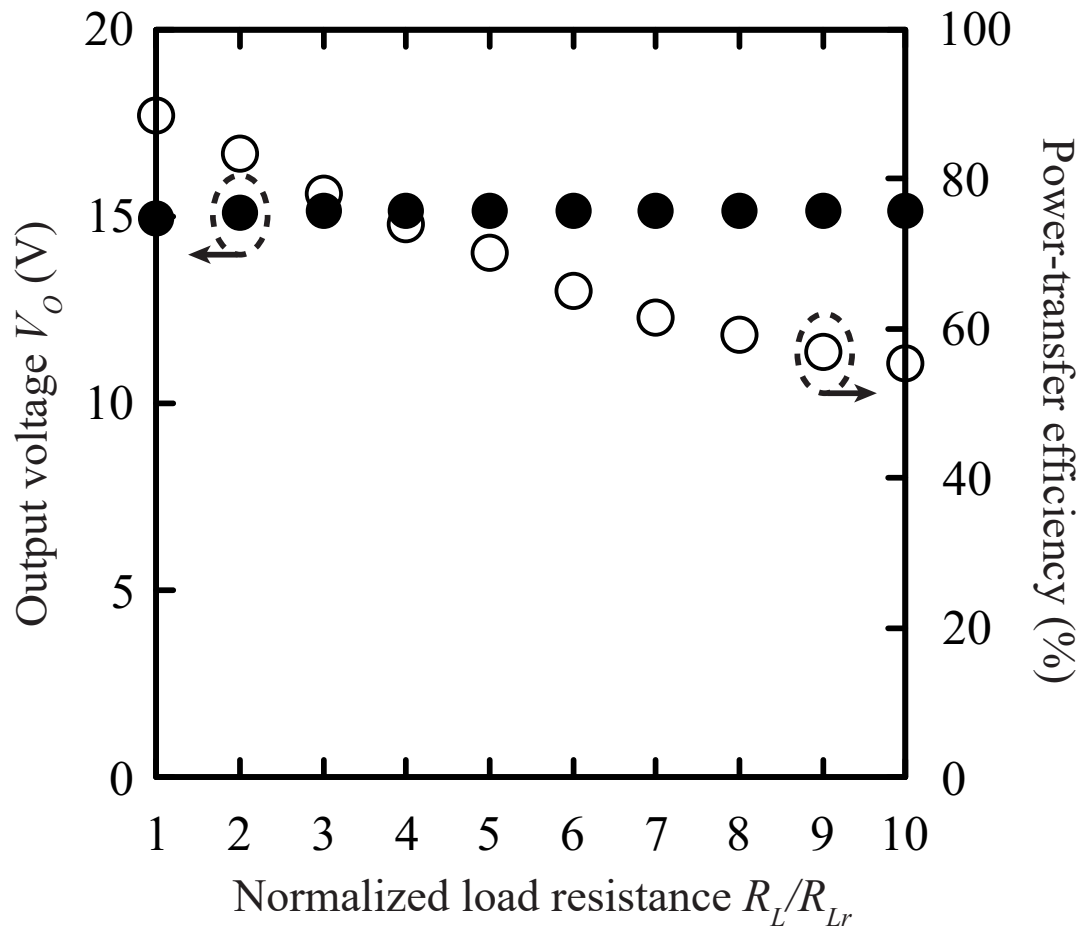


Fig. 7.5: Output voltage and power-transfer efficiency as functions of normalized load resistance.

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## Chapter 8

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# Overall Conclusion and Future Work

### 8.1 Overall Conclusion

This thesis presents high-frequency load-independent resonant circuits, including inverter, power oscillator, and synchronous rectifier. Several load-independent inverters have been proposed in this study. Furthermore, the load-independent design for the inverter is applied to power oscillators. By discovering the time-reversal duality between power oscillators and synchronous rectifiers, the load-independent design for power oscillators can also be applied to synchronous rectifiers. Consequently, it was demonstrated that the load-independent design for inverters can be extended to power oscillators and synchronous rectifiers.

Chapter 3 presents the analysis and design of the load-independent series resonant inverter with CC output, along with its WPT system application. The proposed inverter inherently achieves ZCS and a CC output regardless of the load resistance. Furthermore, the proposed inverter can generate a sufficiently pure sinusoidal output even with a low- $Q$  SR filter. In the experiment, the WPT system that incorporates

the proposed inverter as the transmitter was implemented.

Chapter 4 has proposed the design of the load-independent class- $\Phi_3$  inverter. The load-independent class- $\Phi_3$  inverter achieves the ZVS and constant AC output voltage regardless of the load resistance. Additionally, it achieves higher efficiency and power-output capability than the load-independent class- $\Phi_2$  inverter. In the experiment, the load-independent class- $\Phi_3$  inverter achieved 87.5 %-95.9 % power-conversion efficiency within a tenfold change in the load resistance, showing the effectiveness of the proposed inverter.

Chapter 5 has proposed the self-tuned series resonant power oscillator with LI operation. The proposed oscillator maintains high efficiency and constant AC output even with load variations and component tolerances. The experimental results show the effectiveness of the proposed power oscillator.

Chapter 6 has proposed the load-independent class-E power oscillator. The proposed power oscillator inherently achieves the ZVS regardless of the load resistance. Additionally, the amplitude and phase shift of both gate-drive voltage and output current are also independent of the load. These features enable the circuit to oscillate with high stability and efficiency over a wide range of load variations. The experimental results demonstrated the effectiveness of the proposed power oscillator.

Chapter 7 has proposed the load-independent class-E synchronous rectifier with a passive feedforward network. The proposed rectifier generates the synchronized drive voltage using the voltage across the resonant capacitor. Therefore, additional phase-detection circuits and digital devices are not required for the synchronous rectification. Moreover, the proposed synchronous rectifier achieves the ZVS and constant output voltage against load variations. The validity and effectiveness of

the proposed rectifier are confirmed by the experiment.

Chapter 8 shows the conclusion of this thesis. Additionally, future research topics are introduced in this section.

## 8.2 Future Work

Thus far, load-independent design has been applied to fundamental power electronics circuits, such as DC-AC converters and AC-DC converters. In the future, I plan to research DC-DC converters and WPT systems, which combine these basic circuits. In particular, the synchronous rectifier proposed in this study does not require auxiliary power supplies or additional digital devices, making it highly suitable for application on the secondary side of WPT systems. Furthermore, there are a few examples of WPT systems utilizing power oscillators, and this is one of the areas I want to explore in the future.

# Research achievements

## Academic journal papers

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## Invited Lecture

- **Y. Komiyama**, W. Zhu, A. Konishi, K. Nguyen, and H. Sekiya, "Load-Independent Class-E Power Oscillator and Synchronous Rectifier", IEEE Workshop on Nonlinear Circuit Networks (NCN2024), Tokushima, Japan, Dec. 2024.

## Patents

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